Third-harmonic generation enhancement in an ITO nanoparticle-coated microresonator

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Abstract: We report a ∼3-fold enhancement of third-harmonic generation (THG) conversion efficiency using indium tin oxide (ITO) nanoparticles on the surface of an ultra-high-Q silica microsphere. This is one of the largest microcavity-based THG enhancements reported. Phase-matching and spatial mode overlap are explored numerically to determine the microsphere radius (∼29 µm) and resonant mode numbers that maximize THG. Furthermore, the ITO nanoparticles are uniformly bonded to the cavity surface by drop-casting, eliminating the need for complex fabrication. The significant improvement in THG conversion efficiency establishes functionalized ITO microcavities as a promising tool for broadband frequency conversion, nonlinear enhancement, and applications in integrated photonics.

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1. Introduction

Whispering-gallery-mode (WGM) microresonators have garnered much interest due to their optical mode confinement and ability to effectuate strong nonlinear interactions on compact, low-power devices [1–5]. Applications in high-precision sensing [6,7], optical communications [8,9], and non-classical light generation [10,11] have all seen remarkable advancements as a result of the increased light-matter interaction length provided by microresonators. Many applications utilize third-order nonlinear effects such as four-wave mixing [12,13], stimulated Raman scattering [14,15], stimulated Brillouin scattering [16,17], and third-order sum frequency generation [18,19], which have all been studied in a wide variety of resonator geometries [20–23]. However, the efficiency of third-order nonlinear processes is severely constrained by the low $\chi^{(3)}$ susceptibility in common optical materials, such as silica. Functionalized microcavities offer a novel solution to this problem, providing a way to substantially increase the Kerr nonlinearity ($n_2$) of a resonator and thereby enable high-efficiency interactions [24–26].

Silica microspheres are particularly useful in the study of third-order nonlinear effects due to their ultra-high quality factors and relative ease of fabrication [27,28]. Silica is frequently used as a resonator material due to its favorable optical properties in the near-infrared region, i.e. ultra-low material absorption and inversion symmetry that prohibits the generation of competing $\chi^{(2)}$ effects. Despite the many advantages of silica, its $n_2$ is low (2.2-2.7 × 10^{-20} m^2/W) [29,30], and is not sufficient for facilitating strong nonlinear effects at low pump powers [31]. Recent developments in functionalized microcavities provide a solution to this problem by exploiting the optical properties of highly nonlinear materials to substantially increase the $n_2$ of a microresonator [24–26,32]. By coating the microresonator surface with highly nonlinear, functionalized organic molecules, high-efficiency nonlinear interactions can be realized while retaining the material benefits of silica [33]. Few molecules have been extensively studied for cavity functionalization, and uniform coating is typically achieved through relatively complex fabrication methods such as
chemical vapor deposition, spin-coating, or sputtering [24–26,32]. Due to the small diameter of the ITO nanoparticles (≈9 nm), the application method of drop-casting can be used to achieve uniform surface-coating [34], avoiding the need for specialized fabrication equipment.

In this research, we use indium tin oxide (ITO) nanoparticles on the surface of an ultra-high-$Q$ silica microsphere to demonstrate a $\sim 3$-fold enhancement in third-harmonic generation. Bulk ITO has an exceptionally high $n^2$ at its epsilon-near-zero wavelength (more than 10,000 times greater than the $n^2$ of pure silica) [35]. Strong conductivity and optical transparency in the visible spectrum make ITO an attractive material for many applications [36], but large absorption near the Mie resonance has prevented bulk ITO from becoming a primary material in high-$Q$ microresonators. However, ITO nanoparticles have been shown to provide the desired nonlinearity of bulk ITO while minimizing the associated absorption loss [37]. Here, we achieve a microresonator that possesses both a high $n^2$ and a high $Q$-factor for enhanced nonlinear effects.

2. Third-harmonic generation

Third-harmonic generation (THG) and third-order sum frequency generation (TSFG) occur when three pump photons annihilate to become one photon at a higher frequency. In the degenerate case (THG), each pump photon is of equal frequency, such that $\omega_T = 3\omega_P$, where $\omega_T$ is the angular frequency of the generated photon and $\omega_P$ is the angular frequency of the pump photon. In the non-degenerate case (TSFG), two of the three pump photons become Raman Stokes photons, such that $\omega_T = \omega_P + \omega_{RS,1} + \omega_{RS,2}$, where $\omega_{RS,1}$ and $\omega_{RS,2}$ are the Raman Stokes photons. Phase-matching conditions must be satisfied in order for THG or TSFG to occur. In a microcavity, phase-matching requires the effective index of the pump mode and THG mode to be equal. In order to fulfill this requirement, the dispersion profile of a WGM can be exploited to compensate for the effective index mismatch between the pump and THG modes. Due to the large difference between the pump and THG wavelengths, excitation of higher-order THG modes is necessary to match the effective indices.

Here, numerical simulations are performed using COMSOL Multiphysics [38] to determine the ideal silica microsphere radius that will satisfy phase-matching conditions and maximize spatial overlap between the pump and THG modes. A finite-difference eigenmode solver is used to find the effective indices corresponding to the pump (1550 nm) and THG (516.6 nm) eigenfrequencies of a pure silica sphere. Simulation results in Fig. 1 show the effective index of the resulting pump and THG modes as a function of microsphere radius. The intersection of the pump and higher-order THG modes indicate phase-matched radii that enable strong THG. A sphere radius range of 26 $\mu$m to 35 $\mu$m is chosen to provide a good balance between the quality factor and circulating power density in the cavity [39,40].

For efficient THG conversion in a microsphere, phase-matching of higher-order pump modes and THG modes is crucial. Thus, pump modes with a polar mode number $l$ between 1 and 8 are examined to provide a range of possible interactions. For the phase-matched modes, spatial overlap is calculated to identify the microsphere radius that will generate the strongest THG [see Table 1]. The modal overlap factor is given by [41]:

$$\xi = \frac{\int \int dr dz |E_{az}(r, z)|^2 E_{bz}(r, z)}{\left(\int \int dr dz |E_{az}(r, z)|^2\right)^{1/2} \left(\int \int dr dz |E_{bz}(r, z)|^2\right)^{1/2}}.$$  \hspace{1cm} (1)

where $E_{(a,b)z}(r, z)$ is proportional to the z-component of the electric field distribution for the optical modes in the microsphere.

Spatial overlap depends on the distribution of the radial, polar, and azimuthal fields. Simulation results show mode overlap increasing proportionally to the polar mode number. The strongest overlap factor of $\sim 0.3$ occurs for the higher-order pump mode ($l = 8$; $n = 1$) and THG mode ($l = 27$; $n = 1$), corresponding to a sphere radius of 29.77 $\mu$m. Mode profiles for phase-matched
Fig. 1. Effective index as a function of radius for a pure silica microsphere. Fundamental \((l = n = 1)\) and higher order \((l = 4, 8; 1 \leq n \leq 3)\) TE pump modes at 1550 nm are tracked alongside higher-order THG modes \((3 \leq l \leq 27; 1 \leq n \leq 3)\) at 516.16 nm. Phase-matching between the pump modes and THG modes is achieved at intersection points \(i-vi\).

modes \(i\) and \(iii\) are plotted in Figs. 2(a) and 2(b) respectively, showing \(|E_{a,z}|^2\) of the pump mode (left), \(|E_{b,z}|^2\) of the phase-matched THG mode (middle), and the overlap of the two modes (right). The overlap profile is calculated using \(E_{a,z}(r,z)^3 \times E_{b,z}(r,z)\).

Fig. 2. (a) Overlap profile (right) for a phase-matched fundamental pump mode (left) and higher-order THG mode (middle) [point \(i\) - Fig. 1], corresponding to a radius of 28.81 \(\mu m\) and mode overlap factor of 0.1543. (b) Overlap profile (right) for a phase-matched higher-order pump mode (left) and higher-order THG mode (middle) [point \(iii\) - Fig. 1], corresponding to a radius of 29.77 \(\mu m\) and overlap factor of 0.3058. The overlap is calculated using \(E_{a,z}(r,z)^3 \times E_{b,z}(r,z)\).
| Table 1. Mode overlap factor and radius for phase-matched modes |
|-----------------|-------|-------|-------|-------|-------|-------|
| i               | ii    | iii   | iv    | v     | vi    |
| $R$ (µm)        | 28.81 | 29.30 | 29.77 | 32.38 | 32.59 | 33.41 |
| $\xi$           | 0.1543| 0.2134| 0.3058| 0.1121| 0.2091| 0.1875|

Based on the results of our phase-matching simulations, mode overlap calculations, and previous research on silica microspheres [19,24], a sphere radius of $\sim 29$ µm is used in the experiment. Phase-matching conditions for the ITO-coated sphere are expected to be minimally impacted due to the small diameter of the nanoparticles and the small volume fraction of ITO/silica ($\sim 10^{-8}$).

3. Experimental design

We use a continuously tunable diode laser (Toptica CTL 1550) followed by a polarization controller as a 1550 nm pump. The light is amplified using an erbium-doped fiber amplifier and launched into a tapered fiber. The field in the tapered fiber is evanescently coupled to the microsphere, with the output of the tapered fiber connected to an InGaAs photodetector (Newport 1811-FC). The resonator is mounted on a 3-axis translation stage (Thorlabs MAX313D) with 20 nm precision and imaged with a CCD camera [Fig. 3(a)]. For coupling to the microsphere, we fabricate a silica tapered fiber, with a waist diameter of $\sim 800$ nm, using motorized stages and a butane heat source. Mode-hop-free wavelength scanning is performed through piezo-actuation of the laser cavity and modulated by a triangle waveform. The silica microsphere is fabricated by applying arc discharges in a fiber fusion splicer to one end of a half-tapered fiber. The size of the sphere radius is controllable from 20 µm to 100 µm, determined by the initial size of the half-tapered fiber end and the number of arc discharges applied.

![Fig. 3.](image)

(a) Experimental setup for the third-harmonic generation. A 1550 nm pump is generated by a continuous-wave laser, amplified, and launched into a tapered silica fiber. A 60 µm core fiber probe collects the scattered THG light from the microsphere surface. The transmission of the silica fiber is measured on an oscilloscope to ensure the desired coupling condition between the sphere and tapered fiber. (b) Diagram of drop-casting method used to coat the surface of the silica microsphere with ITO nanoparticles. A transmission electron micrograph image of ITO nanoparticles is shown in the upper right corner of (b). An average nanoparticle diameter of 9.1 ± 2.7 nm is used to enhance nonlinearity and minimize absorption loss.

The ITO nanoparticles are synthesized to have an average diameter of 9.1 ± 2.7 nm (measured using an electron micrograph image [Fig. 3(b)]) to maximize nonlinear enhancement and minimize scattering loss. At this diameter, the Mie resonance of the particle is tuned to match...
the measurement wavelength (1550 nm), providing maximum local electric field enhancement and increased nonlinearity. Larger nanoparticles (~30 nm diameter) were previously shown [37] to produce smaller enhancement and result in a lower $Q$-factor due to the increase in scattering loss. The nanoparticles are then diluted in a toluene colloidal solution to ensure the desired concentration on the sphere surface, and bonded to the silica sphere by method of drop-casting [see Fig. 3(b)]. The sphere is positioned upright during the application to avoid clumping of nanoparticles on the surface that can increase scattering and reduce the $Q$-factor. A single drop-coating of the solution is used to provide a good balance of nonlinear enhancement while retaining a high $Q$-factor. Additional coatings were previously shown [37] to provide a further increase in nonlinearity but resulted in substantially more absorption and a greatly reduced $Q$-factor.

4. Results

THG power in the microresonator is collected with a 60-micron core multi-mode fiber positioned near the surface of the microsphere. The multi-mode fiber is connected to a spectrometer from which the THG spectra are acquired continuously at the rate of 1000/s with a laser scan rate of 50 Hz. For each input pump power, the resulting THG spectra are integrated and averaged to provide the final value of THG output power. As seen in Fig. 4, the ITO-coated sphere produces an average increase in THG power of 186 ± 24%, with a maximum increase of 256% occurring at 5 mW of pump power. Cubic power dependence of the THG output is observed using pump powers from 2.5 mW to 7.5 mW [see Fig. 4(b)].

![Fig. 4. (a) THG power as a function of pump power for a silica microsphere before and after application of ITO nanoparticles. The ITO-coated sphere shows an average increase of 186 ± 24% over the pure silica sphere. (b) Log-log plot of THG power as a function of input pump power. Cubic dependence is observed for both the coated and uncoated sphere as indicated by the ∼3 coefficient for the slope of the linear fit.](image)

The standard deviation of THG power is shown to increase proportionally to pump power as seen in the error bars of Fig. 4(a). This is likely due to increased thermo-optic effects at higher pump powers. In the presence of high intensity optical fields, large changes in temperature can induce a deviation in the circulating optical path which perturbs the resonance [42].

The power intensity of THG scales cubically in relation to pump power [18]. In Fig. 4(b), the 0.11 and 0.18 deviation from the theoretical slope coefficient of 3 is likely due to uncertainty in the lower bound of the power measurements which were slightly above the noise floor of the spectrometer. At pump powers greater than ∼8 mW, competing nonlinear effects such as Raman
scattering begin to dominate. When this occurs, energy in the pump photons is lost and the power relation between the pump input and THG output trends toward a linear dependence [19].

Optical microscope images of the pure silica sphere and ITO-coated microsphere are shown in Fig. 5(a). The images are captured at 5 mW of pump power, corresponding to a 256% increase in measured THG output. Spectrum measurements that correspond to the THG images in Fig. 5(a) are shown in Fig. 5(b), where THG power is measured at 519.05 nm. For a pump wavelength of 1554.45 nm, the theoretical THG wavelength is 518.15 nm, indicating an experimental variance of 0.17%. The deviation of 0.17% from the theoretical value is likely due to the optical resolution of the spectrometer and lack of calibration with respect to the laser.

![Fig. 5.](image)

The same silica sphere is used for both coated and uncoated measurements, and coupling conditions are carefully replicated for each sphere with the aid of camera images and monitoring of the tapered fiber transmission spectrum. Both the pure silica sphere and coated sphere are critically coupled when THG data is collected. By tuning the wavelength at a given pump power, we are able to excite the same modes in the coated and uncoated spheres to ensure an accurate comparison. As pump power is increased, the pump wavelength is adjusted accordingly to counteract this thermally induced resonance shift, ensuring the double resonance condition of the pump and THG modes is maintained [24].

At higher pump powers, competing nonlinear effects such as stimulated Raman scattering (SRS), cascaded Raman scattering (CRS), and parametric oscillation can occur [40,43]. SRS occurs when the inelastic scattering of pump photons generates optical phonons, resulting in pump photons of lower energy. As an intrinsically phase-matched process, SRS often becomes the dominant effect in a microcavity when the threshold is exceeded. TSFG due to SRS and CRS in an ITO-coated sphere is shown in Figs. 6(a) and 6(b) respectively, where the summation of reduced energy photons and pump photons results visible emissions at wavelengths longer than the THG wavelength. For example, the spectrum in Fig. 6(a) is the result of one pump photon at 1549 nm and two Raman Stokes photons at 1667 nm summing to form one photon at 542 nm.

In a WGM microresonator, the efficiency of nonlinear processes is greatly impacted by the quality factor of the device. For THG, the converted power scales proportionally to \((Q/V)^3\), where \(Q\) is the quality factor and \(V\) is the optical mode volume [18]. Here, \(Q\)-factor data is extracted from the power transmission of the tapered fiber using the cavity ringdown method [44–46]. By fitting the decay envelope of the ringdown signal, we determine the decay constant \(\tau\) and use the
relation \( Q = \frac{\pi c \tau}{\lambda} \) to calculate the \( Q \)-factor. At \( \sim 20 \mu W \) of pump power, measurements are taken for both the pure and coated microspheres. Ringdown is measured when the microsphere is weakly coupled to the taper to reduce the presence of thermal effects. The pure silica sphere is determined to have a \( Q \)-factor of \( 2.5 \times 10^8 \) while the coated sphere has a \( Q \)-factor of \( 3.6 \times 10^7 \), resulting in a reduction factor of 6.94 [see Fig. 7].

The relation between \( Q \)-factor and \( n_2 \) plays an important role in determining the ideal volume fraction of ITO/silica to maximize nonlinear effects. An increase in nonlinearity can potentially be outweighed by the corresponding reduction in \( Q \)-factor as seen in the figure of merit (\( Q \times n_2 \)) comparisons in [37]. In this previous work, the \( n_2 \) of a similarly sized ITO-coated and pure
silica sphere was shown to be $7.2 \times 10^{-19}$ m$^2$/W and $1.8 \times 10^{-20}$ m$^2$/W respectively, indicating that the ITO nanoparticles contribute $7.02 \times 10^{-19}$ m$^2$/W to the total $n_2$ of the coated sphere. However, this 40-fold increase in $n_2$ does not yield a similar increase in nonlinear effects as only a small fraction of the mode volume interacts with the nanoparticles on the surface of the sphere. Furthermore, this increase in $n_2$ is offset by a 10-fold reduction in $Q$-factor due to increased absorption, resulting in an overall 3-fold increase in nonlinear effects. These results are in excellent agreement with the experimental results presented here.

$Q$-factor measurements can be used in conjunction with the nonlinear coupling strength $g$ to approximate THG conversion efficiency. When phase matching conditions are satisfied, the azimuthal mode numbers of the pump and THG modes $m_a$ and $m_b$ are related by $3m_a \approx m_b$, and the mode overlap factor $\xi$ [see Table 1] can be used to approximate $g$. The mode overlap for the coated sphere is expected to be similar to that of the pure sphere given the small volume fraction of the ITO, so the maximum mode overlap factor of 0.3058 for a sphere radius of 29.77 µm is used here to evaluate $g$. In the case of critical coupling and zero detuning, nonlinear coupling strength is approximated by [41]:

$$g \approx \frac{\xi \sqrt{3} \hbar \omega_0^2 \chi^{(3)}(r)}{\epsilon_0 4\pi R \sqrt{\epsilon_0 \epsilon_b}} \delta(3m_a - m_b),$$  

(2)

where $\omega_0$ is the angular frequency of the pump mode, $R$ is the resonator radius, and $\epsilon_{a(b)}$ is the relative permittivity of the sphere for the pump (visible) light. The third-order nonlinear susceptibility of the resonator must account for both the silica sphere and the ITO nanoparticles. Using the estimated effective $n_2$ of $7.2 \times 10^{-19}$ m$^2$/W, we can estimate $\chi^{(3)}$ using the relation $\chi^{(3)} = (4/3)n_e^2 \epsilon_0 n_2$. Assuming perfect phase matching, the THG conversion efficiency ($\eta = P_\text{THG}/P_\text{THG}^3$) of the resonator can then be expressed as [41]:

$$\eta = g^2 \frac{64\pi^2 Q_a Q_b}{\hbar \omega_0^6},$$  

(3)

where $Q_a(b)$ are the quality factors for the fundamental pump mode and phase-matched higher-order THG mode. Using the experimentally determined $Q$-factor, $Q_a = 3.6 \times 10^7$, and approximating $Q_b$ to be an order of magnitude smaller than $Q_a$ [24,41], we arrive at an absolute conversion efficiency $\eta' = P_\text{THG}/P_\text{THG}^3$ of 0.0245 for a pump power of 2.5 mW. The uncoated silica sphere shows a conversion efficiency of $\sim 1/3$ of the coated sphere ($\eta' = 0.0097$), which is in strong agreement with experimental results. This value of $\eta'$ is likely larger than what would be measured given the assumptions of $g$ and $\eta$, and is only meant to provide a rough comparison to similar devices. A THG efficiency of 0.0256 is $\sim 3$ orders of magnitude larger than a similar pure silica microsphere with $Q_a = 1.0 \times 10^7$ [19], and compares favorably to other resonator geometries [24,47].

5. Conclusion

We have demonstrated a $\sim 3$-fold enhancement of third-harmonic generation (THG) conversion efficiency using indium tin oxide (ITO) nanoparticles on the surface of an ultra-high-$Q$ silica microsphere. The $\sim 3$-fold increase in nonlinear effects and $\sim 7$-fold decrease in the $Q$-factor of the microsphere was shown to be in excellent agreement with previous results for ITO-coated silica microspheres [37]. The cubic relation between THG and pump power was verified, and the effects of Raman-induced TSFG were explored. A numerical analysis of phase-matching and mode overlap was performed to identify the sphere radius (29 µm) that maximizes THG for a pump wavelength of 1550 nm. To the best of the authors’ knowledge, this is the first demonstration of THG enhancement using ITO nanoparticles, as well as one of the largest reported enhancements of THG in a silica microsphere [24–26,48–50]. We have also shown the benefits of ITO by
achieving uniform surface-coating through the drop-casting fabrication method. This work clearly demonstrates the nonlinear enhancement capabilities and fabrication advantages of ITO nanoparticles in microresonator-based applications. Although this research was limited to silica microspheres, ITO nanoparticles can be used for enhancement of any third-order nonlinear effects and applied to various resonator geometries.

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Disclosures

The authors declare no conflicts of interest.

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