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and the HOV Model of Trade

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# Development-Related Biases in Factor Productivities and the HOV Model of Trade

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## Abstract

Past empirical failures of the basic Heckscher-Ohlin-Vanek (HOV) model related to its restrictive assumptions, particularly identical international technologies and factor price equalization. Trefler (1993) resuscitated HOV by introducing a simple Hicks-neutral (HN) factor-productivity adjustment, an approach that was heavily criticized. In this paper, we reexamine the productivity question by estimating factor productivities from the individual technology data of multiple countries. Using a dataset of 15 OECD countries, we find positive evidence for Trefler's idea, but with factor augmentation. Further, we find that the ratios of factor productivities are strongly correlated with corresponding factor endowments. This systematic bias implies that the ability of HOV to explain North-South factor trade depends both on relative factor abundance and productivity gaps. We thus extend Debaere's (2003) conclusion that North-South trade is determined by HN-adjusted endowment differences.

Keywords: Heckscher-Ohlin-Vanek; Factor Trade, Productivity

JEL classifications: F11 (Neoclassical Model of Trade)

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## 1. Introduction

Early tests of the Heckscher-Ohlin-Vanek (HOV) model of international factor trade demonstrated that it failed to predict trade better than a coin toss (Maskus, 1985; Bowen, Leamer and Sveikauskas, 1987). As noted by Maskus (1985), the assumptions of the strict HOV model are too unrealistic to expect them to generate actual data.<sup>1</sup> Later tests relaxed many of these assumptions to generate augmented HOV models that were more consistent with data (e.g., Trefler, 1995; Davis and Weinstein, 2001; Davis, et al, 1997; Hakura, 2001). Much of this analysis has focused on the unrealistic assumptions of internationally identical technologies and factor price equalization (FPE).

Trefler (1993) made a first important step to integrate international differences in factor-prices into the HOV model. He introduced a simple Hicks-neutral productivity modification to measure factor endowments in productivity-equivalent units. For example, if the labor supplies of the United States and Brazil were the same, but U.S. workers were twice as productive, the former nation would have twice as much labor at the productivity-equivalent level.<sup>2</sup> At the same time, the wage of U.S. workers would be twice that of Brazilian workers and ratios of factor prices could be used to infer relative productivities. This modification is consistent with the HOV model after adjusting for international differences in factor productivity.

Davis and Weinstein (2001) argued that Trefler's productivity modification is incomplete because it fails to introduce general differences in technology. With step-by-step relaxations of the standard HOV assumptions, they found substantial improvements in prediction power when national technologies are modified according to factor abundance measures.

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<sup>1</sup> The Strict version assumes: (1) identical constant returns to scale (CRS) technology and factor price equalization (FPE), (2) perfectly competitive markets in goods and factors, (3) identical and homothetic preferences, (4) factor endowment differences and (5) free trade in goods and services (product prices are identical across the countries) but not factors.

<sup>2</sup> This was Leontief's (1953) conjecture to explain his celebrated paradox.

Though both studies focused on modifying FPE, the conceptual distinction between their empirical approaches is important. Is it differences in productivity of factors or underlying technology that is responsible for factor price disparity? If it is because of factor-productivity differences, the HOV model is fundamentally acceptable, for its failures would come from the inability to measure factors in productivity-equivalent units. However, if the failures occur because of general technology differences, both the standard HOV model and FPE break down.

Because of the empirical success of Trefler's basic approach, several recent papers analyzing factor abundance have relied on it to justify the introduction of productivity adjustments (Trefler, 1995; Antweiler and Trefler, 2002; Debaere, 2003; Fitzgerald and Hallak, 2004). However, the validity of his results has been questioned. Gabaix (1997), for example, showed that Trefler's adjustment to labor productivity (capital productivity) merely reflects differences in GDP/labor (or GDP/capital) due to his method of deriving productivities. There is surely a strong correlation between GDP per unit of factor and factor prices that may not be solely the result of differences in productivity. Thus, Trefler's claim of strong support for the standard HOV model is questionable unless factor productivities are estimated appropriately.

In this paper we introduce a different approach to estimate productivities based solely on a constant returns to scale (CRS) production function.<sup>3</sup> This methodology permits discussion of Trefler's model without facing the argument made by Gabaix. In addition, we can examine the standard HOV testing procedures that Trefler (1993) could not apply. Using a newly constructed dataset covering 15 OECD countries, we find positive evidence for Trefler's model. In particular, incorporating estimated factor productivities raises the fit of the standard signs test from 56.7 percent to 76.7 percent and increases the variance ratio from 0.002 to 0.233.

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<sup>3</sup> Our approach builds on that of Maskus and Webster (1999). Those authors were concerned with ranking endowments across the United States and the United Kingdom, assuming the HOV model to be valid, rather than testing the trade model itself.

More fundamentally, we also find that the estimated productivities are strongly correlated with aggregate factor abundance in a relative sense. For example, capital-abundant Japanese workers are productive (relative to Japanese capital) because they have good access to machines and computers that makes Japanese workers efficient. This systematic correlation between labor-productivity and capital-abundance, which is consistent with general principles of the factor-proportions model of trade without FPE, was previously discussed by Dollar, Wolff, and Baumol (1988). Its importance here is that the empirical success of Trefler's basic model can be attributable to systematic productivity differences across factors that cannot be obtained from the Hicks-neutral form. Thus, similar to Davis and Weinstein (2001) who adjusted national technologies according to factor-abundance,<sup>4</sup> our results also indicate the important link between technology, productivity, and factor abundance.

Our finding points out a potential danger in applying HOV-type models in a relative (i.e., bilateral) sense because factor productivity interacts systematically with factor abundance. For example, Debaere (2003) demonstrated that the HOV equation holds better for South-North country pairs than for North-North country pairs. But it raises the question of whether South-North factor-productivity gaps or South-North factor-abundance differences drive support for the factor contents of trade. In fact, we show that the reason Debaere found strong evidence only for South-North country pairs of particular factor combinations is the systematic South-North differences in factor productivity. Because the abundant factor (unskilled labor) has limited access to capital and skilled labor in the South, its productivities are systematically lower than those of capital and skilled labor. However, Northern data do not entail this feature. This productivity gap contributes to the support found for Debaere's theoretical prediction involving

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<sup>4</sup> Those authors relied on the Dornbush, Fischer, and Samuelson (1980) model and Helpman's (1999) multiple-cone model of specialization to motivate this correlation.

only relative factor abundance for South-North country pairs. Therefore, it is hard to conclude that the success of the relative factor-abundance model is purely derived from South-North differences in factor endowments. Rather, both differences in factor productivities and factor endowments are responsible, with the balance of each element being unclear.

We organize the paper as follows. In Section 2 we revisit Treﬂer’s (1993) model and the criticism in Gabaix (1997). In Section 3 we set out our empirical results from the estimation of factor productivities and relates them to Treﬂer’s model. In addition, we study the characteristics of estimated productivities, particularly the correlation between productivity and factor abundance. In section 4 we examine the potential biases occurred from factor productivities in the context of Debaere’s (2003) relative factor-abundance model. Finally, we conclude the paper with a discussion of the link between factor productivity and technology.

## **2. The HOV Model and Factor-Augmenting Productivity**

We begin by deriving the basic HOV prediction in a world with  $F$  factors,  $C$  countries, and  $N$  products (sectors). Assume that all countries have identical constant returns to scale production technology; markets for goods and factors are perfectly competitive; there are no barriers to trade and zero transportation cost; factors move freely within a country but do not move across countries; and the distribution of factors is consistent with integrated equilibrium so that factor prices are equalized across countries.

For each country  $c$  the net-export vector can be obtained as the difference between net production and the final consumption:

$$T_c = (I - B_c)Q_c - C_c \tag{1}$$

where  $T_c$  is an  $N \times 1$  vector of net exports,  $Q_c$  is an  $N \times 1$  vector of gross output, and  $C_c$  is an  $N \times 1$  vector of final consumption.  $B_c$  is an  $N \times N$  input-output (indirect) matrix for the unit intermediate requirements so that  $(I-B_c)Q_c$  equals the net output vector  $Y_c$ .

Let  $A_c$  be the  $F \times N$  direct technology matrix and its elements  $(a_{cif})$  represent the amount of a factor needed to produce one unit of gross output in sector  $i$ . Pre-multiplying equation (1) by direct and indirect technology matrix  $A_c(I-B_c)^{-1}$  and applying the factor-exhaustion assumption  $A_c Q_c = V_c$  where  $V_c$  is an  $F \times 1$  vector of factor endowments, we have that a country's factor contents of trade is the difference between factors absorbed in production ( $A_c Q_c = V_c$ ) and factors absorbed in final consumption ( $A_c(I-B_c)^{-1}C_c$ ):

$$A_c(I-B_c)^{-1}T_c = V_c - A_c(I-B_c)^{-1}C_c \quad (2)$$

Assuming identical and homothetic preferences, along with identical prices of goods and services, the final consumption vector is proportional to the world net output vector ( $Y_w$ ):

$$C_c = s_c Y_w \quad (3)$$

where  $s_c$  is a scalar representing the share of country  $c$  in world expenditure. Because the production technology is identical worldwide and there is FPE, the technologies of the United States may be used to derive the following standard HOV equation:

$$F_c = V_c - s_c V_w \quad (4)$$

where  $F_c = A_{US}(I-B_{US})^{-1}T_c$  is measured factor contents of trade with U.S. technologies and  $V_c - s_c V_w$  is predicted factor contents of trade. Thus, the HOV model tells us that measured factor contents of trade for any country can be predicted by that country's factor endowments, the world factor endowments, and final consumption shares.

To integrate factor productivity into the HOV model, Trefler (1993) introduced coefficients  $(\pi_{cf})$  with the interpretation that if  $V_{cf}$  is the factor endowment of country  $c$  then

$V_{cf}^* = \pi_{cf} V_{cf}$  is the corresponding factor endowment measured in productivity-equivalent units.

Let  $w_{cf}$  be the price per unit of  $V_{cf}$  and let  $w_{cf}^*$  be the price per unit of  $V_{cf}^*$ . Since one unit of  $V_{cf}$  provides  $\pi_{cf}$  productivity-equivalent units of service,  $1/\pi_{cf}$  units of  $V_{cf}$  provide one productivity-equivalent unit service priced at  $w_{cf}^* = w_{cf}/\pi_{cf}$ . Assuming identical technologies at the productivity-equivalent level and normalizing factor productivities of the United States to unity, the system of equations (5) and (6) follows:

$$F_{cf} = \pi_{cf} V_{cf} - s_c \sum_{g=1}^G \pi_{gf} V_{gf} \quad (5)$$

$$w_{cf} / \pi_{cf} = w_{USf} / \pi_{USf} \Leftrightarrow w_{cf} / w_{USf} = \pi_{cf} / \pi_{USf} \quad (6)$$

where equations (5) capture the elements of  $F_c = A_{US}(I - B_{US})^{-1} T_c$ ,  $\pi_{USf} = 1$ , and  $g$  is the index of countries in the dataset. This framework is the efficiency-unit HOV model in Trefler (1993) in which the standard HOV model is adjusted by factor productivities.

### 2.A. Trefler's Derivation of Factor-Productivity

Trefler built the extended HOV model with the system of equations (5) and (6), using a dataset for 33 countries. Equation (5) is the HOV model with productivity-equivalent factors and equation (6) indicates that FPE holds when international factor productivities are adjusted.

To estimate factor productivities ( $\pi_{cf}$ ), Trefler derived equation (7) from equation (5):

$$F_f = X_f \Pi_f \quad \text{where} \quad F_f = \begin{bmatrix} F_{1f} \\ F_{2f} \\ \vdots \\ F_{cf} \end{bmatrix}, X_f = \begin{bmatrix} (1-s_1)V_{1f} & -s_1V_{2f} & \cdots & -s_1V_{cf} \\ -s_2V_{1f} & (1-s_2)V_{2f} & \cdots & -s_2V_{cf} \\ \vdots & \vdots & \ddots & \vdots \\ -s_cV_{1f} & -s_cV_{2f} & \cdots & (1-s_c)V_{cf} \end{bmatrix}, \Pi_f = \begin{bmatrix} \pi_{1f} \\ \pi_{2f} \\ \vdots \\ \pi_{cf} \end{bmatrix} \quad (7)$$

Normalizing the productivities in terms of the United States, the  $\pi_{cf}$  parameters may be estimated by ordinary least squares (OLS). However, once these estimated factor productivities are introduced into equation (5) it is inappropriate to apply standard testing procedures of the HOV



model because fitted values for predicted factor contents of trade are identical to measured factor contents of trade. That is, all the HOV test statistics automatically would indicate a perfect fit.<sup>5</sup>

To deal with this issue Trefler set out two alternative methods to demonstrate the validity of his estimated factor productivities. One was to check the signs of the productivity parameters, with all expected to be positive. The other was to study the correlation between relative price ( $w_{cf}/w_{USf}$ ) and relative productivity ( $\pi_{cf}/\pi_{USf}$ ) in equation (6) for each factor, with the correlation expected to be unity. Trefler noted that the productivities estimated from equation (7) were positive and that equation (6) performed well, with the correlation for labor being 0.90 and that for physical capital being 0.68.

While the approach generated a number of comments, Gabaix (1997) in particular criticized this methodology for deriving the estimation method (equation (7)) testing factor productivities. His reasoning came from the “missing trade” phenomenon analyzed in Trefler (1995). Missing trade is the finding that measured factor contents of trade are generally very small relative to predicted factor contents of trade. Thus, if the vector of measured factor contents of trade were virtually zero in equation (5), we would have:

$$0 = \pi_{cf}V_{cf} - s_c V_{wf}^* \Leftrightarrow \pi_{cf} = s_c \frac{V_{wf}^*}{V_{cf}} = \frac{Y_c}{Y_w} \frac{V_{wf}^*}{V_{cf}} = \frac{Y_c}{V_{cf}} R \quad (8)$$

where world aggregates ( $V_{wf}^* = \sum_g \pi_{gf} V_{gf}$  and  $R = V_{wf}^*/Y_w$ ) are essentially independent of the data from country  $c$ . In the case of labor, for example, the estimated productivity of labor would equal GDP per worker. Therefore, it is not surprising that Trefler’s estimated productivities were

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<sup>5</sup> Because OLS forces the productivity parameters to equalize measured factor contents of trade (FCT) and fitted (predicted) factor contents of trade (FCT):  $F_f \equiv \hat{F}_f = X_f \hat{\Pi}_f$ , the measured FCT ( $F_f$ ) and the predicted FCT ( $X_f \hat{\Pi}_f$ ) are nearly identical.

positive and correlated strongly with factor prices. In this context, Trefler’s approach offered no independent validation for the empirical success of his productivity modification of HOV.

Although Gabaix’s criticism does invalidate Trefler’s methodology and statistical evidence, it does not necessarily mean the rejection of Trefler’s model *per se*. Rather, if it were possible to estimate factor-productivity parameters independently of the equation system, incorporating them would not make HOV a truism and standard testing procedures would be valid. To this end, we develop unit total factor requirements (technologies  $A_c$  and  $B_c$ ) for each country and estimate factor productivities for each country across sectors. These estimated parameters are then incorporated to test equations (5) and (6). This procedure escapes the problems Gabaix (1997) pointed out.

## 2.B. The Modified Trefler Approach

Within Trefler’s framework, countries share identical production technologies at the productivity-equivalent level, making adjusted unit factor requirements identical across countries for each factor:  $a'_{USif} = a'^*_{cif}$  for country  $c$  and factor  $f$  where  $a'^*_{cif}$  is  $\pi_{cf} a'_{cif}$ . If firms minimize unit cost functions with CRS technology, the quantity of factor  $f$  required in sector  $i$  divided by corresponding output is the unit factor requirement:  $a'_{USif} = V_{USif}/Q_{USif}$  for the United States and  $V^*_{cif}/Q_{cif} = \pi_{cf} V_{cif}/Q_{cif} = \pi_{cf} a'_{cif} = a'^*_{cif}$  for country  $c$ .

We estimate the productivity parameters ( $\pi_{cf}$ ) by regressing the unit factor requirements of the United States against those of individual countries. This approach was proposed by Maskus and Webster (1999) in developing their “factor-augmenting, industry-neutral (FAIN)” specifications. Thus, consider the simple regressions:

$$a'_{USif} = \pi_{cf} a'_{cif} + \varepsilon_{cif} \quad (9)$$

where  $a'_{cif}$  embraces direct and indirect technologies.<sup>6</sup> These equations are estimated using data that vary across 22 sectors for each country. The estimation approach is seemingly unrelated regressions (SUR). We assume that these factor requirements are generated by a process obeying the FAIN assumption, with measurement errors randomly distributed around zero and embodied in the residual terms.<sup>7</sup>

Using the estimated factor-productivities from equation (9), we test both equations (5) and (6). This implicitly assumes that no other sources of international differences in unit factor requirements (technologies) exist after international factor productivities are adjusted. Because the factor-productivities are estimated solely from unit factor requirements, it is possible to examine equations (5) and (6) separately and apply standard testing procedures of the HOV model to equation (5). In addition, we can separately assess equation (6) in terms of the correlations between price and productivity for each factor.

In testing HOV we consider both the aggregate specification in (5) and the pair-wise HOV model (e.g., Staiger, Deardorff, and Stern, 1987; Hakura, 2001). The primary advantage of the pair-wise HOV model is that the testing equation does not include world aggregates. Because our dataset consists of 15 OECD countries, there is some question about data sums representing world aggregates. To derive the pair-wise model, apply equation (4) to two arbitrarily chosen countries. For example, take the ratio of the United States ( $c=1$ ) and Japan ( $c=2$ ) and cancel the net world output ( $Y_w$ ) in equation (3) ( $C_1 = s_1/s_2 C_2 = \alpha C_2$ ). Then, with appropriate subtraction, the pair-wise HOV model follows:

$$F_1 - \alpha F_2 = V_1 - \alpha V_2 \quad (10)$$

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<sup>6</sup> Total technology (direct and indirect):  $A'_c = A_c(I - B_c)^{-1}$ .

<sup>7</sup> Maskus and Webster (1999) discuss potential types of measurement error.

where  $F_1 - \alpha F_2$  is the measured relative factor contents of trade with country 2's technology ( $F_1 = A_2(I - B_2)^{-1}T_1$  and  $F_2 = A_2(I - B_2)^{-1}T_2$ ) and  $V_1 - \alpha V_2$  is the predicted relative factor content of trade.<sup>8</sup>

We next apply estimated factor productivities to the pair-wise HOV model. In this model, technology differs more generally than in equation (9):<sup>9</sup>

$$a'_{1f} = \pi_f^{12} a'_{2f} + \varepsilon_{if}^{12} \quad (11)$$

where  $\pi_f^{12}$  is the factor-productivity of country 2 for factor  $f$  in terms of country 1. These factor productivities are also estimated using SUR for each country pair. Using equations (10) and (11), the pair-wise HOV model with factor-productivity adjustment follows:<sup>10</sup>

$$F_1 - \alpha F_2 = \Pi_{12} V_1 - \alpha V_2 \quad (12)$$

Here  $\Pi_{12}$  is a diagonal  $F \times F$  matrix with elements that are the corresponding productivity coefficients ( $\pi_f^{12}$ ) estimated from equation (11). The difference  $F_1 - \alpha F_2$  is the measured relative factor contents of trade with country 2's technology ( $F_1 = A_2(I - B_2)^{-1}T_1$  and  $F_2 = A_2(I - B_2)^{-1}T_2$ ).

Testing procedures are the same as for the basic HOV model.

### 3. Empirical Results

Estimating factor-productivity parameters from equations (9) and (11) requires data on actual technologies for multiple countries. Thus, we assembled a comprehensive data set for a group of 15 OECD countries, as described in Appendix A. There are two factors (physical capital and aggregate labor) and 23 industrial sectors. The dataset is similar to that in Hakura

<sup>8</sup> This specification is different from that in Hakura (2001) because she used each country's actual technology to measure factor contents of trade ( $F_1 = A_1(I - B_1)^{-1}T_1$  and  $F_2 = A_2(I - B_2)^{-1}T_2$ ).

<sup>9</sup> In the modified Treffer framework, we obtain international productivity differences with respect to the United States as in equation (9). Here, we obtain these parameters for all binary combinations of countries.

<sup>10</sup> Derivation of the relative HOV model with factor-productivity adjustments is as follows. We have the productivity equation:  $A_1(I - B_1)^{-1} = \Pi_{12} A_2(I - B_2)^{-1}$ . Using the relationship for country 1, we have two equations: (1)  $\Pi_{12} A_2(I - B_2)^{-1} T_1 = V_1 - \Pi_{12} A_2(I - B_2)^{-1} s_1 C_1$  and (2)  $A_2(I - B_2)^{-1} T_2 = V_2 - A_2(I - B_2)^{-1} s_2 C_2$ . Pre-multiplying (1) with  $\Pi_{12}^{-1}$  and (2) with  $\alpha$ , and taking the difference between the two gives equation (12).

(2001) who developed a 23-sector dataset of four European countries with seven factors.

Because we combine input-output tables from different sources (OECD and Eurostat) in order to increase the number of countries, we were forced to aggregate to 23 sectors to maintain consistency in classification.<sup>11</sup> Aggregation is inevitable but, as has been noted by Feenstra and Hanson (2000) it raises the risk of systematic bias in the HOV predictions, a problem in all such studies.

### *3.A. Factor-Augmenting Productivity Estimates*

Table 1 reports the estimated factor-productivity parameters and associated statistics for equation (9). All factor-productivities are positive and statistically significant.<sup>12</sup> The coefficients on physical capital for all 14 OECD countries are lower than unity, suggesting that the United States has the highest levels of capital productivity. Regarding labor, workers in Belgium, France, and Italy are more productive than those in the United States. For each country the R-squared coefficients measure the strength of the correlation between countries. In most cases the factor productivities fit well. For example, the R-squares for Canadian capital and labor are 0.847 and 0.590, indicating a strong concordance between Canadian and U.S. technologies. However, if the technology differed in a more complex way, as Davis and Weinstein (2001) suggested, there are additional determinants that the basic approach taken here does not account for. This might be the case for capital productivities in Belgium, France and Japan, which do not perfectly correlate with the U.S. technology,

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<sup>11</sup> Overall there are 23 industries in the OECD STAN database. However, because the figures on gross fixed capital formations (GFCF) contain residential (housing) investments for some countries, the GFCF values for agriculture (sector 1) and finance, insurance, and real estate (sector 22) are contaminated by residential investments. As noted in Appendix A, we were able to adjust the GFCF values for sector 22 but not for agriculture, which we exclude for factor-productivity estimations.

<sup>12</sup> In fact, all are significantly different from both zero and unity at the five percent level.

It is of interest to compare the national factor-productivity parameters developed using Trefler's (1993) method (equation (7)) and those using the method in equation (9) due to Maskus and Webster (1999). In Table 2 we list the parameters computed from Table 1 (the first two columns) and those in Trefler's paper (the next pair of columns). The correlations between the corresponding factors are very high, at 0.81 for physical capital and 0.96 for aggregate labor. Thus, Trefler's estimated factor-productivities are similar to those obtained from estimation based only on unit factor requirements.

In addition, we compare these factor productivities with total factor productivities (TFP), which are estimated from a Cobb-Douglas production function applied to 13 manufacturing sectors in these OECD countries.<sup>13</sup> The correlations between TFP and individual factor productivities are not perfect (around 0.6) and the values of TFP generally lie between those for capital and labor. This would suggest that the empirical success of the factor-productivity adjustments in Trefler (1993) are attributable to systematic productivity differences across factors that the Hicks-neutral form (e.g., TFP) cannot account for. This confirms previous findings in the literature that Hicks-neutral productivity adjustments usually do not overturn the failures of the HOV equation.

### *3.B. Performance of the HOV Models*

Table 3 shows the results of testing the HOV model with and without factor-productivity adjustments. The standard HOV model performs poorly as expected. The sign fit is 56.7 percent for our two factors, the slope is 0.021, and the variance ratio is 0.002. Though the sign fit is marginally better than a coin-flip, the slope and variance ratio tests indicate significant missing trade. Therefore, the results strongly reject the standard HOV model.

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<sup>13</sup> These functions are estimated in Nishioka (2006)

However, once the estimated factor productivities are introduced, these numbers improve considerably. For the HOV specification, as shown in the bottom panel, the sign fit improves to 76.7 percent, the slope coefficient rises to 0.231, and the variance ratio increases to 0.233. Furthermore, Figures 1-1 and 1-2 depict the correlation between factor productivities and factor prices as in equation (6). Both labor and capital fit well, with the correlation for aggregate labor being 0.78 and that for physical capital being 0.79.<sup>14</sup>

Regarding the pair-wise HOV model, Table 3 also shows a considerable improvement when factor-productivity adjustments are incorporated. The sign test improves from 54.8 percent to 71.9 percent and the variance ratio improves from 0.131 to 0.594. These positive improvements from the pair-wise models suggest that the acceptable performance of Trefler's factor-productivity adjustments was not spurious.

### *3.C. Characteristics of Factor-Productivity*

While introducing factor-productivity parameters ( $\pi_{cf}$ ) is a convenient method to modify the HOV model, the interpretation of  $\pi_{cf}$  is not entirely clear. Trefler (1993) explained the source of international difference in factor productivity as based on two possibilities. Suppose that workers in Belgium have the highest labor productivity. Then it could be that: (1) workers in Belgium simply work harder than workers in other countries, or (2) workers in Belgium are no more industrious as workers elsewhere but they have access to technologies that make them more efficient.

We are particularly interested in the second possibility because our aggregate labor flows have been adjusted by working hours. Under the second notion we expect that labor productivity

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<sup>14</sup> We obtain the factor prices from total compensation for each factor divided by total amount of the corresponding factors. Compensation for physical capital is derived as value added minus labor compensation.

correlates positively with capital abundance.<sup>15</sup> As shown in Figures 2-1 and 2-2, this feature characterizes the data, but weakly. Using unadjusted input requirements, capital-productivities decline with capital abundance (correlation equals -0.25) and labor productivities rise with capital abundance (correlation equals 0.24). One reason for these correlations to be weak might be the limitation of our data to just two factors, with other elements such as knowledge capital and human capital being partially responsible for varying productivities.

However, when we incorporate the adjusted productivity ratios ( $\pi_{cL}/\pi_{cK}$ ), they correlate strongly with corresponding factor endowments as shown in Figure 3. For example, capital-abundant Japanese workers are productive relative to Japanese capital because they have good access to abundant capital (machines and computers). It seems that Treﬂer’s original explanation holds well in this “relative” sense. This observation suggests that, similar to the approach of Davis and Weinstein (2001), who adjusted technologies according to factor abundance, our adjusted factor productivities also capture the link between technology, productivity, and factor-abundance that the Hicks-neutral form cannot accommodate.

#### **4. The Relative Factor Abundance Model and Factor-Productivities**

The strong correlation between factor abundance and factor productivity is particularly relevant to the relative factor-abundance model of Debaere (2003). Debaere developed a factor content of trade prediction for the HOV model that relates bilateral differences in endowments to bilateral differences in factor trade. Our objective here is to reexamine his conclusion that the trade of South-North country pairs is consistent with HOV but that of North-North country pairs is not. We show that Debaere’s result is caused not only by South-North differences in factor

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<sup>15</sup> This link was previously discussed by Dollar, Wolff, and Baumol (1988) who find the systematic correlation between labor-productivity and capital-abundance with their factor-price equalization model.



endowments, which is the issue he emphasized, but also by South-North differences in factor productivity. Specifically, because unskilled labor, the abundant factor in the South, has limited access to skilled labor and capital, the productivity of unskilled workers there is systematically lower than that in the North. This difference is an additional important reason that only South-North country-pairs perform well in his examination of HOV.

To develop Debaere's relative factor abundance model, take equation (4) with U.S. technologies and impose identical and homothetic preferences:

$$F_c = V_c - A_{US}(I - B_{US})^{-1} s_c Y_W \quad (13)$$

Divide both sides of equation (13) by the scalar expenditure share  $s_c$  to obtain:

$$F^*_c = V^*_c - A_{US}(I - B_{US})^{-1} Y_W \quad (14)$$

where  $F^*_c = A_{US}(I - B_{US})^{-1} T_c = F_c / s_c$  and  $V^*_c = V_c / s_c$ . Now consider equation (14) for two countries,  $c$  and  $c'$ , and take the difference between their expressions:

$$F^*_c - F^*_{c'} = V^*_c - V^*_{c'} \quad (15)$$

Equation (15) may be expressed for a particular factor ( $f$ ) and divided by the sum of factor endowments,  $V^*_{cf} + V^*_{c'f}$ :

$$\frac{F^*_{cf} - F^*_{c'f}}{V^*_{cf} + V^*_{c'f}} = \frac{V^*_{cf} - V^*_{c'f}}{V^*_{cf} + V^*_{c'f}} \quad (16)$$

Then, express equation (16) for another factor ( $f'$ ) and again take differences:

$$\begin{aligned} \frac{F^*_{cf} - F^*_{c'f}}{V^*_{cf} + V^*_{c'f}} - \frac{F^*_{cf'} - F^*_{c'f'}}{V^*_{cf'} + V^*_{c'f'}} &= \frac{V^*_{cf} - V^*_{c'f}}{V^*_{cf} + V^*_{c'f}} - \frac{V^*_{cf'} - V^*_{c'f'}}{V^*_{cf'} + V^*_{c'f'}} \\ \Leftrightarrow \frac{F^*_{cf} - F^*_{c'f}}{V^*_{cf} + V^*_{c'f}} - \frac{F^*_{cf'} - F^*_{c'f'}}{V^*_{cf'} + V^*_{c'f'}} &= \frac{2V^*_{cf}}{V^*_{cf'} + V^*_{c'f'}} \left( \frac{V^*_{cf'}}{V^*_{cf}} - \frac{V^*_{cf'} + V^*_{c'f'}}{V^*_{cf} + V^*_{c'f'}} \right) \end{aligned} \quad (17)$$

Here, the relative difference in measured factor content of trade is on the left-hand side and the relative difference in predicted factor content of trade is on the right-hand side.

For any two factors  $f$  and  $f'$ , a country  $c$  is said to be relatively abundant in factor  $f$  compared to country  $c'$  when  $V_{cf}^*/V_{c'f}^*$  is larger than  $V_{c'f'}/V_{cf'}^*$ . This statement is easily shown because the relative factor abundance relationship  $V_{cf}^*/V_{c'f}^* > V_{c'f'}/V_{cf'}^*$  holds if and only if  $V_{c'f'}/V_{cf'}^* > (V_{c'f'}^* + V_{cf'}^*) / (V_{cf}^* + V_{c'f}^*)$ , which is the right-hand side of the second equation in (17). Therefore, the testing strategy is to check the sign concordance of measured and predicted relative differences in factor trade.<sup>16</sup> Debaere showed that equation (17) holds even for the case of Hicks-neutral productivity. We show in Appendix B that it holds also for the case of adjusted factor productivities.

Our tests are reported in Table 3, Panels 5 and 6. It is clear that adjusting endowments by factor productivities makes a critical difference in the performance of the relative HOV model. When factors are not adjusted, the sign match is less than 50 percent and the variance ratio is 0.056. However, once factors are adjusted by our estimated productivities, these statistics improve to 60 percent for the sign test and 0.943 for variance ratio.

To be complete, it is important to investigate this issue using the same data as Debaere. Because his dataset is that in Trefler (1993), it is impossible to estimate appropriate factor productivities by using equation (9). Our compromise to use the Trefler's method in equation (7) to obtain factor productivities.

A first step is to show that the relative factor abundance comparison ( $V_{cf}^*/V_{c'f}^* > V_{c'f'}/V_{cf'}^*$ ) can be divided into two parts: (1) relative factor-productivity ratios and (2) productivity-equivalent relative factor abundance. Denote factor endowments at the productivity-equivalent level as  $V'_{cf} = \pi_{cf} V_{cf}^*$  and rewrite relative factor abundance as:

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<sup>16</sup> Though Debaere (2003) reported only sign tests, we report slope tests and variance ratios as well.

$$\frac{V_{cf}^*}{V_{c'f'}^*} > \frac{V_{cf}^*}{V_{c'f'}^*} \Leftrightarrow \frac{V'_{cf}/\pi_{cf}}{V'_{c'f'}/\pi_{c'f'}} > \frac{V'_{cf}/\pi_{cf}}{V'_{c'f'}/\pi_{c'f'}} \Leftrightarrow \frac{V'_{cf}}{V'_{c'f'}} \frac{\pi_{c'f'}}{\pi_{cf}} > \frac{V'_{cf}}{V'_{c'f'}} \frac{\pi_{c'f'}}{\pi_{cf}} \quad (18)$$

Equation (18) explains that relative factor-abundance ratio without productivity adjustments ( $V_{cf}^*/V_{c'f'}^*$  or  $V_{c'f'}^*/V_{cf}^*$ ) is a product of the productivity-equivalent relative factor abundance ratio ( $V'_{cf}/V'_{c'f'}$  or  $V'_{c'f'}/V'_{cf}$ ) and the factor-productivity ratio ( $\pi_{cf}/\pi_{c'f'}$  or  $\pi_{c'f'}/\pi_{cf}$ ). If, as Debaere assumed, the Hicks-neutral form ( $\pi_{cf}/\pi_{c'f'} = \pi_{c'f'}/\pi_{cf}$ ) is realistic, then relative factor abundance and productivity-equivalent factor abundance are identical and his basic conclusion holds. However, if productivity adjustments are more general, then both elements matter. For example, if  $f$  is labor ( $L$ ) and  $f'$  is physical capital ( $K$ ) for the South ( $c=S$ ) and the North ( $c'=N$ ), we expect that labor in the South is less productive than in the North because it operates with a smaller relative capital endowment. As a result, we have an inequality in relative productivity ratios:  $\pi_{SK}/\pi_{SL} > \pi_{NK}/\pi_{NL}$  or  $\pi_{SK}/\pi_{NK} > \pi_{SL}/\pi_{NL}$ .

It is important, therefore, to study South-North differences in factor productivities in addition to relative factor endowments. For this purpose, we use Trefler's dataset, divide countries into the South and the North according to Debaere (2003), and develop the South-North productivity ratios for factors. The parameters ( $\pi_{cf}$ ) are obtained by estimating equation (7) for physical capital, skilled labor, unskilled labor, and aggregate labor. If Hicks-neutral productivity differences were realistic, we would expect these productivity ratios to be identical across any factor pair ( $\pi_{cf}/\pi_{c'f'} = \pi_{c'f'}/\pi_{cf}$ ). However, this is not the case as shown in Figures 4-1 through 4-8. Rather, we find the interesting tendency that the productivity ratio of the South to the North for unskilled labor is always smaller than that for skilled labor and physical capital. There is not a similar tendency for the North-North pairs. Therefore, the systematic tendency in factor productivities supports the inequality in equation (18) only for the South-North country pairs of particular factor combinations: unskilled labor/skilled labor, unskilled labor/capital, and

labor/capital. This evidence implies that Debaere's conclusion could be delivered by interplay between endowment differences and factor-productivity differences.

## **5. Concluding Remarks**

In this paper we reexamine Trefler's (1993) factor-productivity model. Departing from his procedure, which was criticized by Gabaix (1997), we estimate factor-productivity parameters from each country's actual technologies. This approach permits use of the standard evaluations of the HOV model (sign test, slope test, and variance ratio test). Using a dataset of fifteen OECD countries, we show positive evidence for Trefler's basic idea, with both the sign concordance and the variance ratio increasing markedly. However, rather than simple Hicks-neutral adjustments, our results indicate that factor-augmenting productivity differences are an appropriate modification of HOV models.

Prior studies that made technological specifications increasingly more flexible by using country-specific data also supported the extended HOV model (Hakura, 2001; Davis and Weinstein, 2001). Indeed, Davis and Weinstein (2001) established a strong fit of the HOV equations when technologies are modified across both industries and countries according to factor abundance. The contribution here is to show that a simpler modification – factor augmentation that is neutral across industries – can establish considerable gains in the predictive performance of the HOV model.

More fundamentally, the analysis unearthed a particular feature of factor productivities in both the OECD dataset and Trefler's dataset. Specifically, factor productivities are inversely correlated with own-factor endowments and positively correlated with other factor endowments, which is consistent with the neoclassical trade model without FPE due, say, to specialization

within different cones. This is especially the case as regards labor in developing countries. As a result, Debaere's (2003) finding that South-North factor trade may be explained well by the relative HOV model with Hicks-neutral productivity differences needs to be supplemented by the interplay between relative endowments and factor productivities.

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## Appendix A: Construction of Data

### 1) Input-Output Data

Input-output tables (total use) for Australia (1994-1995), Canada (1997), Denmark (1997), Finland (1995), France (1995), Germany (1995), Japan (1997), the Netherlands (1997), Norway (1997), the United Kingdom (1998), and the United States (1997) are from the OECD I-O database (2002). Belgium (1995), Italy (1995), Spain (1995), and Sweden (1995) are from the Statistical Office of the European Communities (Eurostat). The I-O tables from the OECD I-O database employ ISIC Rev.3 classification containing 41 industrial groups and the I-O tables from the Eurostat employ NACE/CLIO classification containing 59 groups. These two classifications are aggregated into 23 industrial groups of ISIC Rev.3. The number of industrial groups is smaller than the 35 sectors used by Davis and Weinstein (2001) but is the same as Hakura (2001). Both the input-output matrices and final consumption, gross output, and net exports are derived from the I-O tables for 1997. Final consumption is the sum of final consumption of households, final consumption and investment of government, gross fixed capital formation, and changes in inventory.<sup>17</sup> Therefore, the total use table of country  $c$  always satisfies the equation:  $T_c = (I - B_c)Q_c - C_c$  where  $B_c$  is a  $23 \times 23$  indirect technology matrix for the unit intermediate requirements and  $(I - B_c)Q_c$  vector equals net output ( $Y_c$ ).  $B_c$  is obtained by taking input-output data from the I-O tables and dividing inputs in each sector by the corresponding sector's gross output.<sup>18</sup> To convert the dataset into U.S. dollars, we use purchasing power parities (1997) from the Penn World Table version 6.2 (Heston, Summers and Aten) and the

<sup>17</sup> Finland's data required adding discrepancies in final consumption in order to maintain consistency of the I-O table.

<sup>18</sup> In the case of two sectors, the input usage matrix can be obtained as following.

$$B_c = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} = \begin{bmatrix} x_{11}/Q_1 & x_{12}/Q_2 \\ x_{21}/Q_1 & x_{22}/Q_2 \end{bmatrix} \quad B_c Q_c = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} \begin{bmatrix} Q_1 \\ Q_2 \end{bmatrix} = \begin{bmatrix} x_{11}/Q_1 & x_{12}/Q_2 \\ x_{21}/Q_1 & x_{22}/Q_2 \end{bmatrix} \begin{bmatrix} Q_1 \\ Q_2 \end{bmatrix} = \begin{bmatrix} x_{11} + x_{12} \\ x_{21} + x_{22} \end{bmatrix}$$



OECD Economic Outlook (2006). Conway (2002) and Trefler (2002) discuss the choice between purchasing power parity (PPP) and nominal exchange rates. For Australia, Belgium, Finland, France, Germany, Italy, Sweden, Spain, and the United Kingdom, nominal values in the I-O tables are uniformly multiplied by the growth rates of total nominal GDP to adjust differences from year 1997.

Table A: Sectors of Industrial Activities

sectors	Branches of Activities	ISIC Rev.3
1	Agriculture	01-05
2	Mining and Quarrying	10-14
3	Food Products	15-16
4	Textiles	17-19
5	Wood Products	20
6	Paper Products	21-22
7	Refined Petroleum Products	23
8	Chemicals	24
9	Rubber and Plastics	25
10	Non-Metallic Products	26
11	Basic Metals	27
12	Fabricated Metals	28
13	Machinery	29
14	Electrical Equipment	30-33
15	Motor Vehicles	34
16	Other Transportation	35
17	Other Manufacturing	36-37
18	Electricity	40-41
19	Construction	45
20	Wholesale and Retail Trade	50-55
21	Transport, Storage and Communication	60-64
22	Finance, Insurance and Real Estate	65-74
23	Community Social and Personal Services	75-99

## 2) Factor Endowment Data

### (A) Physical Capital Stock

Capital stock is developed by the perpetual inventory method (e.g., Keller, 2000). Values for gross fixed capital formation (GFCF) are derived from the OECD structural analysis (STAN) database (2004) and unreported data are estimated from the ISIC Rev.2 version of the OECD STAN database (1995, 1997, and 1998) and the Eurostat. As many GFCF data as possible are derived from these databases but there are still some unavailable data. The following procedure

is taken to interpolate these data. First, some detailed sectors (e.g., 15 and 16) are unavailable but data for their aggregated (15+16) industry exist for certain years. We use the share of the nearest year to allocate those totals to each detailed sector. Second, for Denmark some of the aggregate industry totals were also unavailable, and we use the average growth rates of the nearest four years to interpolate the unreported data.

One major problem with using GFCF data from the OECD STAN database (2004) is that some countries include residential investments but other countries do not. In particular, agriculture (sector 1) and finance, insurance, and real estate (sector 22) are the main sources of errors from residential investments. To avoid serious errors, we first deflate nominal values of the real estate sector's GFCF by 65 percent<sup>19</sup> for countries in the dataset except Canada, Japan, the United Kingdom, and the United States. Figures for total nonresidential GFCF are separately obtained from the OECD National Account Statistics (2006) and allocated to each sector according to the shares developed from the OECD STAN database.<sup>20</sup> Unfortunately, it is impossible to adjust agriculture for residential investment and caution must be exercised when data from that sector are used in to the analysis.

To convert GFCF figures into real series, deflators for nonresidential business investment from the OECD Economic Outlook (2006) are used. After converting into a real local currency series, we compute real capital stock data with the perpetual-inventory method, using a depreciation rate of 0.1333 (e.g., Leamer, 1984; Bowen, Leamer, and Sveilauskas, 1987; and Davis and Weinstein, 2001). Then, the real capital stock is converted into 1997 U.S. dollars by purchasing power parities. For Japan, sectoral GFCF data are unavailable from the OECD

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<sup>19</sup> Based on Japanese value.

<sup>20</sup> We use the dataset developed from the OECD STAN database directly for Belgium. In the case of Norway, to separate "housing investment" from "other construction," we use the corresponding shares from Finland and Sweden.

STAN database (2004). Therefore, we take the total GFCF series from the OECD National Accounts Statistics (2006) and Japan's sectoral shares are obtained from the nominal investment matrix tables of the ESRI-Histat database.

## (B) Labor

Sectoral labor inputs (total employments are derived from the OECD STAN databases (1998 and 2004), the Eurostat, and the OECD Employment by Activities and Status (2006). To interpolate unreported data, we use the available share of the nearest year to allocate aggregated sector totals to each detailed sector. Country-level average working hours from the OECD Employment and Labor Market Statistics (2006) are used to adjust international differences in average working hours, normalized by U.S. working hours.

## Appendix B: Relative Abundance and Factor-Productivity Adjustment

Here we introduce factor-augmenting productivity to the right hand side of equation (17). First, we show that the inequality in relative factor abundance for the factor-productivity model does not coincide with that for the strict (or Hicks-neutral) model, as shown in the following equation. Thus, the empirical prediction of Debaere's model with factor-productivity parameters differs from Debaere's original specification.

$$\frac{V^*_{c'f'}}{V^*_{c'f}} > \frac{V^*_{cf'}}{V^*_{cf}} \Leftrightarrow \frac{\pi_c V^*_{c'f'}}{\pi_c V^*_{c'f}} > \frac{\pi_c V^*_{cf'}}{\pi_c V^*_{cf}} \neq \frac{\pi_{c'f'} V^*_{c'f'}}{\pi_{c'f'} V^*_{c'f}} > \frac{\pi_{cf'} V^*_{c'f'}}{\pi_{cf'} V^*_{c'f}}$$

Proof of the relative factor-abundance model with factor-augmenting productivities is following:

$$\begin{aligned} \frac{\pi_{c'f'} V^*_{c'f'}}{\pi_{c'f} V^*_{c'f}} > \frac{\pi_{cf'} V^*_{c'f'}}{\pi_{cf} V^*_{c'f}} &\Leftrightarrow \pi_{c'f'} V^*_{c'f'} \pi_{cf} V^*_{cf} > \pi_{cf'} V^*_{cf'} \pi_{c'f} V^*_{c'f} \\ &\Leftrightarrow \pi_{c'f'} V^*_{c'f'} \pi_{cf} V^*_{cf} + \pi_{c'f'} V^*_{c'f'} \pi_{c'f} V^*_{c'f} > \pi_{cf'} V^*_{cf'} \pi_{c'f} V^*_{c'f} + \pi_{c'f'} V^*_{c'f'} \pi_{cf} V^*_{cf} \\ &\Leftrightarrow \frac{\pi_{c'f'} V^*_{c'f'} (\pi_{cf} V^*_{cf} + \pi_{c'f} V^*_{c'f})}{\pi_{c'f} V^*_{c'f} (\pi_{cf'} V^*_{cf'} + \pi_{c'f} V^*_{c'f})} > 1 \\ &\Leftrightarrow \frac{\pi_{c'f'} V^*_{c'f'}}{\pi_{c'f} V^*_{c'f}} > \frac{\pi_{cf'} V^*_{cf'} + \pi_{c'f} V^*_{c'f}}{\pi_{cf} V^*_{cf} + \pi_{c'f} V^*_{c'f}} \end{aligned}$$

where  $\pi_{cf}$  is the factor-productivity parameter for factor  $f$  of country  $c$ .

## Tables and Figures

Table 1: The Results of SUR estimations

	Physical Capital			Aggregate Labor		
	$\pi_{cf}$	s.e. of $\pi_{cf}$	r-square	$\pi_{cf}$	s.e. of $\pi_{cf}$	r-square
Australia	0.706	0.029	0.758	0.780	0.028	0.662
Belgium	0.660	0.054	0.105	1.127	0.022	0.896
Canada	0.761	0.024	0.847	0.859	0.034	0.590
Denmark	0.654	0.022	0.822	0.867	0.038	0.476
Finland	0.644	0.036	0.563	0.766	0.026	0.692
France	0.817	0.063	0.211	1.079	0.043	0.591
Germany	0.702	0.027	0.788	0.858	0.031	0.666
Italy	0.692	0.031	0.691	1.084	0.032	0.740
Japan	0.505	0.040	0.158	0.733	0.030	0.546
Netherlands	0.702	0.037	0.548	0.926	0.033	0.607
Norway	0.598	0.029	0.667	0.990	0.038	0.625
Spain	0.614	0.039	0.438	0.721	0.021	0.774
Sweden	0.803	0.038	0.663	0.861	0.027	0.738
UK	0.737	0.042	0.517	0.739	0.033	0.457

Note: (1) Dependent variables are the US technology

(2) Sector 1 "Agriculture" is excluded

Table 2: Estimated Factor Augmenting Productivities

	Maskus and Webster (1999)		Trefler (1993)		TFP (5)
	(1) capital	(2) labor	(3) capital	(4) labor	
Australia	0.706	0.780	0.707	0.819	0.655
Belgium	0.660	1.127	0.641	1.072	0.911
Canada	0.761	0.859	0.852	0.861	0.945
Denmark	0.654	0.867	0.800	0.931	0.705
Finland	0.644	0.766	0.620	0.726	0.670
France	0.817	1.079	0.739	1.085	0.953
Germany	0.702	0.858	0.664	0.919	0.811
Italy	0.692	1.084	0.655	1.057	0.782
Japan	0.505	0.733	0.510	0.778	0.634
Netherlands	0.702	0.926	0.683	0.931	0.965
Norway	0.598	0.990	0.711	1.011	0.809
Spain	0.614	0.721	0.589	0.739	0.659
Sweden	0.803	0.861	0.758	0.850	0.793
UK	0.737	0.739	0.898	0.809	0.839
US	1.000	1.000	1.000	1.000	1.000
(1)	1.000	0.349	0.811	0.346	0.687
(2)	-	1.000	0.155	0.964	0.644
(3)	-	-	1.000	0.228	0.592
(4)	-	-	-	1.000	0.643
(5)	-	-	-	-	1.000

Notes: 1) Maskus and Webster (1999) use SUR model. See equation (9).

2) U.S. technology is the explanatory variable for Maskus and Webster.

3) TFP is estimated from CRS Cobb-Douglas production function for 13 manufacturing sectors (exclude "coke, refined petroleum products and nuclear fuel").

Table 3: Results of the HOV Models

I. Strict Models							
	1. The HOV Model			3. The Pairwise HOV Model			5. The Relative HOV Model
	2 factors	capital	labor	2 factors	capital	labor	Capital-Labor
Sign Test	0.567	0.667	0.467	0.548	0.638	0.457	0.438
Slope Test	0.021	0.021	0.019	0.057	0.057	-0.215	0.092
standard error	0.008	0.012	0.020	0.025	0.035	0.039	0.021
R-squared	0.183	0.173	-0.003	0.010	-0.004	0.175	0.160
Variance Test	0.002	0.002	0.006	0.131	0.130	0.193	0.056

  

II. With Factor Productivity Adjustments							
	2. The HOV Model			4. The Pairwise HOV Model			6. The Relative HOV Model
	2 factors	capital	labor	2 factors	capital	labor	Capital-Labor
Sign Test	0.767	0.733	0.800	0.719	0.695	0.743	0.600
Slope Test	0.231	0.231	0.035	0.376	0.376	0.454	0.514
standard error	0.079	0.114	0.090	0.046	0.066	0.086	0.081
R-squared	0.218	0.209	-0.057	0.227	0.216	0.161	0.280
Variance Test	0.233	0.230	0.107	0.594	0.596	0.917	0.943

Notes: 1) The HOV model refers to the testing method in Trefler (1995).

2) The Pairwise HOV model refers to the testing method in Hakura (2001).

3) The Relative HOV model refers to the testing method in Debaere (2003).









