

On the Geographic Implications of Carbon Taxes*

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August 30, 2022

Abstract

A unilateral carbon tax trades off the distortionary costs of taxation and the future gains from slowing down global warming. Because the cost is local and immediate, whereas the benefit is global and delayed, this tradeoff tends to be unfavorable to unilateral carbon taxes. We show that this logic breaks down in a world with trade and migration where economic geography is shaped by agglomeration economies and congestion forces. Using a multisector dynamic spatial integrated assessment model (S-IAM), this paper predicts that a carbon tax introduced by the European Union (EU) and rebated locally can, if not too large, increase the size of Europe's economy by concentrating economic activity in its high-productivity non-agricultural core and by incentivizing immigration to the EU. The resulting change in the spatial distribution of economic activity improves global efficiency and welfare. Other forms of rebating can dilute or revert this positive effect.

1 Introduction

Global carbon taxes have long been heralded as the best solution to combat climate change. The logic is straightforward: they help bridge the gap between the private and social cost of carbon, caused by the negative effects of carbon-induced climate change. Unfortunately, global agreements on climate policy have not been easy to forge. Instead, climate policy has mostly progressed through local, national, and sometimes regional unilateral initiatives. Unilateral policy, however, has the obvious drawback of generating economic and carbon leakage by shifting production and emissions to areas where carbon is taxed less, or not at all. Unilateral carbon taxes therefore seem, at first glance, costly due to the implied short-term distortion, and ineffective in the long run to combat climate change due to the implied leakage. In this paper we argue that this reasoning is incomplete and misleading, because it ignores how unilateral carbon taxes interact with the forces that shape the economic geography of the world. We show that the spatial response to a unilateral carbon tax can lead to a local expansion of the region introducing the tax and to global welfare gains.

Carbon taxes affect primarily industries that use energy intensively. For example, firms in the manufacturing sector tend to be more energy-intensive than in agriculture. Hence, because sectoral specialization exhibits large variation across space, a uniform tax within a region will affect some locations significantly more than others. This heterogeneity in the size of the effective tax will naturally lead to reallocation across space. In an economy with trade and migration where the spatial distribution of economic activity is driven by agglomeration economies and other externalities, this reallocation can trigger a host of indirect effects.

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In particular, they can improve the efficiency of the spatial allocation and result in overall welfare gains. Hence, under certain circumstances, unilateral carbon taxes can improve global welfare by bringing the spatial distribution of economic activity closer to the efficient equilibrium.

Because global warming has different effects across locations, sectors, and time, evaluating the effects of a carbon tax requires a high-resolution multi-sector dynamic spatial integrated assessment model (SIAM). Our quantitative model features a realistic world economy divided into more than 17,000 locations with positive land mass.¹ Firms in multiple sectors can improve their technology by innovating, and sell their products around the world subject to trade costs. Agents work, consume a basket of products, and have the possibility of migrating between locations subject to moving costs. Production uses energy that leads to carbon emissions, which accumulates in the atmosphere, causing global warming. As temperatures rise, they affect firm productivity differentially across sectors. In this model, a carbon tax affects the geography of absolute and comparative advantage, because sectors differ in their energy intensity and because it mitigates global warming. The rebating of the revenue of a carbon tax further impacts relative income across space. In response, migration and trade patterns adjust. Locations that gain population benefit from both static and dynamic agglomeration economies. As the economic geography changes due to a carbon tax, the spatial equilibrium may become more or less efficient, hence impacting welfare positively or negatively.

Our quantitative policy analysis focuses on the European Union (EU) because it is perhaps the region of the world that has been most active in introducing a region-wide tax on carbon (or, equivalently, a carbon trading system). Our evaluation predicts that a hypothetical uniform carbon tax of 40 US\$/tCO₂ introduced by the EU and rebated locally can increase the size of the EU economy by further concentrating economic activity in its high-productivity non-agricultural core and by attracting more immigrants to Europe. This, in turn, leads to a more efficient global distribution of population, so that world welfare improves. Understanding this result requires exploring the spatially heterogeneous effects of a carbon tax on local sectoral specialization and on the spatial distribution of economic activity.

Because non-agriculture is more intensive in energy use than agriculture,, we might have expected an EU carbon tax to weaken Europe’s comparative advantage in non-agriculture, leading to a relative drop in non-agricultural output. If carbon tax revenue were lost, this is indeed what would happen: the increase in the relative price of non-agricultural goods would cause a relative decline of non-agriculture in Europe. The EU would shrink, and global welfare would decline. However, when carbon tax revenue is locally rebated, the results are reversed. The higher relative tax burden in non-agriculture is only partly passed on to wages, so once local rebating is added, regions specializing in non-agriculture experience a relative gain in income. This income effect generates migration from agricultural to non-agricultural regions, causing non-agricultural output to increase relative to agricultural output. This effect is further amplified by agglomeration forces.

As Europe’s non-agricultural core grows, the EU attracts more immigrants, and its economy becomes larger. Although real income per capita in the EU drops, the reallocation of population and economic activity improves global efficiency and welfare. This suggests that in the absence of a carbon tax there is too little geographic concentration in the EU core and there are too few people in Europe. As such, an EU carbon tax with local rebating acts as a place-based policy that subsidizes Europe’s non-agricultural core and as a migration policy that attracts more people to move to the European Union. The importance of these results cannot be overstated: not only does a unilateral EU carbon tax lower global carbon emissions, thus mitigating the warming of the planet, it also increases Europe’s weight in the world economy and it improves global welfare and efficiency. When carbon taxes increase above ~55 US\$ per tCO₂, the distortions

¹The model structure and quantification follows closely the model in [Conte et al. \(2021\)](#).

generated by the tax start to dominate and the EU economy shrinks, although global welfare gains continue for relatively high levels of carbon taxes.

These findings show that using a spatial integrated assessment model (S-IAM) is essential if we want to correctly quantify the economic effects of a carbon tax. Rather than simply imposing a distortionary cost, an EU carbon tax with local rebating corrects a pre-existing spatial inefficiency that would be ignored in a model without the forces that determine the geography of economic activity. One could argue that changes in migration policy would be a more direct way of improving global welfare, or that first-best taxes and subsidies that are heterogeneous across space would be more effective at strengthening Europe’s non-agricultural core. However, in practice no such spatially heterogeneous tax and subsidy scheme is currently on the table, while an EU-wide carbon tax is. In that sense, our contribution should be viewed as a policy-relevant evaluation where we show that a modest unilateral carbon tax can be globally welfare-improving, while locally expanding the size of the economy.

In addition to this key result, our assessment provides comprehensive and detailed insights into how an EU carbon tax with local rebating reshapes the world’s economic geography. Apart from reinforcing the EU’s non-agricultural core, we see southern Europe, Scandinavia, and eastern Europe move more into agriculture. Over time, these patterns are reinforced, with the exception of Scandinavia. There, future agricultural productivity is depressed by a carbon tax that limits global warming. Regions bordering the EU, such as Great Britain, benefit from an industrial revival, as the EU grows and its periphery specializes in agriculture. Outside the EU, the developed world expands, whereas the developing world shrinks, as more people move to higher-income countries.

A consequential policy choice in our model is how the revenue of a carbon tax is rebated. A key driver of the welfare-improving effect of a unilateral carbon tax is that it acts as a subsidy to the spatial agglomeration of economic activity in Europe. That result depends crucially on the local rebating scheme generating a positive income effect in the EU core. To see how sensitive our results are to this type of rebating, we consider several alternatives. First, if revenues of a carbon tax are rebated to the EU population on a per capita basis, the income effect in the EU core is smaller, and the global welfare gains more limited. A carbon tax of 40 US\$ per tCO₂ no longer expands the size of the EU economy, though a lower carbon tax still does. Second, if revenues are rebated to the developing world, less migrants come to Europe and its economy shrinks. By keeping more people in low-productivity places, global efficiency and welfare drop. In contrast, spatial inequality across the globe falls, as income per capita drops in Europe and rises in sub-Saharan Africa.

Our work is related to the large literature on the climate and welfare effects of carbon taxes. Because a decrease in carbon emissions causes a global externality, a central result of this literature is that carbon taxes are only welfare-improving if adopted by a large part of the world. That is why many models have focused on quantifying the optimal global carbon tax (Nordhaus, 2010; Golosov et al., 2014; Hassler et al., 2016, 2018). However, those papers ignore the complex forces that shape the world’s economic geography. Our paper shows that taking these forces into account is key, hence the need for introducing space into standard integrated assessment models.²

Our work expands the growing literature that uses dynamic spatial integrated assessment models (S-IAM) to evaluate the economic impact of climate change. An early S-IAM in one-dimensional space is Desmet and Rossi-Hansberg (2015). Later S-IAMs in two-dimensional space include Desmet et al. (2018),

²See also Weisbach et al. (2022) and Kortum and Weisbach (2021) for an analysis of optimal unilateral carbon policy in a multi-country economy.

Conte et al. (2021), Cruz and Rossi-Hansberg (2021) and Cruz (2021). Other papers in that vein are Conte (2020) and Nath (2020), though they are static and ignore migration as a key adaptation strategy to climate change. Balboni (2019) is another relevant paper that looks at the specific case of flooding and infrastructure investment in Vietnam. Most of these papers do not focus on carbon taxes and policy. An exception is Cruz and Rossi-Hansberg (2021), though that model does not have multiple sectors and does not consider the possibility of unilateral carbon taxes implemented by a subset of the world economy. Cruz and Rossi-Hansberg (2022) do study unilateral carbon policy and the impact of the pledges in the Paris Agreement, but also ignore multiple sectors and the role of different rebating schemes.

The rest of the paper is organized as follows. Section 2 presents a description of our model, describes the local effects of carbon taxes, and discusses the quantification. Section 3 presents the quantitative analysis of the EU carbon policy when the revenue of the tax is discarded. Section 4 present the case when the carbon tax revenue is rebated locally and shows that the tax can lead to an increase in the size of the EU economy as well as global welfare. Section 5 presents the cases of alternative rebating schemes. Section 6 concludes. An Appendix presents additional figures and tables and model details.

2 Model, Data and Calibration

2.1 Model

We extend the dynamic spatial model of Desmet et al. (2018) and Conte et al. (2021) to allow for carbon taxes. This section gives a brief overview of the main elements of the model. We refer the reader to those papers for additional details.

Endowments and preferences. The economy occupies a two-dimensional surface S . A location is a point $r \in S$, with land density $H(r)$. Each of the \bar{L} agents in the economy supplies one unit of labor.

An agent j who resides in location $r \in S$ in period t , and in locations $\{r_0, \dots, r_{t-1}\}$ in the past, has utility

$$U_t^j(r_0, \dots, r_{t-1}, r) = a_t(r) \prod_{i=1}^I \left[\int_0^1 c_{it}^\omega(r)^\rho d\omega \right]^{\frac{\chi_i}{\rho}} \varepsilon_t^j(r) \prod_{s=1}^t m(r_{s-1}, r_s)^{-1} \quad (1)$$

in period t , where $a_t(r)$ is the level of local amenities, $c_{it}^\omega(r)$ is the consumption of variety ω of good i , $1/(1-\rho)$ is the elasticity of substitution between different varieties of the same good, χ_i is the share of good i in the agent's expenditure, $\varepsilon_t^j(r)$ is a location preference shock drawn from a Fréchet distribution with shape parameter $1/\Omega$, and $m(r_{s-1}, r_s)$ is the flow cost of moving from r_{s-1} to r_s in period s .

This setup is characterized by two dispersion or congestion forces. First, locational preference heterogeneity implies that not everyone prefers the same location. The higher the value of Ω , the greater this preference heterogeneity, and hence the stronger this first spatial dispersion force. Second, local amenities are subject to local congestion. More specifically,

$$a_t(r) = \bar{a}(r) \left(\frac{\bar{L}_t(r)}{H(r)} \right)^{-\lambda},$$

where $\bar{L}_t(r)$ denotes the agents residing in r . The higher the value of λ , the stronger this second dispersion force.

The cost of moving from r to s is the product of an origin-specific cost, $m_1(r)$, and a destination-

specific cost, $m_2(s)$, so that $m(r, s) = m_1(r) m_2(s)$. Remaining in the same place is costless, and so $m(r, r) = m_1(r) m_2(r) = 1$. This implies that the cost of leaving a location is the inverse of the cost of entering that location, i.e., $m_2(r) = m_1(r)^{-1}$. As a result, an immigrant only pays the flow utility while residing in the host location. This makes the decision to migrate fully reversible, simplifying an agent's forward-looking migration decision to a static one.

In addition to earning income from work, $w_t(r)$, an agent residing in r at time t gets a proportional share of local land rents, $R_t(r) H(r) / \bar{L}_t(r)$, as well as a proportional share of global profits from the resource extraction sector, Π_t / \bar{L} , and possibly a carbon tax rebate, $b_t(r)$. We can then define $u_t(r)$, the utility level associated with local amenities and real income as

$$u_t(r) = a_t(r) \frac{w_t(r) + \Pi_t / \bar{L} + R_t(r) H(r) / \bar{L}_t(r) + b_t(r)}{\prod_{i=1}^I P_{it}(r)^{\chi_i}}, \quad (2)$$

where P_{it} is the price index of sector i in location r , which we specify below. We use $u_t(r)$ as a measure of social welfare, though it does not include the idiosyncratic preferences of agents for a location nor any mobility costs agents might have incurred. The total nominal income of agents in a location can be written as

$$y_t(r) = w_t(r) \bar{L}_t(r) + (\Pi_t / \bar{L}) \bar{L}_t(r) + R_t(r) H(r) + b_t(r) \bar{L}_t(r). \quad (3)$$

Technology. A firm producing variety ω in sector i in location r at time t uses a production function given by

$$q_{it}^\omega(r) = L_{\phi, it}^\omega(r)^{\gamma_i} z_{it}^\omega(r) L_{it}^\omega(r)^{\mu_i} E_{it}^\omega(r)^{\sigma_i} H_{it}^\omega(r)^{1-\gamma_i-\mu_i-\sigma_i}, \quad (4)$$

where $q_{it}^\omega(r)$ denotes the firm's output, $L_{\phi, it}^\omega(r)$ is innovation labor, $L_{it}^\omega(r)$ is production labor, $E_{it}^\omega(r)$ is energy use, $H_{it}^\omega(r)$ is land use, and $z_{it}^\omega(r)$ is an idiosyncratic productivity shifter drawn from a Fréchet distribution with c.d.f. $Pr[z_{it}^\omega(r) \leq z] = e^{-(Z_{it}(r)/z)^\theta}$ and $\theta > 0$. The average productivity of good i in location r at time t , $Z_{it}(r)$, is given by

$$Z_{it}(r) = \tau_{it}(r) g_i(T_t(r)) (\bar{L}_{it}(r) / H_{it}(r))^{\alpha_i}, \quad (5)$$

where $\tau_{it}(r)$ denotes the location's fundamental productivity in sector i at time t , $g_i(\cdot)$ is a sector-specific temperature productivity discount factor, $T_t(r)$ denotes temperature in r at time t , and $\bar{L}_{it}(r)$ is total sectoral employment, $L_{\phi, it}(r) + L_{it}(r)$. We assume that $\alpha_i > 0$ so average productivity is increasing in local density, $\bar{L}_{it}(r) / H_{it}(r)$. Hence, sectoral productivity benefits from local agglomeration economies. The higher the value of α_i , the stronger these sectoral agglomeration economies. A location's fundamental productivity in sector i evolves according to

$$\tau_{it}(r) = L_{\phi, i, t-1}(r)^{\gamma_i} \left[\int_S e^{-\delta \text{dist}(r, s)} \tau_{i, t-1}(s) ds \right]^{1-\delta} \tau_{i, t-1}(r)^\delta, \quad (6)$$

where $\text{dist}(r, s)$ denotes the geographic distance between locations r and s . A location's fundamental productivity in sector i depends on local past sectoral innovation, local past sectoral productivity, and the spatial diffusion of past sectoral productivity from all other locations. Note that there is a dynamic agglomeration effect whereby more innovation today leads to more population and a larger market, and therefore more

innovation tomorrow. The sector-specific temperature discount factor is bell-shaped in temperature, so

$$g_i(T_t(r)) = \exp \left[-\frac{1}{2} \left(\frac{T_t(r) - g_i^{opt}}{g_i^{var}} \right)^2 \right] \quad (7)$$

where g_i^{opt} denotes the optimal temperature in sector i , and g_i^{var} is a parameter that determines the variance of the bell-shaped relationship between temperature and productivity in sector i .

Firms pay an ad-valorem tax $\Upsilon_t(r)$ on energy expenditure. Because there is a fixed relationship between energy use and carbon emissions, this tax can be interpreted as a carbon tax. Firms are perfectly competitive. Taking all prices and the carbon tax rate as given, a firm producing variety ω of good i chooses its inputs, and therefore its innovation rate, to maximize its static profits

$$p_{it}^\omega(r, r) q_{it}^\omega(r) - w_t(r) [L_{\phi, it}^\omega(r) + L_{it}^\omega(r)] - (1 + \Upsilon_t(r)) e_t E_{it}^\omega(r) - R_t(r) H_{it}^\omega(r) \quad (8)$$

subject to the production function (4), where e_t denotes the global price of energy and $p_{it}^\omega(r, r)$ is the price of variety ω of good i produced and sold in r . Firms maximize static profits because land markets are competitive and any local investment in innovation becomes available to all potential entrants next period. In order to win the competition for land, they optimally choose to innovate, leading to growth in local technology (Desmet and Rossi-Hansberg, 2014; Desmet et al., 2018). All rents from innovation then go to land, which is the only fixed local factor of production.

Energy supply. The world supply of energy is exogenously given by $E_t = e_t^\varphi$, where $\varphi \in (0, 1)$. We ignore resource extraction costs, so that profits are equal to revenue in the energy sector, $\Pi_t = e_t E_t = e_t^{1+\varphi}$.

Carbon cycle and temperature. Carbon emissions caused by the use of energy add to the atmospheric stock of carbon according to

$$K_t = \varepsilon_1 K_{t-1} + \varepsilon_2 E_{t-1}, \quad (9)$$

where $\varepsilon_1 \leq 1$ determines how the carbon stock decays over time, and ε_2 determines how energy use generates carbon emissions that are added to the stock of carbon. Global temperature T_t at time t then evolves with the carbon stock according to

$$T_t = T_{t-1} + \nu (K_t - K_{t-1}), \quad (10)$$

where $\nu > 0$. Changes in global temperatures have heterogeneous effects across space,

$$T_t(r) = T_{t-1}(r) + (T_t - T_{t-1}) \xi(r), \quad (11)$$

where $\xi(r)$ are location-specific downscaling parameters that map changes in global temperature into changes in local temperatures.

Jurisdictions and governments. A jurisdiction J is a set of locations $r \in J$ with a government that sets carbon taxes. Each location r belongs to one jurisdiction and therefore has one government that collects carbon taxes. Government revenues from carbon taxes in location r are

$$A_t(r) = \sum_{i=1}^I \Upsilon_t(r) e_t E_{it}(r) = \sum_{i=1}^I \Upsilon_t(r) e_t \frac{\sigma_i}{\gamma_i + \mu_i} \frac{w_t(r)}{(1 + \Upsilon_t(r)) e_t} \bar{L}_{it}(r) \quad (12)$$

where the second equality comes from the firm's profit maximization problem in sector i and location r . We consider four different schemes for how the government of jurisdiction J rebates carbon tax revenues. First, carbon tax revenues may be lost, in which case $b_t(r) = 0$. Second, carbon tax revenues may be rebated on a per-capita basis to the location that paid them, so $b_t(r) = A_t(r)/\bar{L}_t(r)$. Third, carbon tax revenues of the jurisdiction may be rebated on a per-capita basis to the jurisdiction's population, so $b_t(r) = \sum_{r \in J} A_t(r) / \sum_{r \in J} \bar{L}_t(r)$. Fourth, carbon tax revenues from jurisdiction J may be paid out on a per-capita basis to a set of jurisdictions \mathcal{J} that may or may not include J , so $b_t(r) = \sum_{s \in J} A_t(s) / \sum_{r \in \mathcal{J}} \sum_{r \in \mathcal{R}} \bar{L}_t(r)$.

Prices and export shares. Under perfect competition, the price of a variety produced and consumed at r equals its marginal cost, $p_{it}^\omega(r, r) = \frac{mc_{it}(r)}{z_{it}^\omega(r)}$ where

$$mc_{it}(r) = \gamma_i^{-\gamma_i} \mu_i^{-\mu_i} \sigma_i^{-\sigma_i} (1 - \gamma_i - \mu_i - \sigma_i)^{\gamma_i + \mu_i + \sigma_i - 1} w_t(r)^{\gamma_i + \mu_i} e_t^{\sigma_i} (1 + \Upsilon_t(r))^{\sigma_i} R_t(r)^{1 - \gamma_i - \mu_i - \sigma_i}. \quad (13)$$

The iceberg trade cost from r to s is denoted by $\varsigma(s, r)$. As in Eaton and Kortum (2002), trade is balanced location by location, so the spending of location s on sector- i varieties of location r as a share of its spending on sector- i varieties is given by

$$\pi_{it}(s, r) = \frac{Z_{it}(r)^\theta [mc_{it}(r) \varsigma(s, r)]^{-\theta}}{\int_S Z_{it}(u)^\theta [mc_{it}(u) \varsigma(s, u)]^{-\theta} du}. \quad (14)$$

The price index of sector i at location s is then

$$P_{it}(s) = \bar{p} \left[\int_S Z_{it}(r)^\theta [mc_{it}(r) \varsigma(s, r)]^{-\theta} dr \right]^{-\frac{1}{\theta}}, \quad (15)$$

where $\bar{p} = \Gamma(1 - \frac{\rho}{(1-\rho)\theta})^{-\frac{1-\rho}{\rho}}$ with $\Gamma(\cdot)$ denoting the Gamma function.

Market clearing and equilibrium. Market clearing implies that the revenue of the firms producing varieties of good i at location r equals total spending on these varieties in the entire world. Market clearing for energy requires that worldwide revenues of the energy sector, $e_t^{1+\phi}$, equals worldwide spending on energy net of carbon taxes, $e_t \sum_{i=1}^I \int_S E_{it}(r)$. Hence,

$$e_t = \left[\sum_{i=1}^I \int_S \frac{\sigma_i}{\gamma_i + \mu_i} \frac{w_t(r) \bar{L}_{it}(r)}{1 + \Upsilon_t(r)} dr \right]^{\frac{1}{1+\phi}}. \quad (16)$$

Competitive labor and land markets also clear at all locations.

For a given period t and a given distribution of fundamental amenities $\bar{a}(r)$, productivities $\tau_{it}(r)$, temperatures $T_t(r)$, carbon tax rates $\Upsilon_t(r)$, and carbon revenue rebate schemes, utility maximization of agents, profit maximization of firms, and market clearing conditions determine the world price of energy e_t , profits in the energy sector Π_t , the distribution of population $\bar{L}_t(r)$, utility $u_t(r)$, amenities $a_t(r)$, land rents $R_t(r)$, wages $w_t(r)$, and carbon tax rebates $b_t(r)$ across locations, as well as the distribution of price indices $P_{it}(s)$ and employment $\bar{L}_{it}(r)$ across sectors and locations. The equilibrium conditions of period t , together with (6), yield the distribution of fundamental productivities in period $t + 1$, $\tau_{i,t+1}(r)$. To update the distribution of temperature in $t + 1$, $T_{t+1}(r)$, we use equations (9) to (11).

2.2 The Local Effect of Carbon Taxes

Our goal is to characterize the effect of carbon taxes on the distribution of economic activity and the resulting aggregate effect. To do so it is useful to understand the direct and indirect effects that a carbon tax has on a particular location. Consider first the case of a carbon tax $\Upsilon_t(r)$ on location r , where we throw away the tax revenue, so $b_t(r) = 0$.

Given local wages and rents, equation (13) implies that the marginal cost of producers at r increases with an elasticity of σ_i with respect to the tax. According to equation (14), total expenditures on goods produced in r then decrease with an elasticity of θ relative to the increase in the marginal cost. The reduction in revenues, together with our Cobb-Douglas production function, then implies that total income of agents in location r must decline. That is, local wages and rents fall. This partly offsets the increase in the marginal cost.³ Because local income is lower, location r experiences out-migration. The magnitude of this out-migration depends on the elasticity of population to real income which is governed by Ω , the dispersion in idiosyncratic preferences (which is the inverse of the elasticity of migration to income). The lower Ω , the greater the outmigration, and the larger the drop in output. The falling population leads to smaller static and dynamic agglomeration effects on productivity, which amplify the effect, and smaller congestion forces which attenuate it. The end result is a smaller economy, with less people and less output.

Consider now the more complicated case when we rebate the carbon tax locally, so $b_t(r) = A_t(r)/\bar{L}_t(r)$. The same logic applies to this case, except that the decline in wages and rents does not necessarily lead to lower income and out-migration. Instead, since agents are getting the tax revenue as a rebate, the decline in wages and rents can be less than the rebate, leading to increases in income and in-migration. Whether income increases or not depends on the magnitude of the tax, as well as on the parameter values, in particular, θ and Ω . If the tax is large, its distortionary effect is large too, so that local wages and rents drop substantially. The magnitude of the decline depends on the trade elasticity, θ . The greater its value, the larger the reduction in local revenue. If the fall in income is big, it is not compensated by the tax rebate. This rebate amounts to the fraction of energy expenditures that are taxed rather than paid to energy producers outside the region. If local income drops even when considering the rebate, the location experiences out-migration, leading to a smaller population and a further reduction in output. The lower Ω , the larger this effect.

In contrast, if the tax is sufficiently small, the distortionary effect of the tax will be small. And if θ is low, the drop in income will be small. The rebate, which shifts income from energy suppliers to the local population, compensates this drop and leads to an increase in local income per capita. This attracts an inflow of workers, which attenuates the increase in the marginal cost induced by the carbon tax. Again, this last effect is stronger, the lower is the value of Ω . Hence, if the tax or θ are low enough, local population and output will grow, and these effects will be larger if Ω is small. As before, the expansion of the local economy is amplified by agglomeration effects, and attenuated by congestion forces. In sum, the effect of the tax on the local economy is positive but close to zero when the tax is negligible, grows as the tax increases, and then starts to decline, eventually turning negative, when the tax becomes large enough.

Perhaps surprisingly, the reasoning above implies that a local tax on carbon, if locally rebated, can have positive effects on local output and population. Intuitively, the incidence of the tax falls on all the trading partners of a location, including energy suppliers, but the rebate is only distributed among locals. Hence, if the tax is not too distortionary, locals can command a higher total income, leading to in-migration and an

³If it were fully offset, then total demand for goods produced in r would be the same as before. However, because of the distortionary effects of the tax, production in r drops. With excess demand for goods produced in r , the marginal cost would increase above its original level.

expansion of the local economy. This is reminiscent of arguments on optimal tariffs. As in that literature, a location can change its terms of trade in a way that is beneficial to the local economy. Naturally, if we rebate the revenue in alternative ways that are not local, the effect on the local economy might go from positive with local rebating, to negative if the tax revenue is lost or redistributed uniformly everywhere. Furthermore, if the tax leads to a larger population and GDP, it will lead to higher productivity and more innovation. These static and dynamic agglomeration effects result in even larger increases in the size of the local economy.

Finally, note that a tax on carbon is effectively larger in industries that are intensive in energy; namely, industries with high σ_i . Because of local comparative advantage, this will lead to differences in the effective tax rate across locations. As such, a similar carbon tax leads to larger changes in population and output in regions that are more specialized in industries intensive in energy.

2.3 Data and Calibration

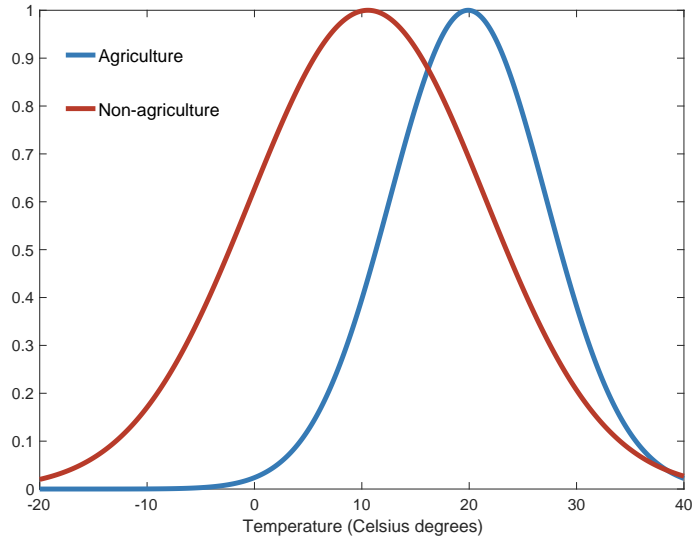
Data. We partition the world into 64,800 $1^\circ \times 1^\circ$ cells, and focus on two sectors, agriculture and non-agriculture. At that level of spatial resolution, our quantification uses initial distributions of population, total output, agricultural output, temperature, and land. These data come from Nordhaus et al. (2006), IIASA and FAO (2012) and IPCC (2020). We also use estimates of bilateral transport costs between any two cells (Desmet et al., 2018).

Parameter values. The parameter values are given in Appendix Table A1 and come mostly from Conte et al. (2021). The carbon cycle parameters are calibrated to emissions consistent with the relatively pessimistic business-as-usual Representative Concentration Pathway (RCP) 8.5. More specifically, we set parameter values so that in the absence of carbon taxes, we get a 1200 GTC increase in the stock of carbon by the end of the 21st century and an increase in global temperature of 3.7°C by 2100. To parameterize the bell-shaped temperature discount function in agriculture, we rely on agronomy studies to estimate an optimal growing season temperature of 21.1°C (or an optimal average annual temperature of 19.9°C). We set the variance parameter of the agriculture discount so that only 0.1% of world agricultural production takes place in locations with a temperature discount factor below 0.01.⁴ For non-agriculture, we calibrate the temperature discount to the observed relation between temperature and the model-generated non-agricultural productivity across grid-cells. This gives us an optimal temperature in non-agriculture of 10.5°C. Figure 1 shows the sectoral temperature discounts. As can be seen, productivity in non-agriculture is less sensitive to temperature relative to agriculture.

A few other parameter values are worth mentioning. First, global warming is heterogeneous across space. We use the location-specific downscaling parameters from Conte et al. (2021) which tell us how much temperature goes up in location r for a one-degree global increase in temperature. Second, our results depend crucially on energy use by sector. For agriculture, Schnepf (2004) estimates direct energy use as share of overall expenditure to be 5.2%. Figures of the Australian Bureau of Statistics for the period 1995-2010 report a figure of 3.4% (Australian Bureau of Statistics, 2021). Taking an average, we use 4%. For non-agriculture, we start with two estimates of the energy share of total GDP: 8% according to Grubb et al. (2018) based on data of 32 OECD countries for the period 1971-2012, and 5.6% according to King et al. (2015) based on data of 44 countries covering almost 95% of world GDP for the period 1980-2010. Combining these two

⁴We use this criterion since otherwise regions that produce some agriculture but have a large temperature discount given their currently low temperatures experience an implausible large boom when temperatures rise.

Figure 1: Temperature Discount in Agriculture and Non-Agriculture



estimates with our parameter values for the share of agriculture in world GDP (5.1%) and the energy share in agriculture (4%) yields an energy expenditure share in non-agriculture of, respectively, 8.2% and 5.7%. Taking an average, we use 7%.⁵

In the model simulations our baseline exercise investigates the impact of a hypothetical European Union-wide carbon tax of 40 US\$/tCO₂. If we take the four largest economies of the European Union as reference, current carbon taxes are 27 US\$/tCO₂ in Germany, 48 US\$ in France, 0 US\$ in Italy, and 16 US\$ in Spain (World Bank, 2022). One unit of energy corresponds to emissions equal to ε_2 GTC, so that one ton of CO₂ corresponds to $1/(3.664 * \varepsilon_2 * 10^9)$ units of energy. Hence, $\Upsilon(r)e_0/(3.664 * \varepsilon_2 * 10^9 * \text{numéraire}) = 40$, where the model's numéraire is the level of average nominal wages in US\$ PPP of 2000. This gives us

$$\Upsilon(r) = \frac{40}{e_0} \times \frac{3.664 * \varepsilon_2 * 10^9}{\text{numéraire}} = 0.863.$$

This is the tax rate on energy spending that corresponds to a carbon tax of 40 US\$/tCO₂ in the first period of our simulation. We maintain this tax rate constant over time.

Solving and simulating the model. Using the initial distributions of land, total population, total output and agricultural output, together with the parameter values and the trade costs, we can back out the distributions of the initial fundamental productivities in agriculture and non-agriculture. We then use data on population and subjective well-being to determine the distribution of fundamental amenities. Moving costs are then set to match the model-predicted changes in population between 2000 and 2005. Using the equilibrium allocation in period t , we can determine fundamental productivities and local temperatures in period $t + 1$. This allows us to solve for sectoral employment levels, wages, and prices in $t + 1$. Using this algorithm, we can simulate the model forward for as many periods as needed.

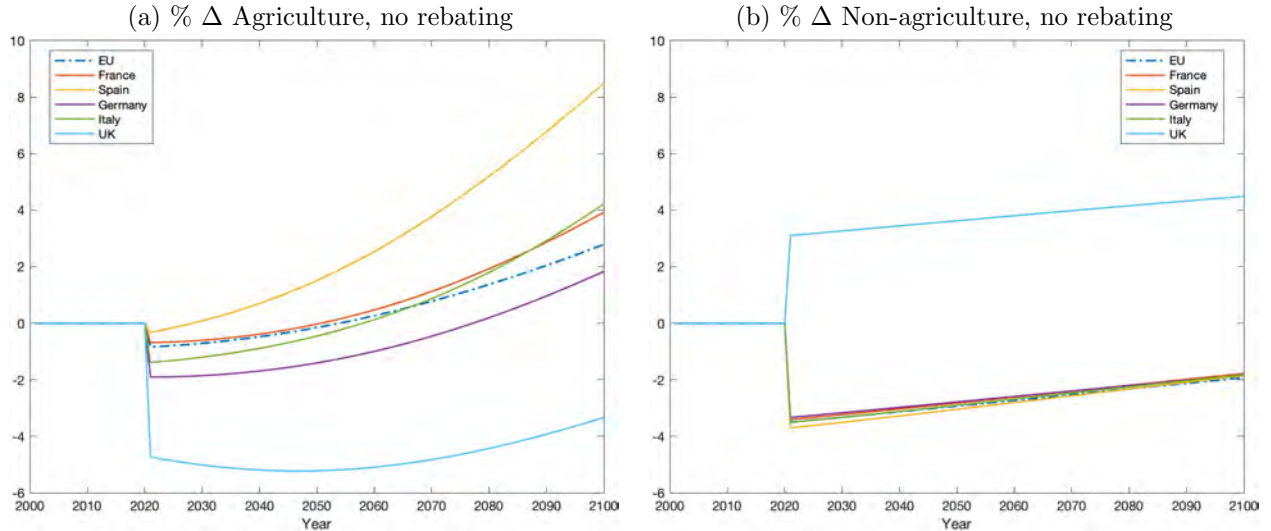
⁵Alternatively, we could define non-agriculture to be industry. For the energy expenditure share in industry, Grave et al. (2016) estimate a weighted average of 7.7% across 14 manufacturing sectors for the year 2011, whereas the Australian Bureau of Statistics estimates an energy share in manufacturing of 6.4% for the period 1995-2010 (Australian Bureau of Statistics, 2021). This also gives an average of around 7%.

3 Carbon Taxes without Rebating

Starting in the year 2000, we simulate our model forward for 100 periods, until the year 2100. For the first 20 periods, there is no carbon tax anywhere. In 2021, the European Union introduces a unilateral tax rate on energy spending of $\Upsilon(r) = 0.863$, equivalent to a carbon tax of 40 US\$/tCO₂. In this section, we assess the spatial effects and the welfare impact of this carbon tax in the absence of rebating. While in practice it is unlikely that carbon tax revenues will be lost, we start with this evaluation because it will facilitate the understanding of our findings when we introduce alternative rebating schemes.⁶

Sectoral specialization. Figure 2 depicts, for different European countries, the percentage difference in agricultural and non-agricultural nominal output between the baseline with a carbon tax and a counterfactual exercise without such a tax. Upon impact, in 2021, the carbon tax has two effects. On the one hand, in the absence of rebating, the EU economy shrinks, leading to a drop in output across the board. On the other hand, the lower energy intensity of agriculture implies that comparative advantage in the EU shifts towards agriculture. Taking the two effects together, for the EU as a whole we see a larger output drop in non-agriculture (-3.44%) than in agriculture (-0.83%). As for the UK, a border country outside the EU, the changing comparative advantage of its neighbor causes a drop in agricultural output and an increase in non-agricultural output. After the initial shock to comparative advantage, innovation allows countries to over time regain part of the lost output.

Figure 2: Change in Sectoral Output Due to Carbon Taxes (No Rebating), Select Countries



Note: Figure displays for different countries the log difference (*100) in nominal sectoral output between the baseline with carbon taxes (and no rebating) and a counterfactual without a carbon tax. Formally, for country C and sector i , it measures the difference in $100 * \log(\sum_{r \in C} w_t(r) \bar{L}_{it}(r))$ (which is a fixed share of nominal output) with and without carbon taxes. Panel (a) refers to agricultural nominal output, and Panel (b) to non-agricultural nominal output.

Figure 3 displays the change in sectoral output due to the carbon tax on a map of Europe and its neighbors in 2021 (top row) and 2100 (bottom row).⁷ Upon impact, carbon taxes lower EU nominal output

⁶Of course, this exercise could also be interpreted as an analysis of the effect of an increase in a region's carbon price due to outside factors such as restrictions in world supply.

⁷In Panels (b) and (d) that display the change in non-agricultural output, a few cells exhibit very large percentage changes.

in both sectors, especially in non-agriculture, but there are some notable differences across regions (Panels (a) and (b)). Agriculture declines relatively less in the EU periphery than in its core. In fact, in Ireland, Sweden, Finland and Bulgaria, some areas see an increase in agricultural activity. Conversely, non-agriculture drops across the EU, but slightly less in the core. By the year 2100, Panel (c) shows that agriculture expands in the EU, especially in the southernmost peripheral regions as well as in Ireland. The northernmost peripheral regions do not experience this gain in agriculture, as the carbon tax limits the rise in temperature that benefits them. Non-agriculture partly recovers from the initial shock, though output is still lower than in a world without carbon taxes (Panel (d)).

As for regions neighboring the EU, they are affected by both the shrinking EU market and the gain in EU comparative advantage in agriculture. Both forces lead to a drop in agricultural activity in neighboring regions. In contrast, the two forces have opposite effects on non-agricultural output in neighboring regions. The maps show that the shift in comparative advantage is more important: neighboring regions mostly experience an increase in non-agricultural output. For regions further afield, Appendix Figure B1 and Figure B2 display similar maps for the entire world. The model-predicted numbers for different regions of the world are given in Table 1. Because of lower carbon emissions, global warming slows down. Focusing on 2100, this hurts agricultural output in regions that benefit from climate change, such as Siberia and Canada, and it helps agricultural output in regions that gain from less warming, such as South and East Asia.

Table 1: Effect of Carbon Tax on Different Regions of the World (No Rebating)

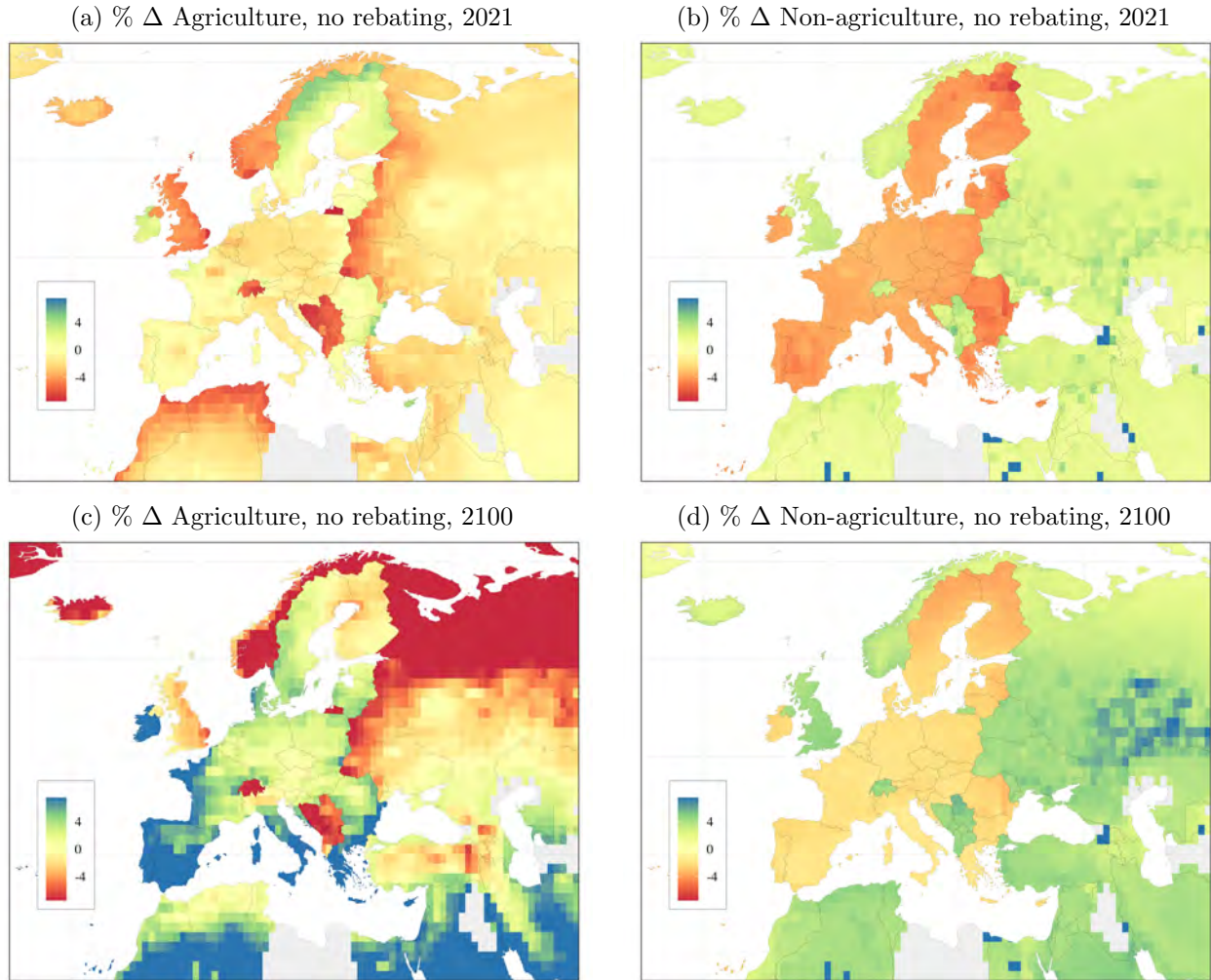
	World		EU		US		Japan		SSA		S. & E. Asia	
	2021	2100	2021	2100	2021	2100	2021	2100	2021	2100	2021	2100
%Δ Real income	-0.65	-0.67	-4.95	-4.32	2.03	3.11	1.88	2.91	-3.11	-6.1	-1.34	-1.62
%Δ Real income pc	-0.65	-0.67	-3.3	-3.18	-0.2	0.1	-0.27	0.03	-0.96	-2.36	-1.2	-1.42
%Δ Welfare	-0.62	-0.57	-2.76	-2.86	-0.93	-0.84	-0.97	-0.88	-2.51	-3.53	-1.72	-2.11
%Δ Population	0	0	-1.71	-1.17	2.23	3	2.16	2.87	-2.17	-3.83	-0.15	-0.2
%Δ Agricultural output	-0.07	0.86	-0.83	2.83	-0.07	0.63	-0.07	1.93	-0.46	1.56	0.58	1.96
%Δ Non-agric. output	0.74	1.94	-3.44	-1.91	2.75	4.69	2.41	4.11	0.25	0.67	0.63	1.97
%Δ Emissions	-2.16	-2.71	-43.42	-41.24	12.13	16.83	11.77	16.19	9.36	12.36	9.83	13.8

Note: For different variables and regions of the world, Table displays log difference (*100) between the baseline with a carbon tax and no rebating and a counterfactual without a carbon tax. SSA refers to Sub-saharan Africa, and S. & E. Asia refers to South and East Asia, which includes Bangladesh, Brunei, China, Indonesia, India, Cambodia, Laos, Sri Lanka, Myanmar, Malaysia, Philippines, Thailand, and Vietnam.

Real income, population and welfare for different tax levels. Figure 4 Panel (a) displays the change in real income and population in the EU in 2021 as a function of the level of the carbon tax. As expected, the higher the carbon tax, the more the EU economy shrinks. For a carbon tax of 40 US\$/tCO₂, the drop in EU real income is 4.95% in 2021. This drop is due partly to the revenues of the carbon tax not being rebated, partly to the distortionary effects of the carbon tax, and partly to the drop in population. The shrinking of the EU economy because of the distortionary impact of the carbon tax is reflected in Panel (b), where we see output in both sectors monotonically decline with the level of the carbon tax. Because EU comparative advantage is shifting toward agriculture, the drop is greater in non-agriculture. Panel (c) shows that a carbon tax makes the EU worse off at impact: real income per capita and welfare decline in 2021. For a carbon tax of 40 US\$/tCO₂, the reduction in real income per capita in the EU is 3.3% in 2021 (Table 1). This explains the loss in population in the EU, observed in Panel (a). When considering sectoral output

These cells are characterized by discontinuities in the underlying data, either because they have almost no population or almost no non-agricultural output. The same discontinuities show up in some other maps, such as Figures B1 and B2.

Figure 3: Change in Sectoral Output Due to Carbon Taxes (No Rebating), Europe



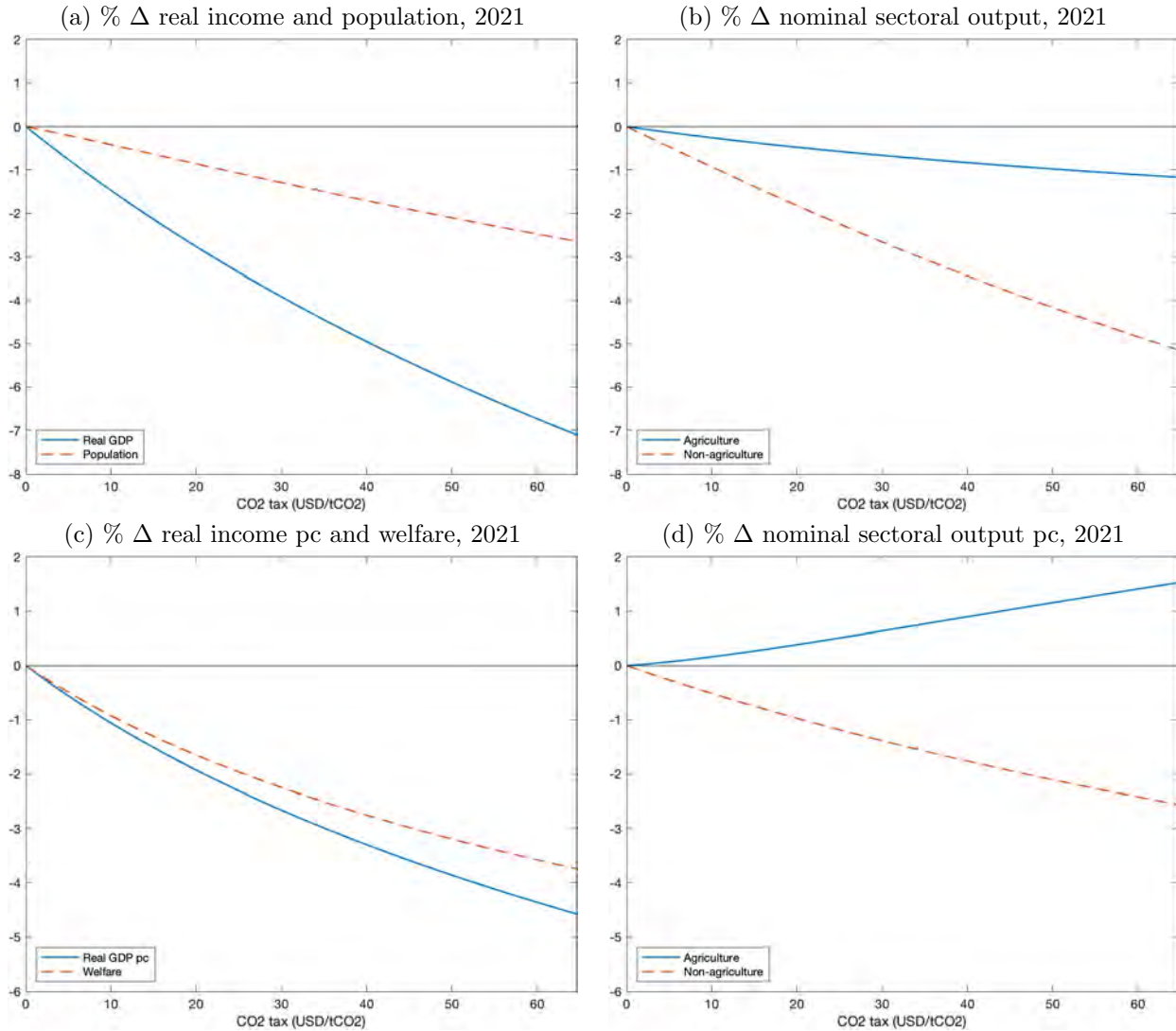
Note: Map displays for different countries the log difference in nominal sectoral output between the baseline with a carbon tax (and no rebating) and a counterfactual without a carbon tax. Panels (a) and (c) refer to agricultural nominal output, and Panels (b) and (d) to non-agricultural nominal output. Panels (a) and (b) are for 2021, whereas Panels (c) and (d) are for 2100.

per capita, Panel (d) shows an increase in agriculture and a drop in non-agriculture. This is consistent with a shift in comparative advantage, away from non-agriculture, due to a concentration of agricultural output in the most productive regions of the EU.

Figure 5, Panels (a) and (b) map the effect of carbon taxes on real income across the world for the years 2021 and 2100. As we already know, real income declines in the EU. Two forces determine which other regions of the world lose and which ones gain. On the one hand, regions with stronger comparative advantage in agriculture, such as Brazil and sub-Saharan Africa, are more likely to lose, because the EU experiences a relative shift into agriculture. In contrast, regions that specialize in non-agriculture, such as North America, Australia and Japan, tend to gain. On the other hand, carbon taxes limit global warming over the next century, hurting regions that stand to benefit in the future from higher temperatures and hurting the ones that stand to lose. Consistent with this, in 2100 higher EU carbon taxes are expected to hurt northern Canada and northern Siberia, but benefit Mexico.

Panel (c) of the same figure shows which regions gain and which regions lose in terms of real income per

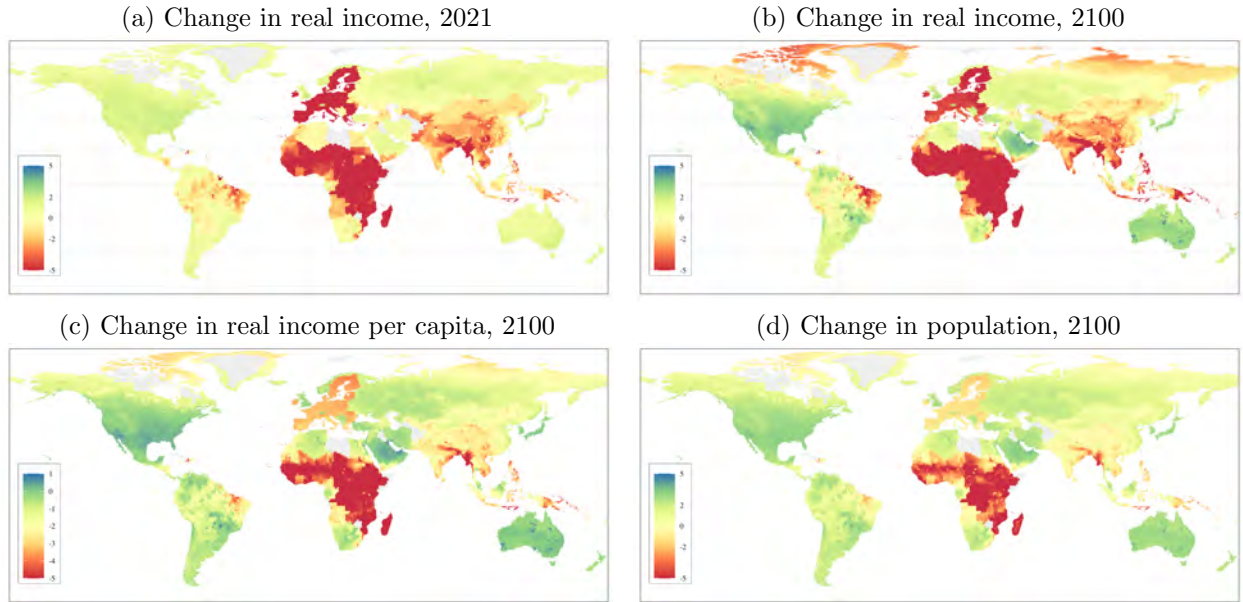
Figure 4: Effect of Carbon Tax on EU Economy (No Rebating), 2021



Note: For different EU variables, Figure displays the log difference ($\times 100$) in 2021 between the baseline with carbon taxes (and no rebating) and a counterfactual without carbon taxes. Panel (a) shows EU real income and population, Panel (b) shows EU nominal sectoral output, Panel (c) shows EU real income per capita and welfare, and Panel (d) shows EU nominal sectoral output per capita.

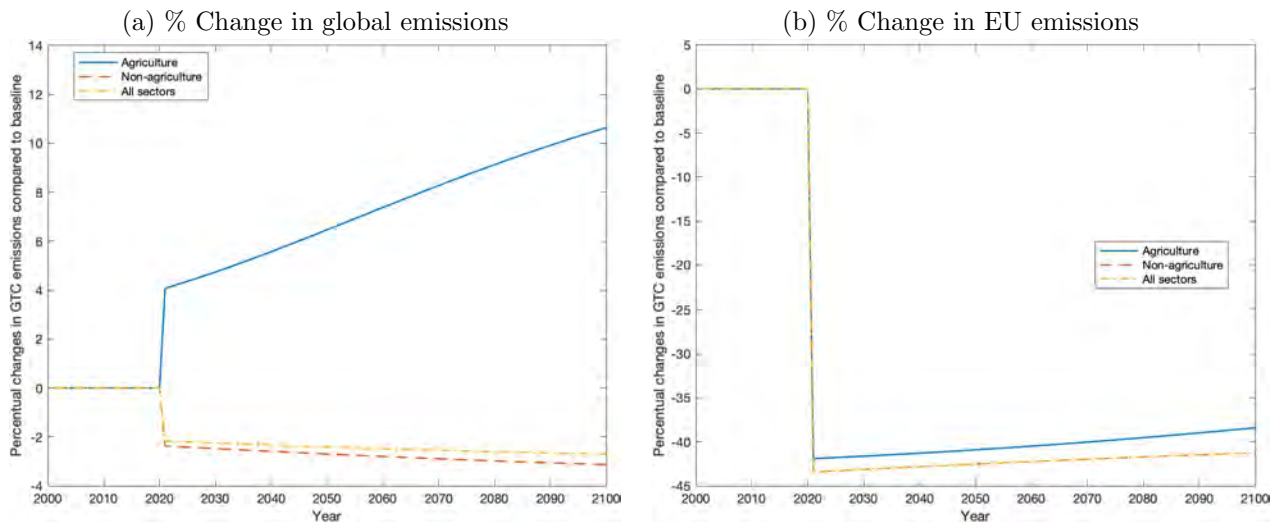
capita in 2100 due to carbon taxes. North America, Australia, Argentina and Japan gain, whereas Europe, most of sub-Saharan Africa, parts of Brazil, and many regions of East Asia lose. Because carbon taxes mitigate global warming, northern Siberia and northern Canada also lose. More specifically, real income per capita in 2100 increases by 0.1% in the US and by 0.03% in Japan, and it declines by 2.36% in sub-Saharan Africa and by 1.42% in South and East Asia (see Table 1). Overall, the winners do not compensate for the losers: in the absence of rebating, global real income per capita declines by 0.67% in 2100. Population changes mirror real income per capita changes, as migration patterns adjust to changes in real income per capita (Panel (d)). Compared to a world without an EU carbon tax, in 2100 population is predicted to fall by 1.17% in the EU, by 3.83% in sub-Saharan Africa and by 0.2% in South and East Asia, whereas population is predicted to increase by 3% in the US (Table 1).

Figure 5: Effect of Carbon Tax and Real Income and Population across the Globe (No Rebating)



Note: Map displays for different variables the log difference (*100) between the baseline with carbon taxes (and no rebating) and a counterfactual without carbon taxes. Panel (a) shows real income in 2021, Panel (b) shows real income in 2100, Panel (c) shows real income per capita in 2100, Panel (d) shows population in 2100.

Figure 6: Effect of Carbon Tax on Global and EU Emissions (No Rebating)



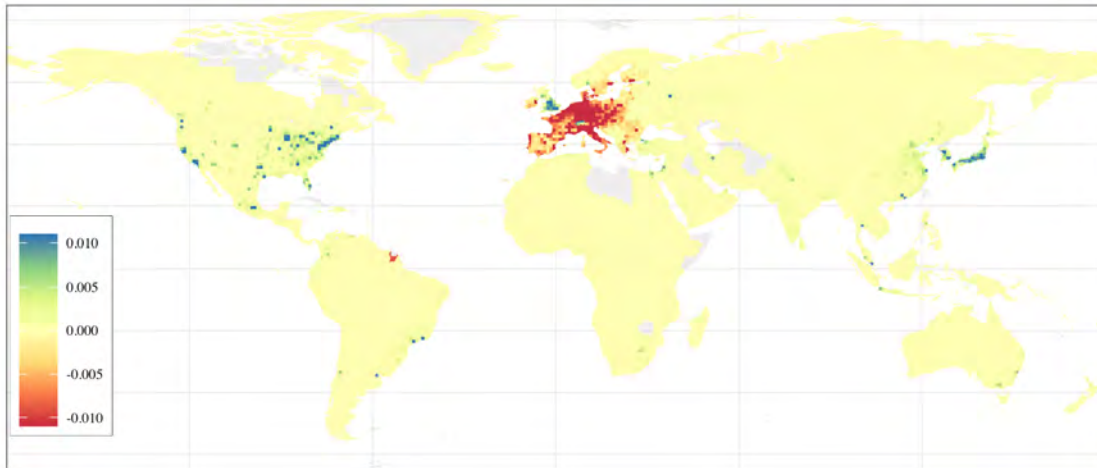
Note: Figure displays log difference (*100) in emissions between the baseline with carbon taxes (and no rebating) and a counterfactual without carbon taxes. Panel (a) shows global emissions and Panel (b) shows EU emissions.

Emissions. As expected, a carbon tax in the EU leads to a reduction in emissions in the EU (Figure 6, Panel b). This reduction is apparent in both sectors, reflecting the overall shrinking of the EU economy. The overall drop in EU emissions in 2100 is 41%. Globally, emissions drop by almost 3% in 2100. The small drop of global emissions is partly the result of the size of the EU in the global economy but also of carbon leakage, by which production is shifted to other regions. Interestingly, global emissions increase in agriculture but decrease in non-agriculture. Given that Europe becomes more specialized in agriculture,

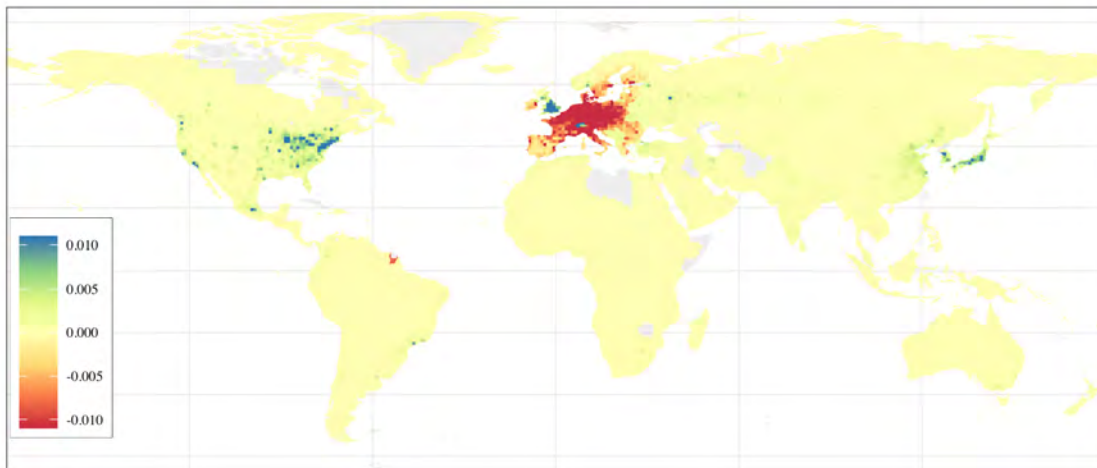
we might have expected the carbon leakage in non-agriculture to be greater. However, several forces work in the other direction. First, non-agriculture is being displaced towards high-productivity regions, with therefore relatively low emissions per unit of output. Second, carbon taxes limit global warming, and reduce agricultural production in places such as Siberia that would acquire high agricultural productivity in the absence of carbon taxes. Instead, agriculture expands in less efficient areas, such as sub-Saharan Africa and parts of Asia.

Figure 7: Effect on Carbon Tax on Emissions around the World (No Rebating), 2021 and 2100

(a) Change in emissions, 2021



(b) Change in emissions, 2100



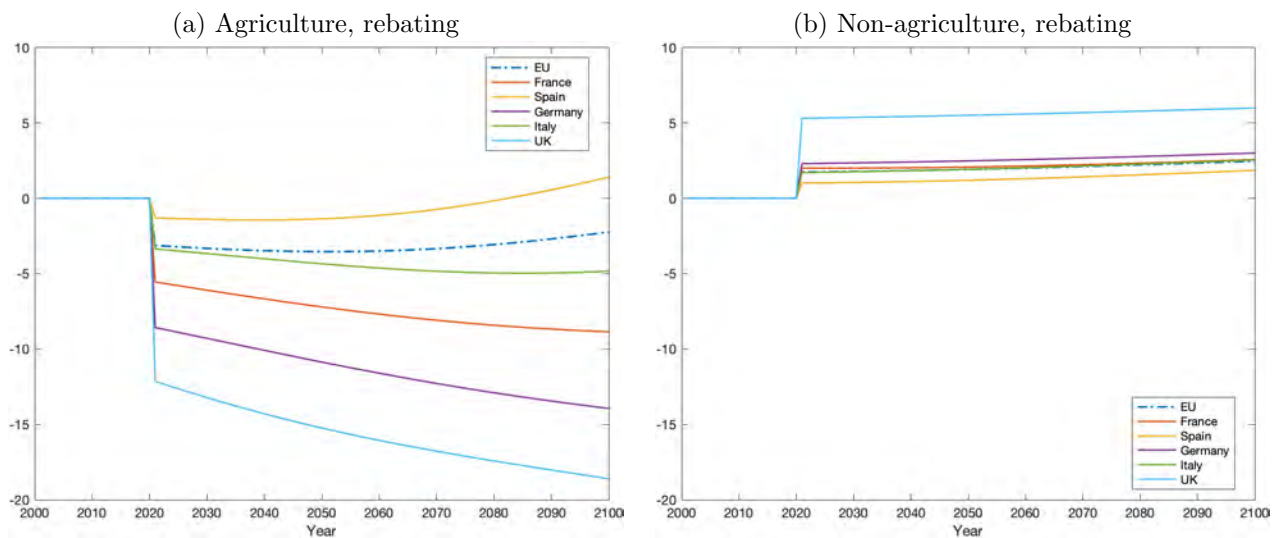
Note: Maps display differences in emission levels (in tCO_2) between the baseline with a carbon tax (and no rebating) and a counterfactual without a carbon tax. Figure B3 shows the equivalent European map.

Figure 7 shows a global map of the changes in emissions in 2021 and 2100. Across Europe we see a decline in emissions, especially in the non-agricultural core and less so in the periphery. Carbon leakage increases emissions across the world, and especially in regions that specialize in non-agriculture. For example, in 2100 the model predicts emissions to increase by 17% in the US and 16% in Japan. Though less apparent in the map due to the low base, emissions are also set to increase in sub-Saharan Africa (by 12%). In a world with less global warming, that region continues to specialize in relatively low-productivity agriculture.

4 Carbon Taxes with Local Rebating

We now proceed to analyze the case where the carbon tax revenue is rebated on a per-capita basis to the cell that paid the tax. Because the combination of taxes and rebates changes the spatial distribution of income, it has an impact on migration. And since the initial spatial distribution of economic activity is not efficient due to static and dynamic externalities, there is a possibility that this policy improves overall efficiency. In addition, since the carbon tax slows down global warming, it obviously also impacts output and welfare through that channel.

Figure 8: Change in Sectoral Output Due to Carbon Taxes (Local Rebating), Select Countries

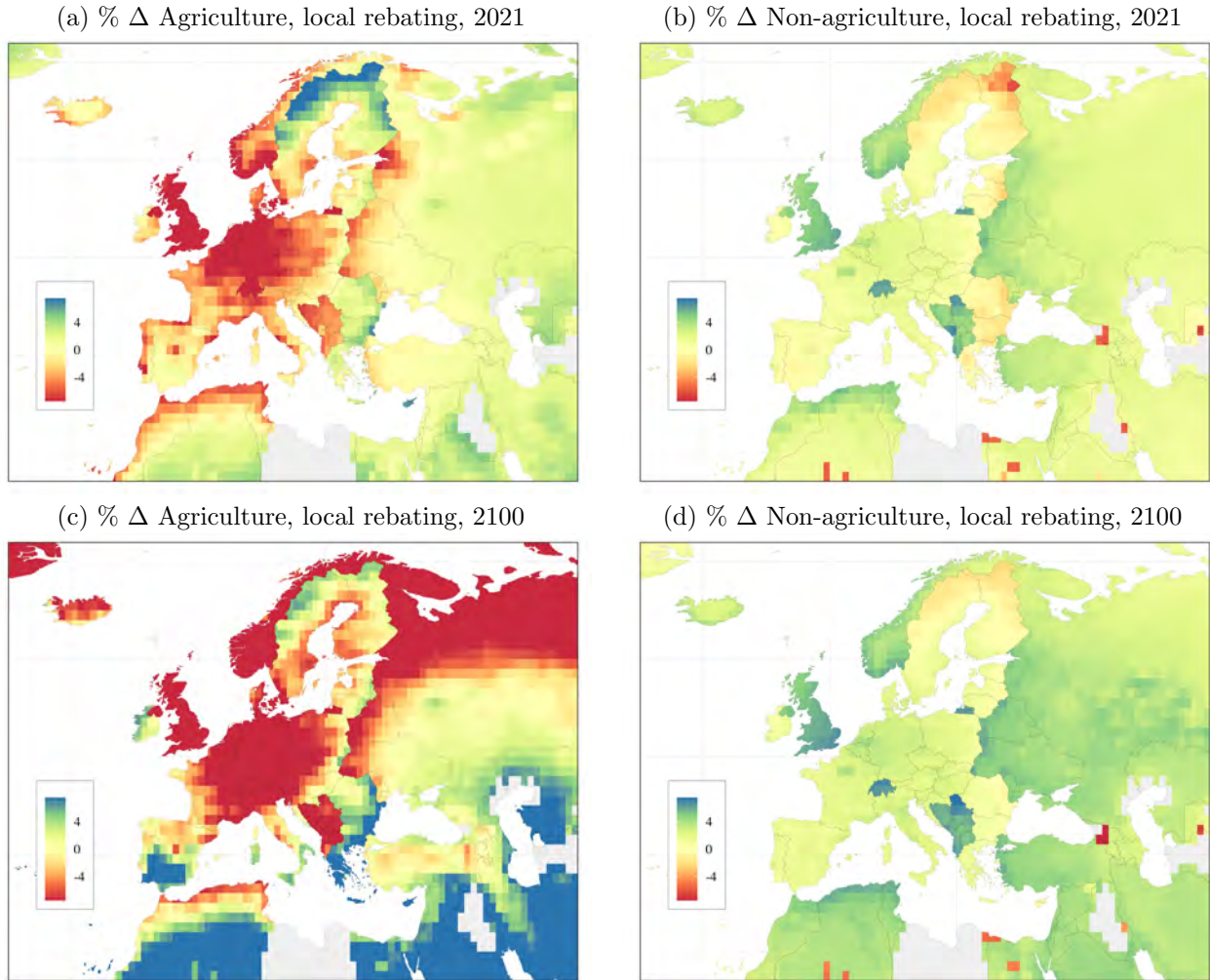


Note: Figure displays for different countries the log difference (*100) in nominal sectoral output between the baseline with carbon taxes (and local rebating) and a counterfactual without a carbon tax. Panel (a) refers to agricultural nominal output, and Panel (b) to non-agricultural nominal output.

Sectoral specialization. Non-agriculture is more energy-intensive, so it is harder hit by a carbon tax than agriculture. Because the direct effect of such a tax is a reduction of the EU’s comparative advantage in non-agriculture, we would expect a relative drop in non-agricultural output. In fact, this is precisely what we saw in Figure 2. However, once we introduce local rebating, this result is reversed: Figure 8 shows that EU output in non-agriculture grows relative to agriculture. So how and why does local rebating change the result? Carbon taxes increase the relative price of non-agricultural goods, so that the higher carbon tax incidence in non-agriculture is not fully passed on to lower wages in regions specialized in non-agriculture. Once carbon tax revenue is rebated locally, these non-agricultural regions experience an increase in income per capita relative to the rest of the EU if the distortionary effect of the tax is not too strong (as we discussed in Section 2.2). This income effect generates migration from the agricultural regions to the non-agricultural regions of the EU. This effect is further magnified by agglomeration forces and moderated by congestion forces. As a result, we observe an increase in non-agricultural output, and a decrease in agricultural output.

Because local rebating benefits the non-agricultural regions of the EU, it strengthens the core region of the union, in particular, the area covering Germany, the Benelux, northern and eastern France, and northern Italy (Figure 9). This roughly coincides with an area sometimes called Europe’s “blue banana”, in reference to the shape of the region and the color of the European Union flag. As such, the carbon tax causes a

Figure 9: Change in Sectoral Output Due to Carbon Taxes (Local Rebating), Europe

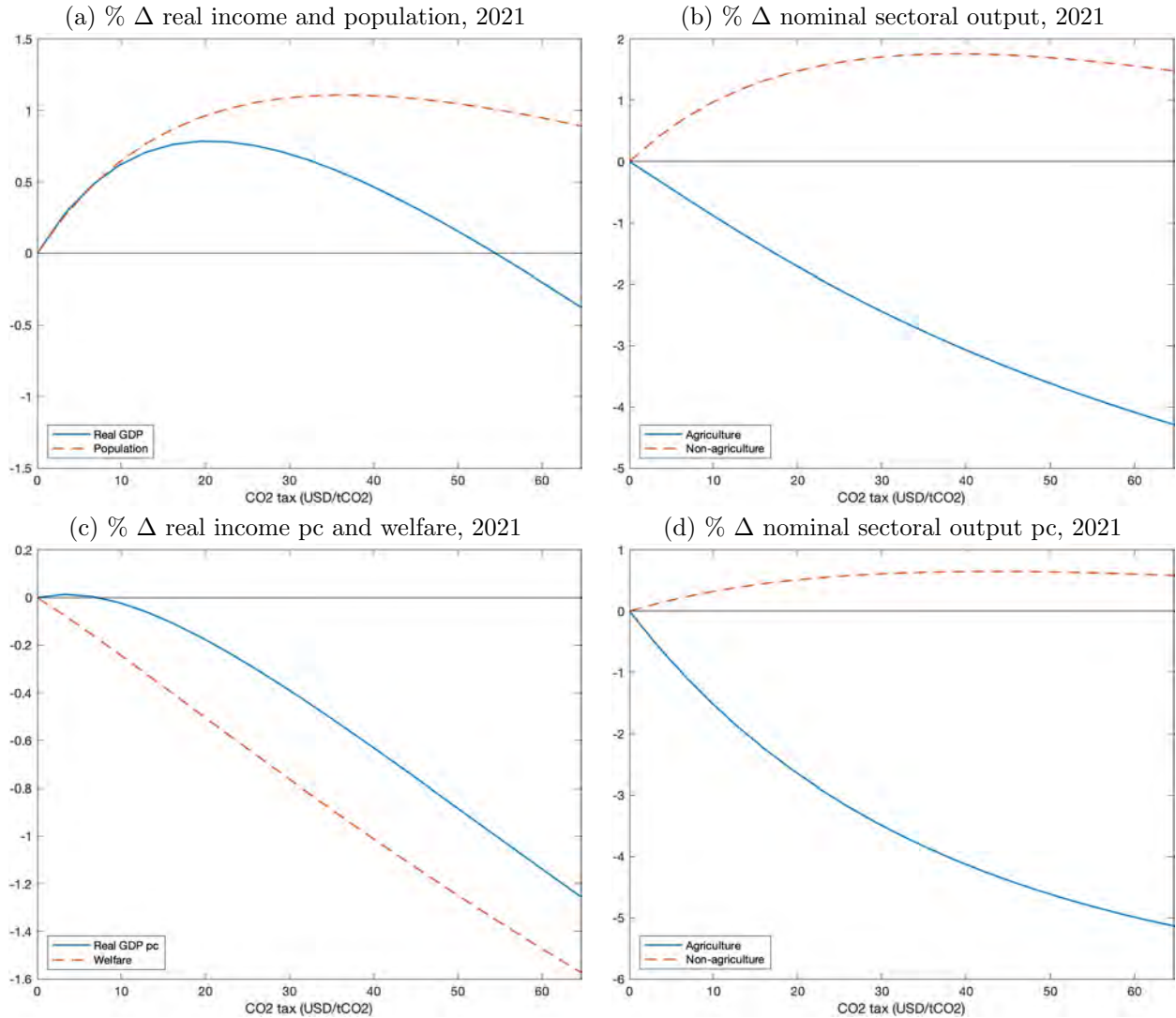


Note: Map displays the log difference ($\times 100$) in nominal sectoral output between the baseline with a carbon tax (and local rebating) and a counterfactual without a carbon tax. Panels (a) and (c) refer to agricultural nominal output, and Panels (b) and (d) to non-agricultural nominal output. Panels (a) and (b) are for 2021, whereas Panels (c) and (d) are for 2100.

recentralization of the EU, and a strengthening of its non-agricultural base. Because the increased density of the core enhances its comparative advantage, it leads to a drop in agricultural output in those regions. In contrast, agriculture expands in countries and regions of the EU periphery, such as Sweden, Finland, southern Spain, Romania, Bulgaria, and Greece. By the year 2100, these patterns get further magnified, except in Scandinavia. There, the growing comparative advantage in agriculture due to global warming is eroded by carbon taxes that limit emissions and keep temperatures lower. In regions bordering the EU, we see a clear decline in agricultural activity and an increase in non-agricultural activity. This shift is expected, given their proximity to the EU periphery which shifts increasingly into agriculture. Taken together, we see that carbon taxes with local rebating have rich and spatially heterogeneous effects on specialization across the EU and its bordering regions.

Real income, population and welfare for different tax levels. While it would be natural to expect the EU economy to shrink by less if the carbon tax is rebated locally, Figure 10 Panel (a) shows that the EU

Figure 10: Effect of Carbon Tax on EU Economy (Local Rebating), 2021



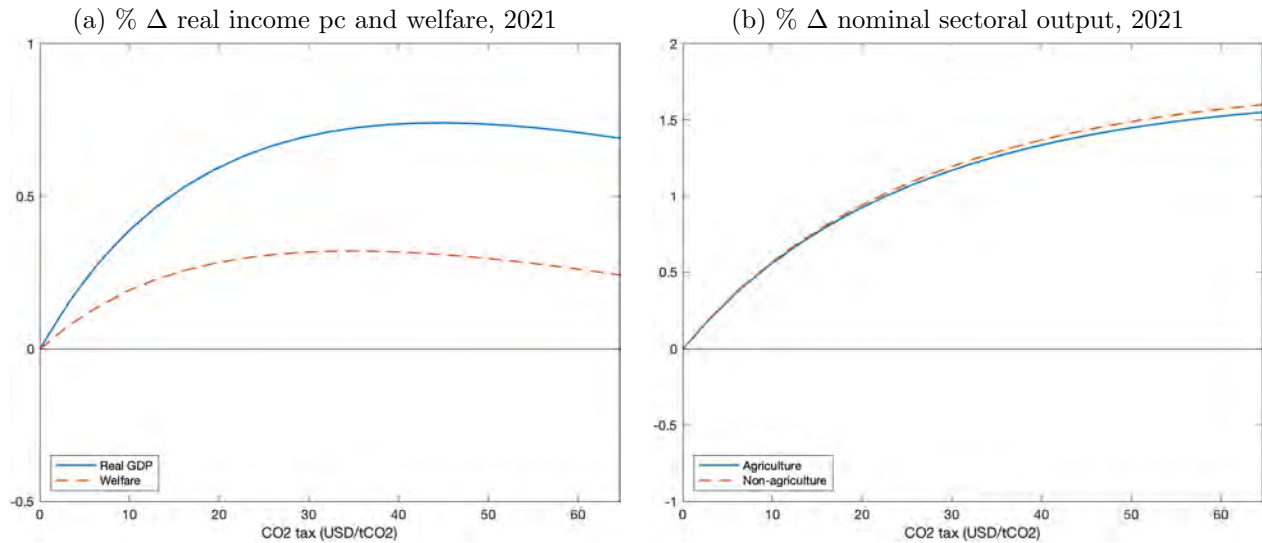
Note: For different EU variables, Figure displays the log difference (*100) in 2021 between the baseline with carbon taxes (and local rebating) and a counterfactual without carbon taxes. Panel (a) shows EU real income and population, Panel (b) shows EU nominal sectoral output, Panel (c) shows EU real income per capita and welfare, and Panel (d) shows EU nominal sectoral output per capita.

economy actually expands at impact. For a carbon tax of 40 US\$/tCO₂, EU real income increases by 0.47% in 2021 (Table 2). The EU economy expands partly because people move to Europe. Under the baseline carbon tax, population in the EU goes up by 1.1% in 2021. Welfare in the EU falls, and this loss is increasing in the level of the carbon tax (Panel (c)). However, output per capita in non-agriculture increases, even for large carbon taxes. This, again, illustrates the strengthening of the EU core as a non-agricultural production hub.

World real income per capita and welfare improves due to the EU carbon tax, with world output increasing in both sectors (Figure 11). With local rebating, the EU carbon tax leads to a more efficient distribution of economic activity across the globe. Although for the baseline tax real income per capita in 2021 declines in all major regions (-0.63% in the EU, -0.22% in the US, -0.96% in sub-Saharan Africa, and -1.14% in Asia), world real income per capita increases by 0.74%. This global gain occurs because more

people move to the productive areas of the world. For a carbon tax of 40 US\$/tCO₂, population in 2021 increases in the EU, the U.S., and Japan, and drops in sub-Saharan Africa and South and East Asia. By 2100, some of the major regions, such as the U.S., gain in terms of real income per capita. For the world as a whole, in 2100 real income per capita is predicted to increase by 1.25% in response to the carbon tax. As expected, population changes follow real income per capita changes. Figure 12 depicts this on a world map. Appendix Figure B4 shows that the global efficiency and global welfare effects of the EU carbon tax are robust to changes in θ and Ω .

Figure 11: Effect of Carbon Tax on World Economy (Local Rebating), 2021



Note: For different world variables, Figure displays the log difference (*100) in 2021 between the baseline with carbon taxes (and local rebating) and a counterfactual without carbon taxes. Panel (a) shows world real income per capita and welfare, Panel (b) shows world nominal sectoral output per capita.

Table 2: Effect of Carbon Tax on Different Regions of the World (Local Rebating)

	World		EU		US		Japan		SSA		Asia	
	2021	2100	2021	2100	2021	2100	2021	2100	2021	2100	2021	2100
% Δ Real income	0.74	1.25	0.47	1.16	1.72	2.69	1.52	2.48	-3.43	-6.46	-1.46	-1.8
% Δ Real income pc	0.74	1.25	-0.63	-0.5	-0.22	0.07	-0.31	0	-0.96	-2.37	-1.14	-1.34
% Δ Welfare	0.32	0.77	-1.01	-1.08	-0.84	-0.73	-0.89	-0.79	-2.42	-3.41	-1.57	-1.94
% Δ Population	0	0	1.1	1.66	1.94	2.61	1.84	2.47	-2.5	-4.19	-0.33	-0.46
% Δ Agricultural Output	1.34	2.74	-3.07	-2.21	2.47	5.63	2.96	6.96	1.13	2.86	2.35	4.14
% Δ Non-agric. Output	1.37	2.76	1.76	2.5	1.34	2.97	0.46	2.41	-0.46	0.15	-0.64	0.55
% Δ Emissions	-2.15	-2.66	-40.46	-38.73	10.55	14.7	9.6	14.08	8.72	11.62	8.76	12.58

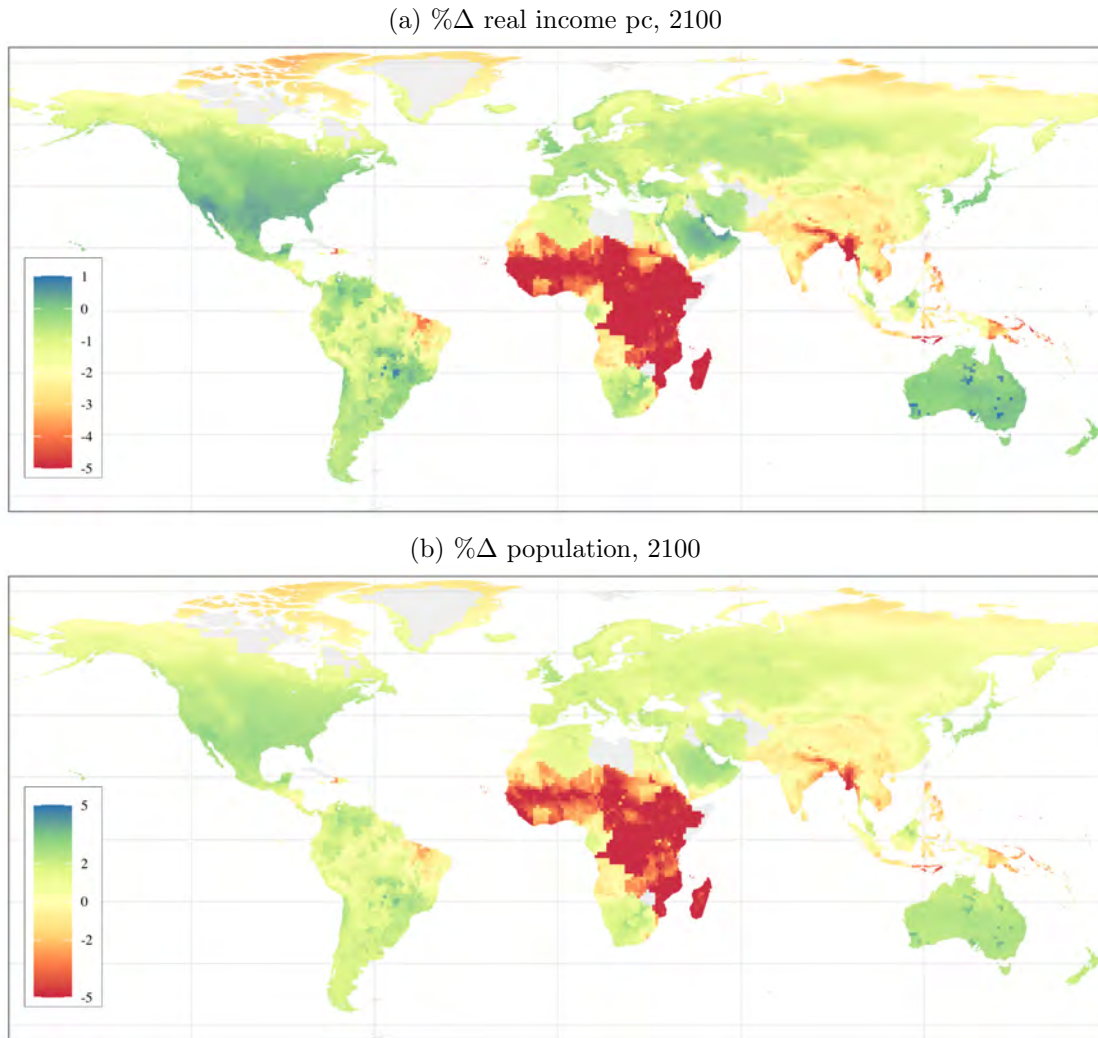
Note: For different variables and regions of the world, Table displays log difference (*100) between the baseline with a carbon tax and local rebating and a counterfactual without a carbon tax. SSA refers to Sub-saharan Africa, and S. & E. Asia refers to South and East Asia, which includes Bangladesh, Brunei, China, Indonesia, India, Cambodia, Laos, Sri Lanka, Myanmar, Malaysia, Philippines, Thailand, and Vietnam.

The overall gain in real income per capita and the greater weight of the EU economy point to carbon taxes and rebates correcting pre-existing inefficiencies. In the baseline without a carbon tax, there is not enough economic activity in the EU non-agricultural core and there is insufficient migration to the EU. The carbon tax with local rebating acts as a place-based policy that subsidizes the non-agricultural core, and as an immigration policy that incentivizes people to move to the EU. As Europe's weight in non-agriculture

increases, regions such as sub-Saharan Africa and South and East Asia increasingly revert back to agriculture. As this increases income per capita differences, there is outmigration from those regions to the EU and other developed regions across the globe. These flows improve global real income per capita and welfare. This suggests that an EU carbon tax may lead to a double win for the world: it increases global welfare and it reduces emissions and global warming. From the point of the EU, it increases the weight of its economy and it reinforces its non-agricultural core.

However, these positive effects come at the cost of greater spatial inequality. Table 2 shows larger real income per capita losses in 2100 in low-income regions, such as sub-Saharan Africa (-2.37%) and South and East Asia (-1.34%), than in high-income regions, such as the European Union (-0.5%) and the US (+0.07%). Welfare effects in these regions follow similar patterns.

Figure 12: Effect of Carbon Tax on Real Income per Capita and Population across the Globe (Local Rebating)



Note: For different variables, map displays log difference ($\times 100$) in 2100 between the baseline with carbon taxes (and local rebating) and a counterfactual without carbon taxes. Panel (a) shows real income per capita and Panel (b) shows population.

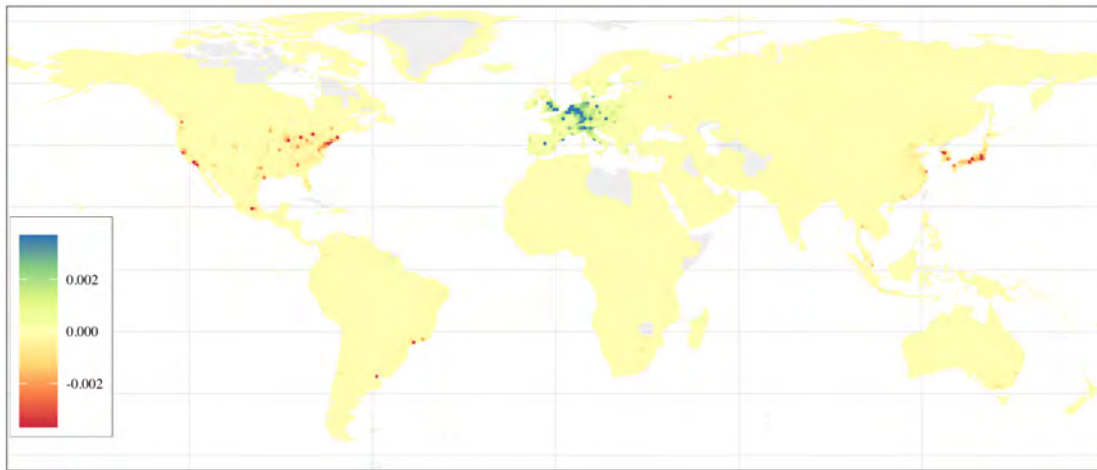
Which pre-existing inefficiencies might a carbon tax with local rebating correct? The world's economic geography is shaped by agglomeration and congestion externalities, and carbon emissions constitute a global externality that affects temperature and welfare. In principle, a carbon tax might reduce the inefficiency

stemming from any of these externalities. As can be seen in Table 2, the effects on global welfare are already present in 2021, when the carbon tax is first introduced. This is before any possible effect on global warming. As such, this points to the carbon tax correcting inefficiencies coming from agglomeration and congestion externalities. By 2100, the welfare effect of the carbon tax is magnified, so that in the long run its impact on global warming might also play a role in reducing certain inefficiencies.

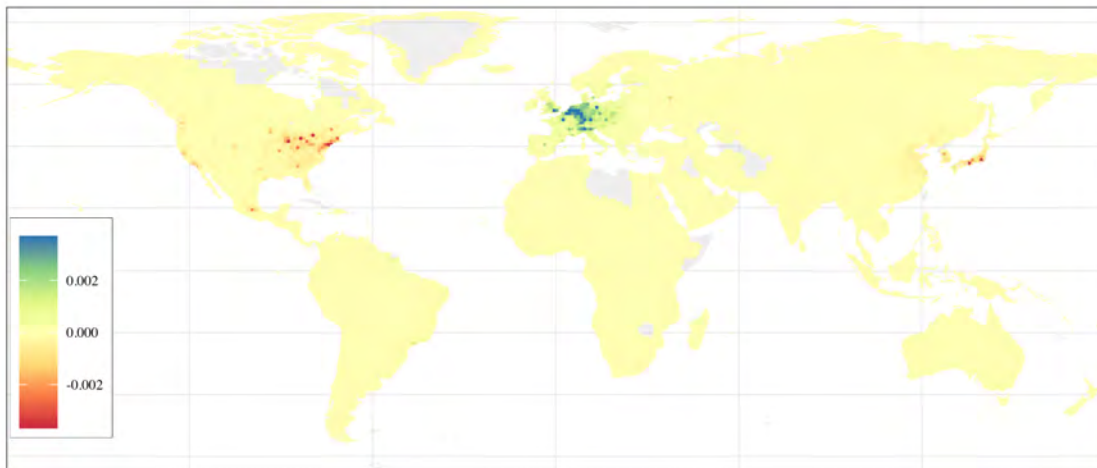
Carbon emissions. Going from no rebating to local rebating does not change EU and global emissions much. With local rebating, EU emissions drop slightly less than in a scenario with no rebating, by around 40% instead of by around 43% in 2021 (Figure 13, Panel (a), and Table 2). This small difference can be understood as a consequence of the EU economy expanding with local rebating. Because the tax revenues from the carbon tax are not lost, the EU attracts more population. By shifting more people into the more productive regions, emissions per unit of output produced drop. When focusing on global emissions, overall emissions drop by around 2.2% with or without rebating.

Figure 13: Effect on Carbon Tax on Emissions around the World (Local vs No Rebating), 2021 and 2100

(a) Δ emissions (local - no rebating), 2021



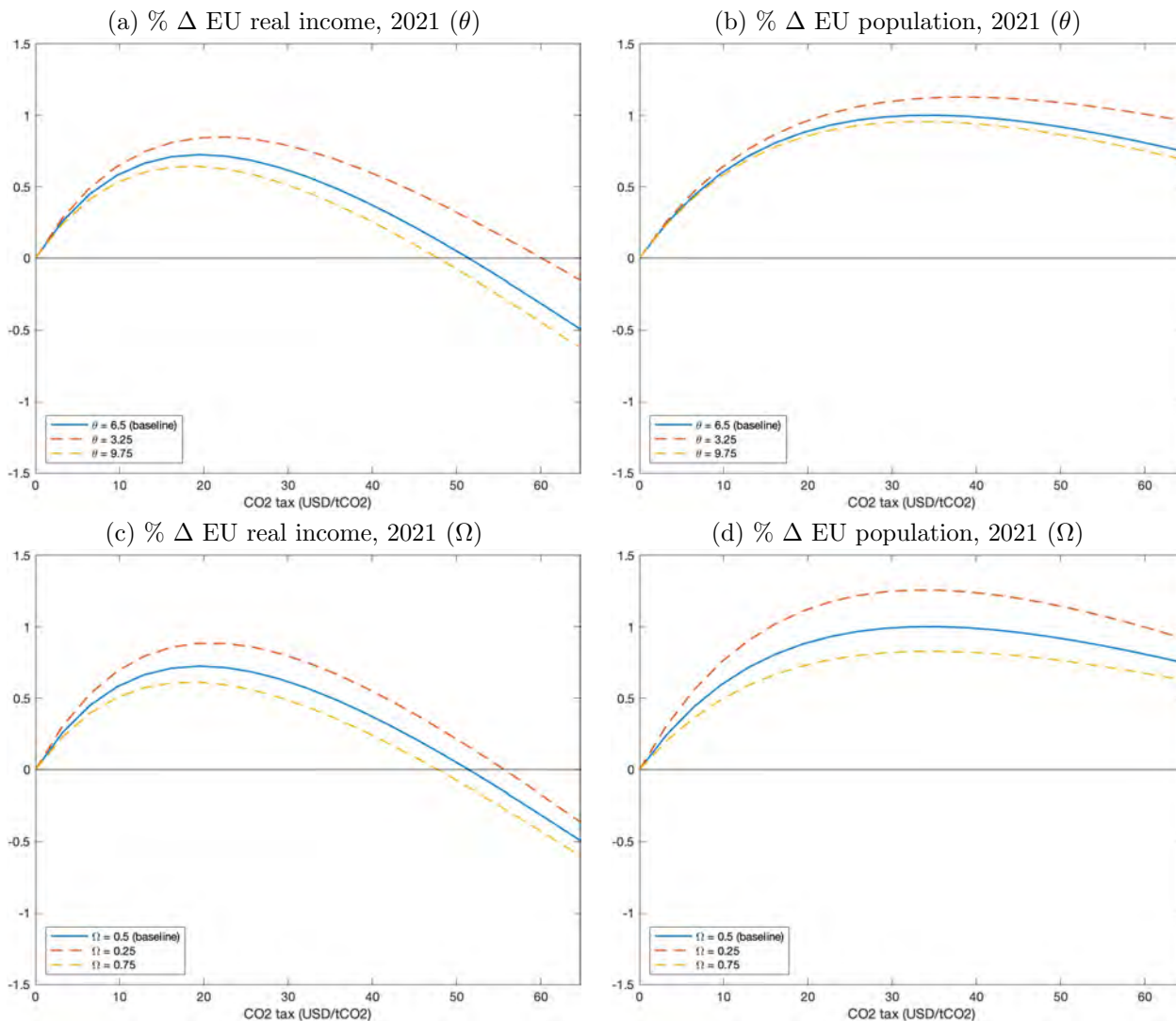
(b) Δ emissions (local - no rebating), 2100



Note: Maps display differences in emission levels (in tCO₂) between the case with a carbon tax (and local rebating) and the case with a carbon tax (and no rebating).

Effect of trade elasticity and preferences heterogeneity. Recall the argument for why a unilateral carbon tax may expand the EU economy. The higher tax burden in non-agriculture is only partly passed on to wages, so once local rebating occurs, income per capita in locations specialized in non-agriculture increases. This attracts migrants to the EU core, and the economy expands. As explained in Section 2.2, the size of this effect depends crucially on the trade elasticity, θ , and on the degree of preference heterogeneity, Ω .

Figure 14: Effect of Different θ and Ω on EU Outcomes with Local Rebating, 2021



Note: Figure displays the effect of EU carbon taxes in the case of local rebating on EU real income and population for different values of θ (Panels a and b) and for different values of Ω (Panels c and d).

If the trade elasticity θ is low, the increase in the relative price of non-agricultural goods due to the carbon tax has a smaller negative effect on local revenue and local income. Because of this, once we add the rebate, the overall positive effect on local income will be greater. As a result, more people will move to the EU core, and the economy of the European Union will expand by more. Hence, for low values of θ we should see a greater expansion of the EU. Figure 14 Panels (a) and (b) show the effects for values of θ

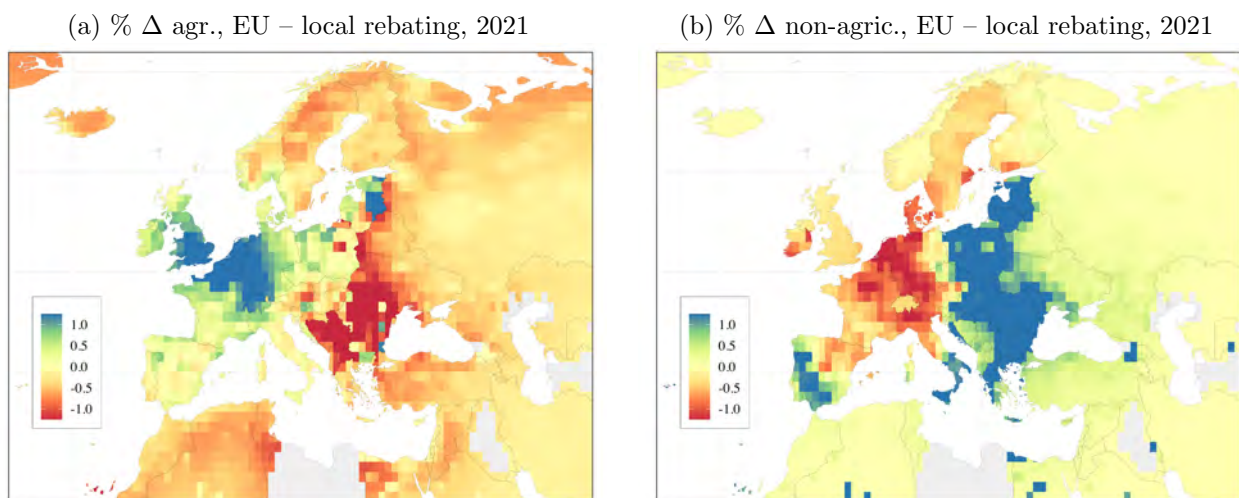
that are 50% higher and 50% lower than the baseline.⁸ Consistent with our argument, we indeed find larger positive effects on EU population and EU real income for smaller values of θ .

If locational preference heterogeneity Ω is low, the elasticity of migration to income differences is large. In that case, the increase in income in the EU core induced by the carbon tax attracts more migrants, both from within the EU and from outside the EU. The concentration of more people in the most productive areas of the EU leads to a larger expansion of EU output. The lower the value of Ω , the greater these effects should be. Figure 14 Panels (c) and (d) plots the effects for both higher (+50%) and lower (-50%) values of Ω . In line with our argument, the EU grows more in terms of population and real income for smaller values of Ω .

5 Alternative Rebating Schemes

In this section we consider two additional rebating schemes: EU rebating, where the EU carbon tax revenue is rebated on a per-capita basis to the whole EU population, and developing countries rebating, where the EU carbon tax is rebated on a per-capita basis to lower-income countries, defined as countries with an income per capita below that of the poorest EU country.

Figure 15: Change in Sectoral Output Due to Carbon Taxes: EU Rebating vs Local Rebating

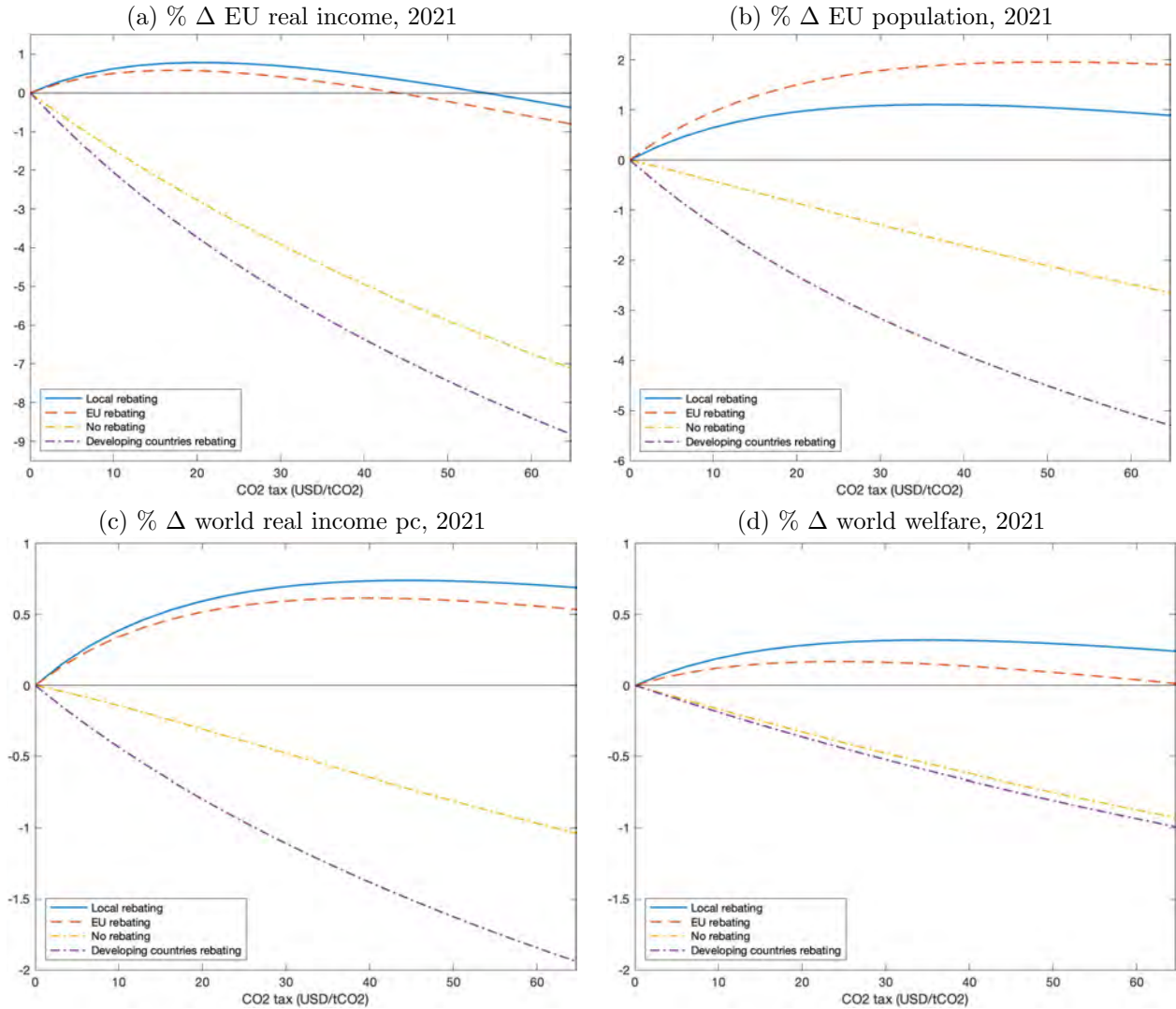


Note: Maps display log difference (*100) in nominal agricultural and non-agricultural output in 2021 between the case with a carbon tax and EU rebating and the case with a carbon tax and no rebating.

Compared to local rebating, EU rebating benefits the EU periphery more and the EU core less. Because the richer non-agricultural core contributes more on a per-capita basis to carbon tax revenues, EU rebating amounts to a transfer from the EU core to the EU periphery. As a result, the positive impact of the carbon tax on the non-agricultural EU core is smaller (Figure 15). Real income in the EU expands less than under local rebating (Figure 16 Panel (a)). World real income per capita and welfare continue to increase, but less so than under local rebating (Panels (c) and (d)).

⁸In this exercise, we are keeping the baseline economy in 2020 unchanged. Taking the alternative parameter value for θ and without recalculating trade and migration costs, we re-invert the model using the data that come out of the baseline simulated model of 2020. As such, our economy in 2020 with the alternative parameter value will be identical to the simulated baseline economy in 2020 in terms of the spatial distribution of total population, total output and agricultural output.

Figure 16: Effect of Different Rebating Schemes on EU and World Economy, 2021

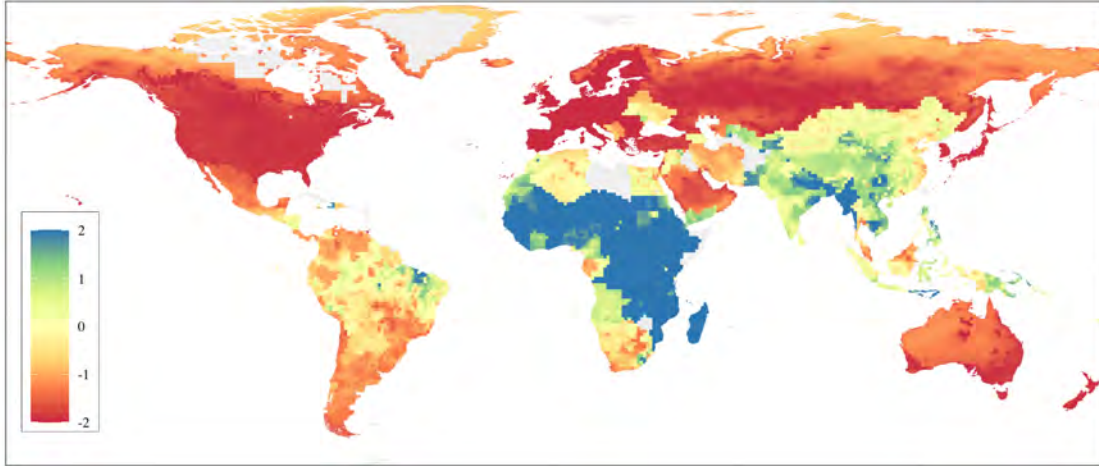


Note: Figure displays the effect of EU carbon taxes under different rebating schemes (no rebating, local rebating, EU rebating, and developing countries rebating) in 2021 on EU real income (Panel a), EU population (Panel b), world real income per capita (Panel c), and world welfare (Panel d).

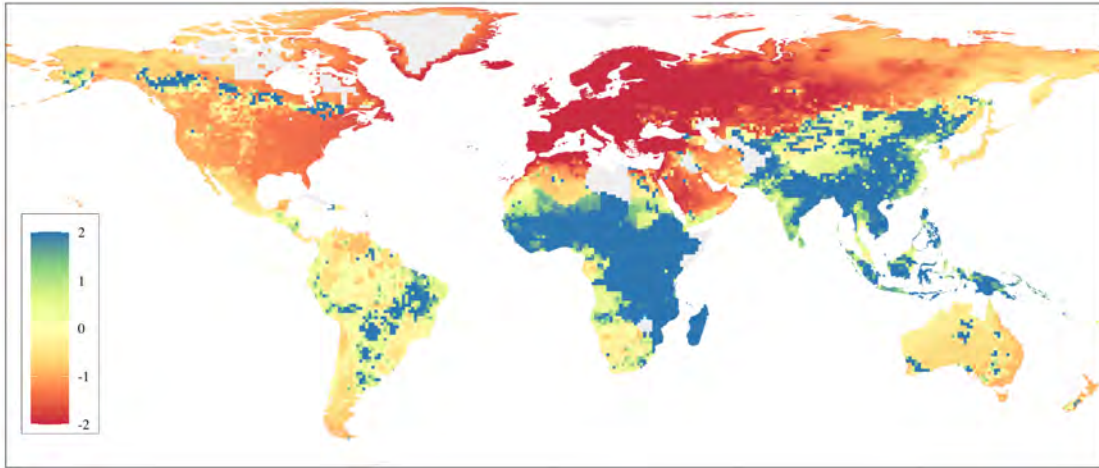
Developing countries rebating, instead, benefits lower-income countries. From the point of view of the EU, the revenue from the carbon tax is lost. It is therefore not surprising that the EU shrinks, both in terms of real income and population (Figure 16, panels (a) and (b)). In fact, the drop in income and population in the EU is greater than when the proceeds of the tax are thrown away. The reason is simple: developing countries rebating keeps more people in low-income regions (Figure 17 Panel (a)). For the baseline carbon tax of 40 US\$/tCO₂, population in sub-Saharan Africa increases by 0.65% in 2021, compared to a drop of 2.17% under no rebating and a drop of 2.5% under local rebating. Slowing down out-migration from Africa and South East Asia also has global efficiency effects. For the baseline carbon tax, developing countries rebating lowers world real income per capita in 2021 by 1.38%, compared to an increase of 0.74% in the case of local rebating (Table 3). Spatial inequality is mitigated though: in 2100 real income per capita is 2.13% lower in the EU and 2.18% higher in sub-Saharan Africa.

Figure 17: Effect of Carbon Tax across the Globe (Developing countries vs Local Rebating)

(a) $\% \Delta$ population, dev. countries – local rebating, 2021



(b) $\% \Delta$ non-agric., dev. countries – local rebating, 2021



Note: Maps display the log difference (*100) in population and nominal non-agricultural output between a carbon tax with developing countries rebating and a carbon tax with local rebating.

When looking at the impact on the carbon stock and temperature, we notice that developing countries rebating reduces emissions and lowers temperature more than other rebating schemes (Figure 18). This is due to developing countries rebating lowering world production more than other rebating arrangements. The effects are still small in magnitude: by 2100 the stock of carbon declines by 2-2.5% compared to a world without carbon taxes, and global temperatures go down by almost 0.1°C. Recall, of course, that we are considering a carbon tax implemented only by the EU. To have larger effects on global temperatures, either the carbon tax would have to be substantially larger, or the carbon tax would have to be implemented by more countries.⁹

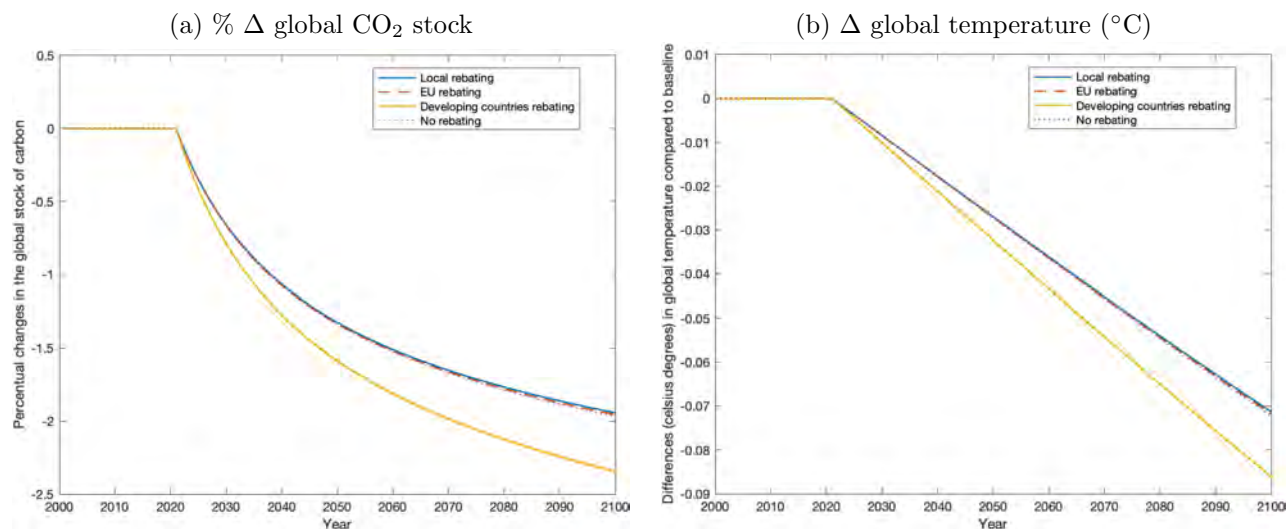
⁹See Cruz and Rossi-Hansberg (2022) for a related finding on the small effect of the unilateral pledges in the Paris Agreement.

Table 3: Effect of Carbon Tax on Different Regions of the World (EU and Developing Countries Rebating)

	World		EU		US		Japan		SSA		Asia	
	2021	2100	2021	2100	2021	2100	2021	2100	2021	2100	2021	2100
<i>Panel A: EU rebating</i>												
%Δ Real GDP	0.62	1.12	0.13	0.87	1.69	2.65	1.49	2.44	-3.49	-6.55	-1.52	-1.86
%Δ Real GDP pc	0.62	1.12	-1.75	-1.49	-0.19	0.1	-0.28	0.03	-0.94	-2.36	-1.12	-1.32
%Δ Welfare	0.14	0.46	-2.51	-2.67	-0.8	-0.69	-0.85	-0.74	-2.39	-3.38	-1.53	-1.9
%Δ Population	0	0	1.92	2.4	1.89	2.55	1.78	2.41	-2.58	-4.3	-0.4	-0.54
%Δ Agricultural Output	1.22	2.62	-2.85	-1.97	2.33	5.47	2.81	6.84	1.01	2.78	2.22	4.05
%Δ Non-agric. Output	1.25	2.65	1.39	2.24	1.34	2.94	0.45	2.35	-0.51	0.09	-0.68	0.49
%Δ Emissions	-2.17	-2.68	-40.63	-38.84	10.62	14.75	9.66	14.1	8.73	11.63	8.77	12.59
<i>Panel B: Developing countries rebating</i>												
%Δ Real GDP	-1.38	-1.85	-6.37	-6.39	0.53	0.97	0.39	0.79	1.44	3.45	1.26	2.29
%Δ Real GDP pc	-1.38	-1.85	-2.59	-2.13	0.55	1.24	0.48	1.19	0.78	2.18	0.82	1.61
%Δ Welfare	-0.67	-0.76	-1.32	-0.76	0.54	1.35	0.5	1.31	0.8	2.09	0.74	1.75
%Δ Population	0	0	-3.88	-4.35	-0.01	-0.26	-0.09	-0.39	0.65	1.25	0.44	0.67
%Δ Agricultural Output	-1.46	-1.12	-1.05	2.32	-0.37	-0.91	0.13	-0.13	-1.56	3.92	-1.24	-0.29
%Δ Non-agric. Output	-1.44	-1.08	-6.28	-5.66	-0.02	0.97	-0.18	0.85	0.9	2.93	0.76	2.41
%Δ Emissions	-2.57	-3.25	-44.14	-42.19	10.95	15.26	10.77	15.12	11.74	17.51	11.56	16.47

Note: For different variables and regions of the world, Table displays log difference (*100) between the baseline with a carbon tax and a counterfactual without a carbon tax. Panel (a) shows results for a carbon tax with EU rebating (where the EU carbon tax revenue is rebated on a per-capita basis to the EU population), and Panel (b) shows results for a carbon tax with developing countries rebating (where the EU carbon tax revenue is rebated on a per-capita basis to developing countries). SSA refers to Sub-saharan Africa, and S. & E. Asia refers to South and East Asia, which includes Bangladesh, Brunei, China, Indonesia, India, Cambodia, Laos, Sri Lanka, Myanmar, Malaysia, Philippines, Thailand, and Vietnam.

Figure 18: Effect of Different Rebating Schemes on Global CO₂ Stock and Temperature



Panel (a) displays change in global CO₂ stock under different rebating schemes, and Panel (b) displays change in global temperature (°C) under different rebating schemes.

6 Conclusion

Unilateral carbon policy has an effect on the spatial distribution of economic activity and its efficiency. Understanding this impact can help design better carbon policy and minimize, and even revert, the short run negative local effects of the policy. This paper uses a dynamic spatial integrated assessment model (S-IAM) to evaluate the economic effects of a unilateral carbon tax implemented by the European Union. With local rebating, we find that such a carbon tax would expand the size of the European Union economy and improve global welfare. Local rebating of the tax acts as a place-based policy that subsidizes the EU's non-agricultural core, and as a migration policy that incentivizes people to move to Europe. With a greater share of the world population residing in the developed world, global efficiency and global welfare improve. Alternative rebating schemes lead to different results. In particular, rebating the revenues of the EU carbon tax to developing countries improves the lot of lower-income countries. This slows down migration to the EU, leading to a less efficient spatial distribution of population and economic activity. As a result, global welfare declines. Our analysis underscores the importance of taking into account the spatial effects of carbon taxes. Because the initial spatial equilibrium need not be efficient, carbon taxes have the potential of improving efficiency, though this depends on how tax revenues are rebated, as well as on their size.

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A Appendix: Additional Tables

Table A1: Parameter Values

Parameter	Target/Comment
1. Preferences	
$\beta = 0.96$	Annual discount factor
$\rho = 0.75$	Elasticity of substitution of 4 ¹
$\lambda = 0.32$	Relation between amenities and population ¹
$\Omega = 0.5$	Elasticity of migration flows with respect to income ¹
$\psi = 1.8$	Subjective well-being parameter ¹
$\chi_A = 0.051$	Data on agricultural and total output
$\chi_M = 0.949$	Data on agricultural and total output
2. Technology	
$\alpha_A = 0$	No agglomeration externality in agriculture
$\alpha_M = 0.01$	Agglomeration externality in non-agriculture ¹
$\theta = 6.5$	Trade elasticity ¹
$\mu_A = \mu_M = 0.6$	Labor share in agriculture and non-agriculture ²
$\gamma_A = 0.001$	Growth rate of agricultural productivity ³
$\gamma_M = 0.0002$	Growth rate of non-agricultural productivity ³
$\sigma_A = 0.04$	Energy share in agriculture (Schnepf, 2004; Australian Bureau of Statistics, 2021)
$\sigma_M = 0.07$	Energy share in non-agriculture (Grubb et al., 2018; King et al., 2015)
$\delta = 0.993$	Technology diffusion ¹
$\aleph = 0.004$	Spatial decay of diffusion ⁴
$\phi = 0.25$	Energy supply elasticity ²
3. Temperature and carbon cycle	
$g_A^{opt} = 19.9^\circ\text{C}$	Optimal temperature in agriculture ²
$g_A^{var} = 7.28^\circ\text{C}$	0.1% of world agricultural production at locations below discount factor 0.01
$g_M^{opt} = 10.5^\circ\text{C}$	Relationship between non-agricultural productivity and temperature
$g_M^{var} = 11.0^\circ\text{C}$	Relationship between non-agricultural productivity and temperature
$\varepsilon_1 = 0.9975$	Decay of carbon stock ²
$\varepsilon_2 = 0.29$	1200 GTC increase in global carbon stock by 2100
$\nu = 0.0031$	3.7°C increase in global temperature by 2100

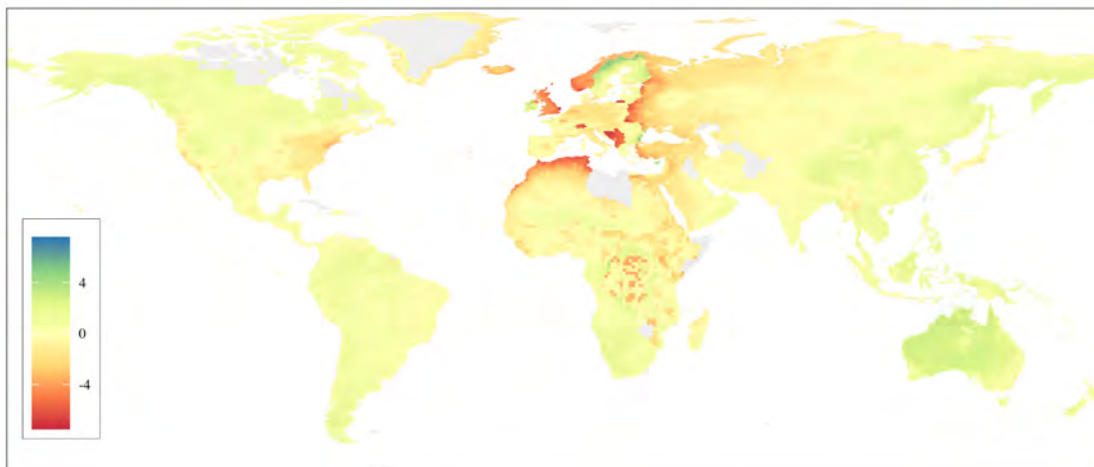
¹Desmet et al. (2018), ²Desmet and Rossi-Hansberg (2015), ³Duarte and Restuccia (2010), ⁴Comin et al. (2012). Note that α_M in the current paper is equal to α_M divided by θ in Desmet et al. (2018).

B Appendix: Additional Figures and Robustness

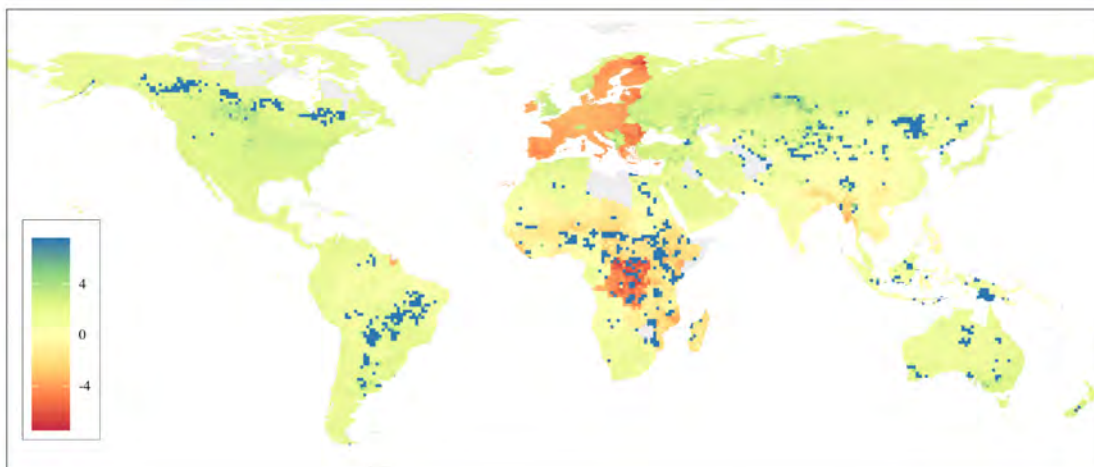
B.1 Additional Figures

Figure B1: Effect of Carbon Tax on Sectoral Output (No Rebating), 2021

(a) Agricultural output, no rebating, 2021



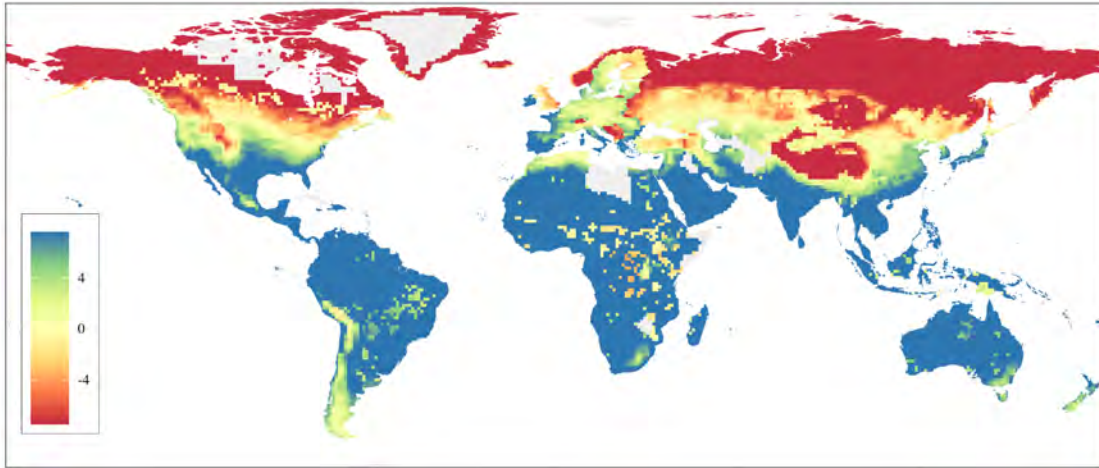
(b) Non-agricultural output, no rebating, 2021



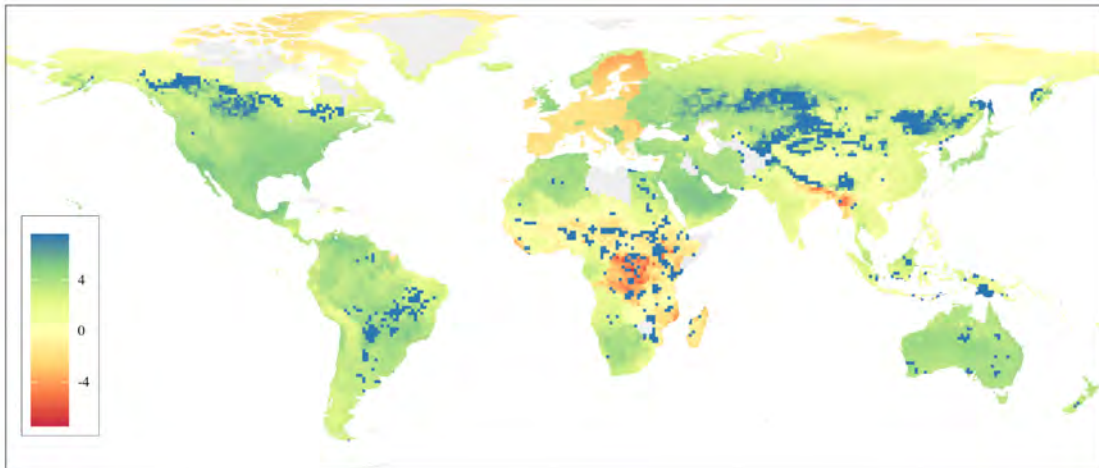
Note: Maps display log differences in nominal sectoral output in agriculture (Panel a) and non-agriculture (Panel b) in 2021 between the case with a carbon tax (and no rebating) and the case without a carbon tax.

Figure B2: Effect of Carbon Tax on Sectoral Output (No Rebating), 2100

(a) Agricultural output, no rebating, 2100



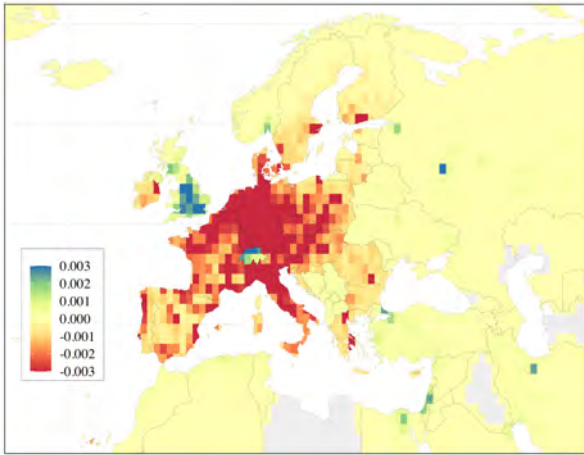
(b) Non-agricultural output, no rebating, 2100



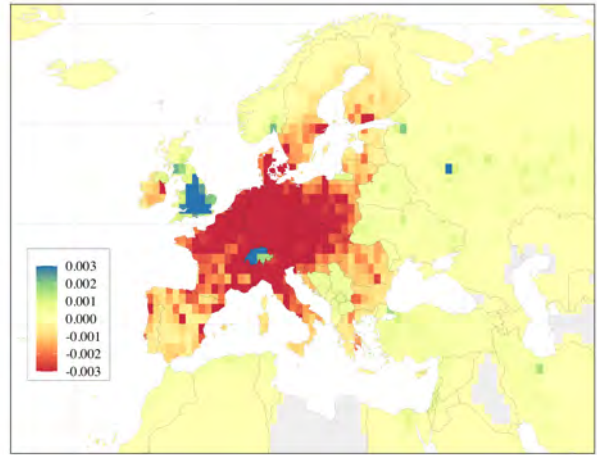
Note: Maps display log differences in nominal sectoral output in agriculture (Panel a) and non-agriculture (Panel b) in 2100 between the case with a carbon tax (and no rebating) and the case without a carbon tax.

Figure B3: Change in Emissions in the EU Due to Carbon Tax (No Rebating)

(a) Difference in emissions (tCO₂), 2021



(b) Difference in emissions (tCO₂), 2100

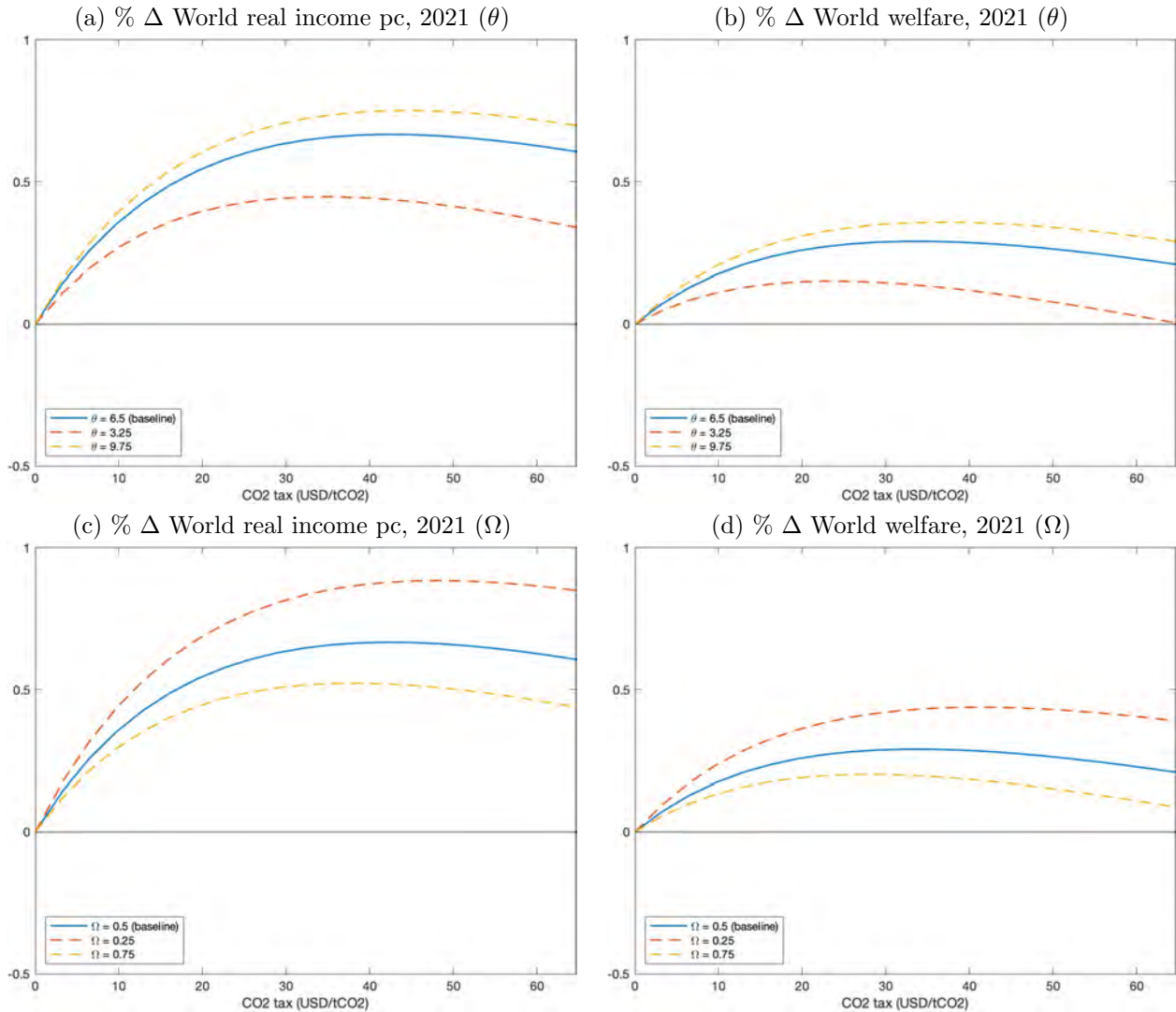


Note: Maps display differences in emissions levels (tCO₂) between the case with a carbon tax (and no rebating) and the case without a carbon tax.

B.2 Robustness

In this subsection we show that the positive effect of an EU carbon tax on global efficiency and global welfare is robust to changes in the trade elasticity (θ) and the degree of locational preference heterogeneity (Ω). Figure B4 shows these results for both higher (+50%) and lower (-50%) values of θ and Ω . For any of these values, an EU carbon tax of 40 US\$/tCO₂ induces improvements in both global real income per capita and global welfare. This, once again, reflects the EU carbon tax generating a more efficient distribution of economic activity across the globe.

Figure B4: Effect of Different θ and Ω on World Outcomes with Local Rebating, 2021



Note: Figure displays the effect of EU carbon taxes in the case of local rebating on world's real income per capita and welfare for different values of θ (Panels a and b) and for different values of Ω (Panels c and d).

C Appendix: Solving the Model

The solution method of the model follows closely [Conte et al. \(2021\)](#). In particular, the algorithm to solve for the equilibrium in each period t consists of a 3-level loop that solves for the distribution of the following 4 endogenous variables: $\bar{L}_t(r)$, e_t , $\bar{L}_{At}(r)$, and $w_t(r)$. Ultimately, the first 3 become explicit (but complex), functions of $w_t(r)$, which is the actual endogenous variable that solves for the period- t equilibrium. The nesting structure works as follows:

- **Outer loop:** solves for $\bar{L}_t(r)$ and e_t .
- **Middle loop:** solves for $\bar{L}_{At}(r)$.
- **Inner loop:** solves for $w_t(r)$ combining sectoral market clearing conditions:

$$w_t(r)^{1+\theta} = \int_S f(\mathbf{w}_t, \cdot) y_t(s) ds \quad \forall r. \quad (17)$$

For the inner loop, we proceed as in [Conte et al. \(2021\)](#) and retrieve $y_t(s)$ as an explicit function of $w_t(s)$ only. That allows us to iterate over (17) and solve for the distribution of wages. The main difference between [Conte et al. \(2021\)](#) and our method is that, when doing so, we also retrieve carbon tax revenues as an explicit function of nominal wages. We achieve this by substituting the carbon tax revenues in equation (12) into the nominal income in equation (3). As an illustration, in the case of local rebating, that becomes

$$\begin{aligned} y_t(s) &= \overbrace{w_t(r) \bar{L}_t(s) + (\Pi_t/\bar{L}) \bar{L}_t(s) + R_t(s) H(s) + b_t(s) \bar{L}_t(s)}^{\equiv g(\mathbf{w}_t, \cdot)} \\ &= g(\mathbf{w}_t, \cdot) + \sum_{i=1}^I \Upsilon_t(s) e_t \frac{\sigma_i}{\gamma_i + \mu_i} \frac{w_t(s)}{(1 + \Upsilon_t(s)) e_t} \bar{L}_{it}(s). \end{aligned} \quad (18)$$

Note the equivalence of all but the last elements of the right hand side with the function $(g(\mathbf{w}_t, \cdot))$ in [Conte et al. \(2021\)](#). Then, with the guesses for sectoral employments $L_{it}(r)$ and energy prices e_t , it is possible to iterate on (17) and retrieve the equilibrium distribution of wages.

We then proceed with the middle loop by plugging the solution for wages from the inner loop into the sectoral market clearing conditions. This yields sectoral employment levels, $\bar{L}_{At}(r)$, using an analogous iterative procedure. Finally, the outer loop uses the previous results together with migrations shares and energy market clearing conditions to obtain an update for the population distribution and energy prices, $\bar{L}_t(r)$ and e_t . We iterate this 3-level procedure until all conditions hold simultaneously.