

Rydberg atoms in optical tweezers

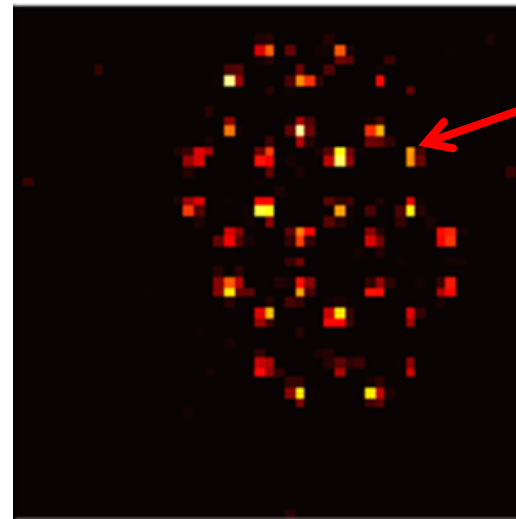
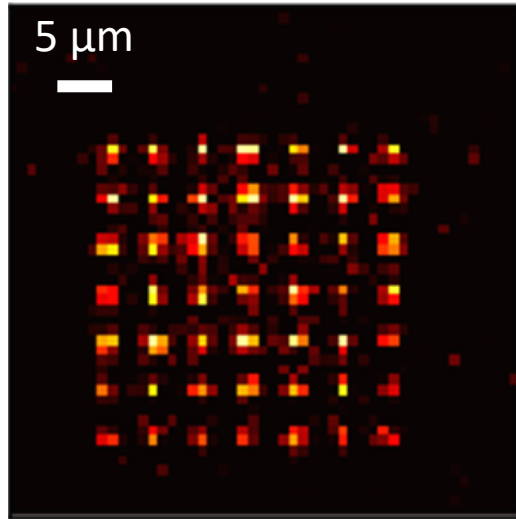
Lecture 1: Dipolar interactions between atoms

Lecture 2: Arrays of atoms. Basics of Rydberg physics.
Rydberg blockade

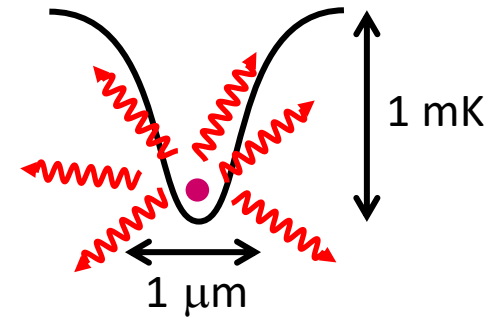
Lecture 3: Many-body physics with Rydberg atoms:
spin models and transport

[Review](#): A. Browaeys, T. Lahaye, Nature Physics **16**, 132 (2020)

Recap lecture 2: tweezer, arrays & Rydberg

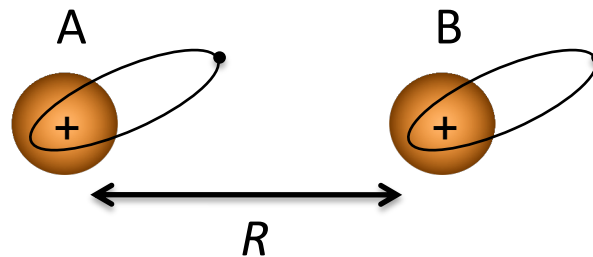


1 Rb atom
(fluorescence)



Grangier (2001)
Sortais (2007)

Rydberg interactions



Van der Waals

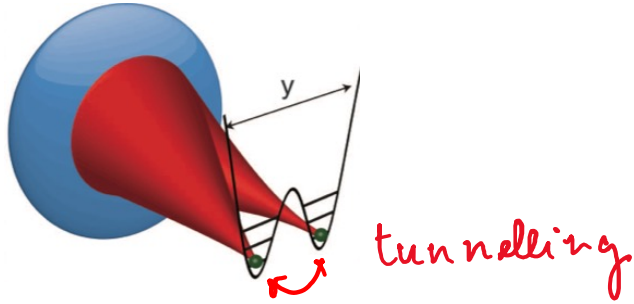
$$\frac{C_6}{R^6}$$

resonant

$$\frac{C_3}{R^3}$$

Tweezers and tweezer arrays: what for?

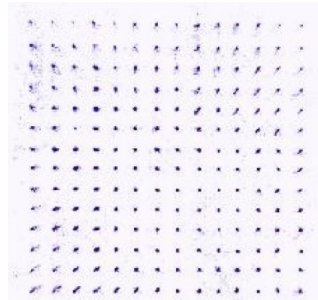
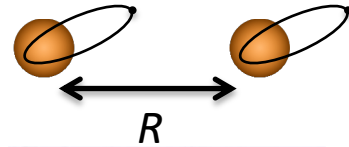
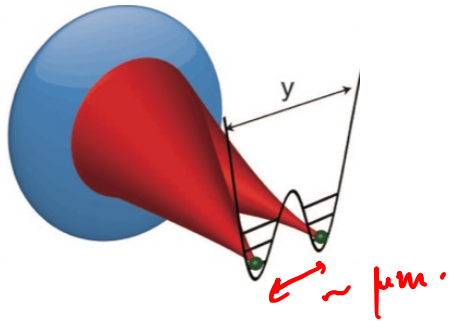
Quantum simulation



Regal, Kaufman, Thomson...

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Quantum simulation

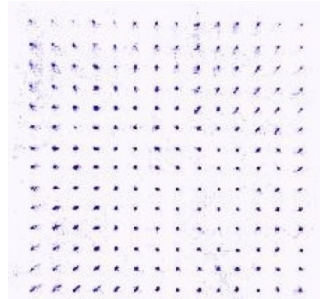
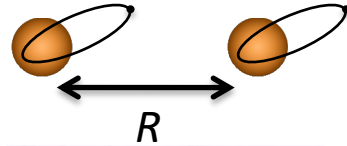
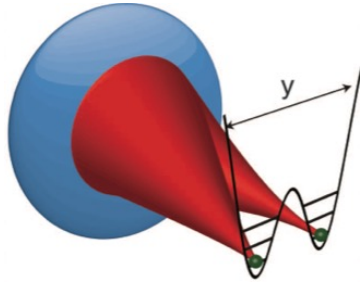


$\sim 5-10 \mu\text{m}$

Regal, Kaufman, Thomson...

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Regal, Kaufman, Thomson...

Optical clocks

PHYSICAL REVIEW X 9, 041052 (2019)

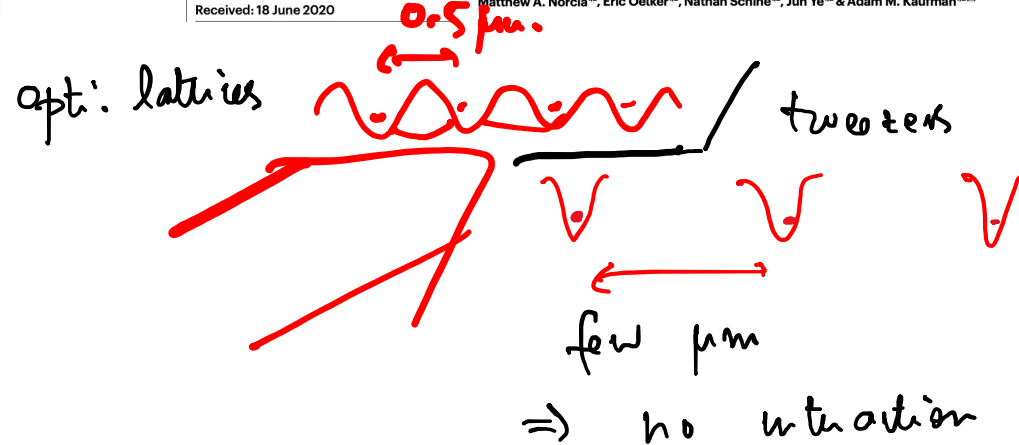
Featured in Physics

An Atomic-Array Optical Clock with Single-Atom Readout

Ivaylo S. Madjarov,¹ Alexandre Cooper,¹ Adam L. Shaw,¹ Jacob P. Covey,¹ Vladimir Schkolnik,² Tai Hyun Yoon,^{1,†} Jason R. Williams,² and Manuel Endres^{1,*}

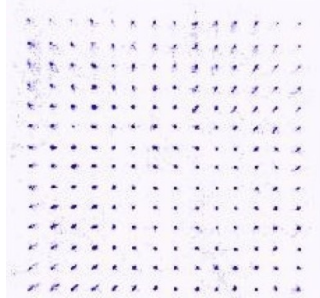
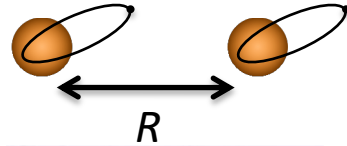
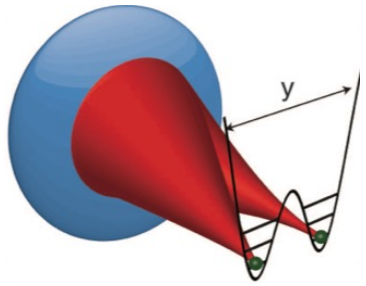
Half-minute-scale atomic coherence and high relative stability in a tweezer clock

<https://doi.org/10.1038/s41586-020-3009-y> Aaron W. Young^{1,2}, William J. Eckner^{1,2}, William R. Milner^{1,2}, Dhruv Kedar^{1,2}, Matthew A. Norcia^{1,2}, Eric Oelker^{1,2}, Nathan Schine^{1,2}, Jun Ye^{1,2} & Adam M. Kaufman^{1,2,§}
Received: 18 June 2020



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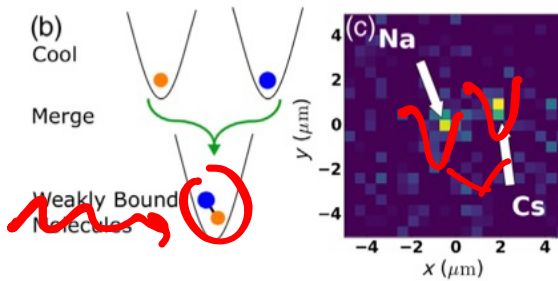
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Molecule engineering



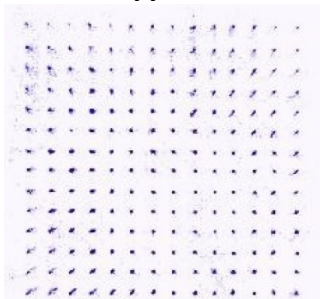
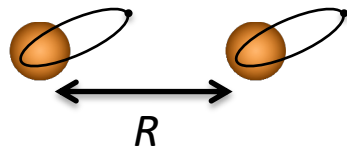
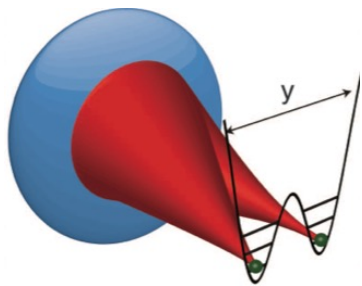
CaF



Ni, Doyle...

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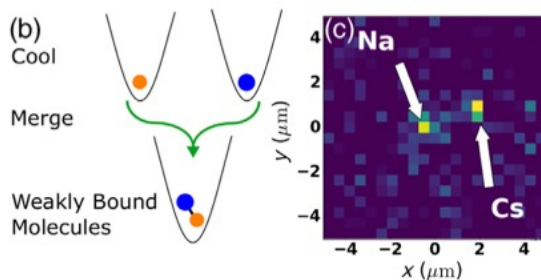
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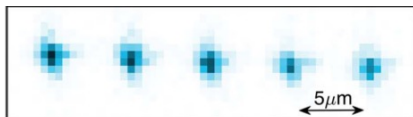
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Regal, Kaufman, Thomson...

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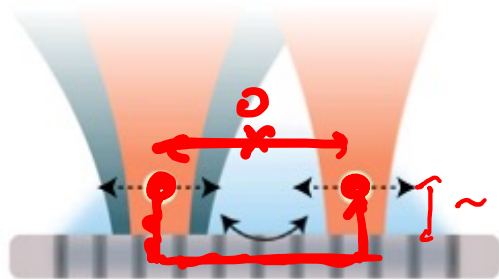


CaF



Ni, Doyle...

Tool for cQED

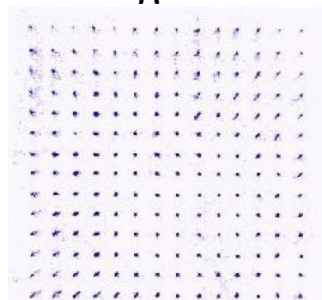
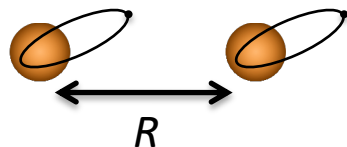
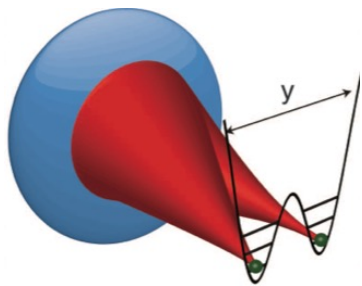


$\sim 120 - 500 \text{ nm}$
2 waveguide.

Lukin

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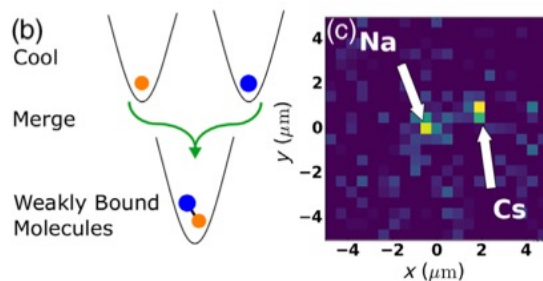
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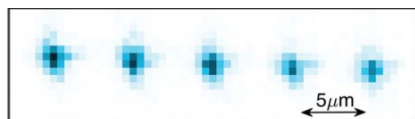
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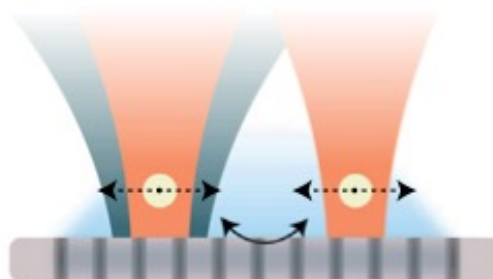


CaF



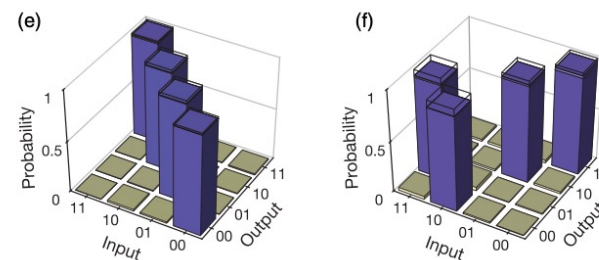
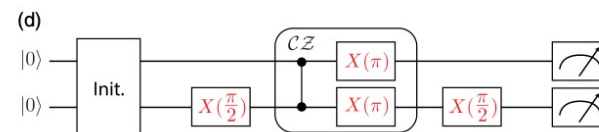
Ni, Doyle...

Tool for cQED



Lukin

Quantum gates



Saffman, Lukin...

Outline

1. Quantum simulation and spin models
2. Simulation of the quantum Ising model using van der Waals interactions: quantum magnetism
3. Topological systems using resonant dipole interactions

Many-body physics with synthetic matter

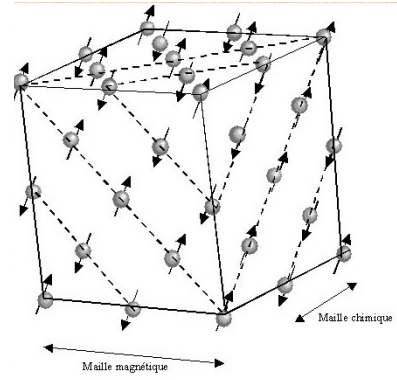
Goal: Understand ensembles of **interacting quantum particles**



superfluidity



superconductivity



magnetism



neutron star

Open questions: Phase diagram, **dynamics** (hard for $N > 40 \dots$)

Topology, disorder, entanglement,...

$\uparrow -$
 $\downarrow -$
 $\dim \Sigma = 2^N$
Record obiviti'o : $N \sim 46$ atoms
Spis.

Many-body physics with synthetic matter

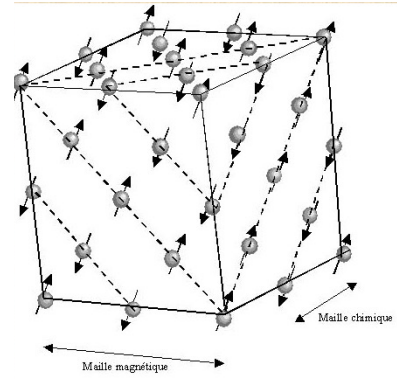
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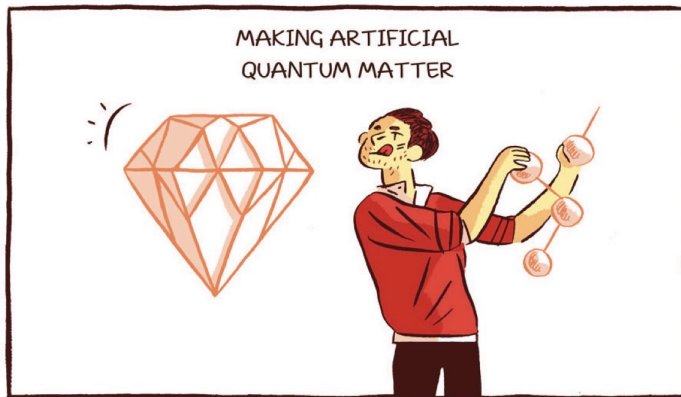
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Use experimental control to

Implement **many-body Hamiltonians**
(including “mathematical” ones...)

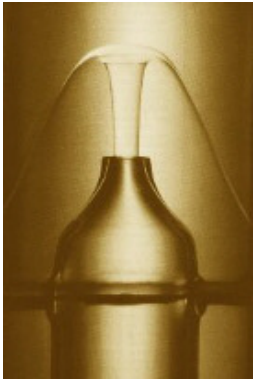
Larger **tunability** than « real » systems



R.P. Feynman

Many-body physics with synthetic matter

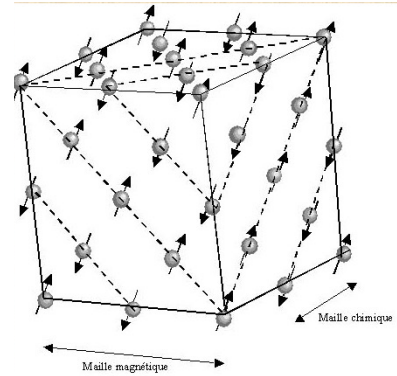
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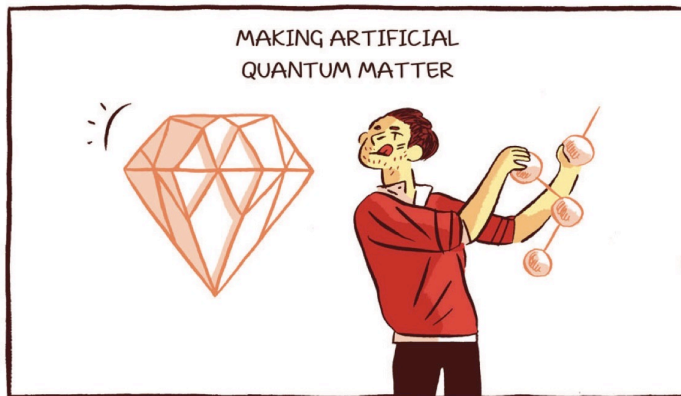
magnetism



neutron star

Open questions: Phase diagram, **dynamics** (hard for $N > 40 \dots$)

Topology, disorder, entanglement,...



R.P. Feynman

1982

Use experimental control to

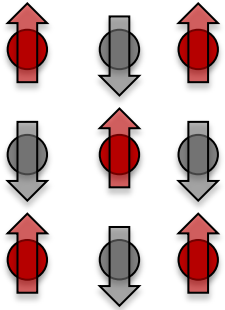
Implement **many-body Hamiltonians**
(including “mathematical” ones...)

Larger **tunability** than « real » systems

= QUANTUM SIMULATION

Spin models: one of the “simplest” many-body problem

Interacting spin $\frac{1}{2}$ particles on a lattice:



$$\hat{H}_{ij} = J_{ij} \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_j$$

$$\hat{S} = \frac{\hbar}{2} \boldsymbol{\sigma}$$

$$\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}_{\uparrow, \downarrow}$$

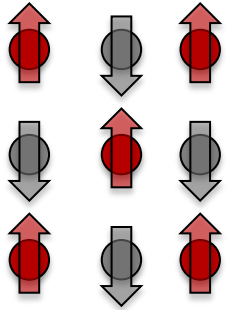
$$\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \quad \sigma_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$$

$$\sigma_+ = |\uparrow\rangle\langle\downarrow| \quad \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix}$$

$$\sigma_- = (\sigma_+)^{\dagger}$$

Spin models: one of the "simplest" many-body problem

Interacting spin 1/2 particles on a lattice:



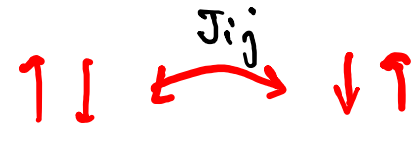
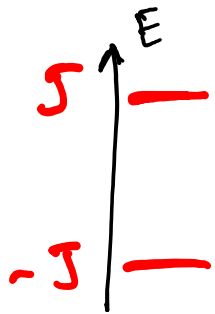
$$\hat{H}_{ij} = J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

Ising

$$\hat{H} = \sum_{i \neq j} J_{ij} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)}$$

XY model

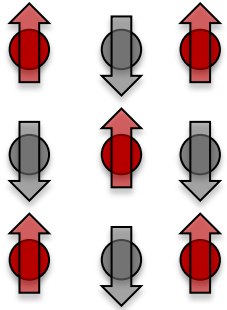
$$\hat{H} = \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+)$$



"Flip-Flop."

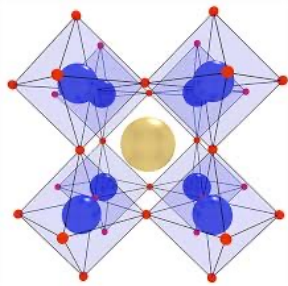
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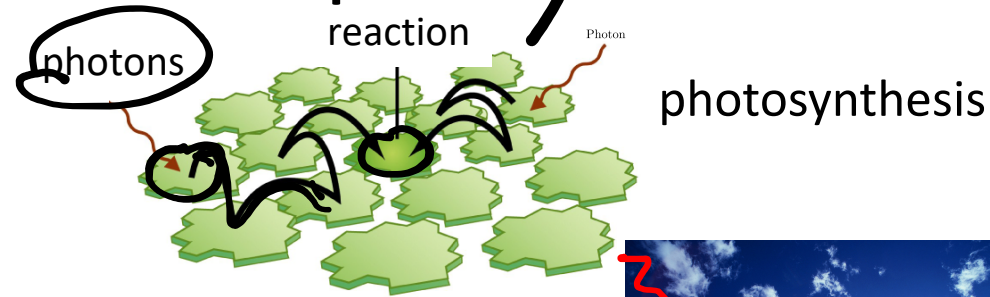
Magnetism



Ising $\hat{H} = \sum_{i \neq j} J_{ij} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)}$

XY model $\hat{H} = \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+)$

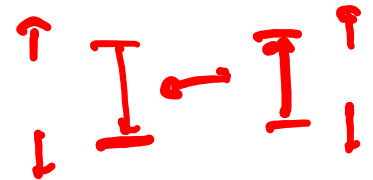
Transport of excitations



Light scattering
(dissipative)

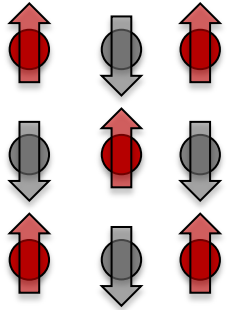


$J_{ij} \in \mathbb{C}$
dissipative



Spin models: one of the “simplest” many-body problem

Interacting spin ½ particles on a lattice:

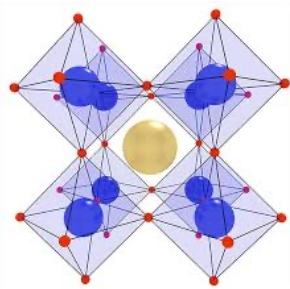


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Ising $\hat{H} = \sum_{i \neq j} J_{ij} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)}$

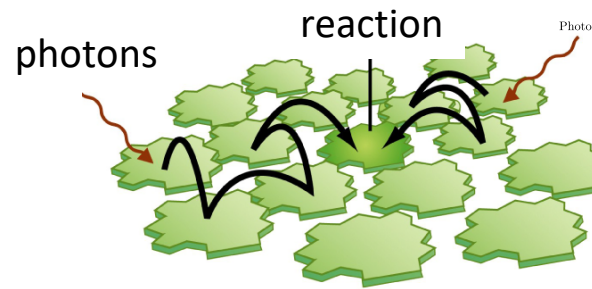
XY model $\hat{H} = \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+)$
 $(\hat{\sigma}_x \hat{\sigma}_x + \hat{\sigma}_y \hat{\sigma}_y)$

Magnetism



Perovskite
 $Y_2Ti_2O_7$

Transport of excitations



photosynthesis

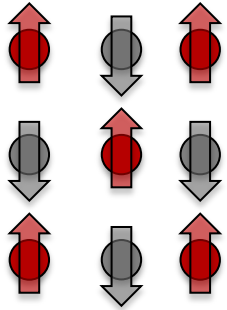
Light scattering
(dissipative)



Open questions: **Dynamics** (hard for $N > 30$, long range...)
 Entanglement, disorder, **topology**...
Geometry (frustration: spin liquids?) ...

Spin models: one of the “simplest” many-body problem

Interacting spin ½ particles on a lattice:

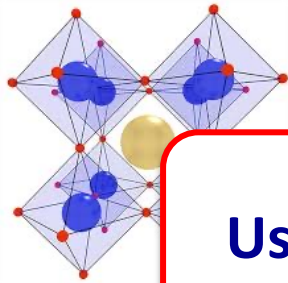


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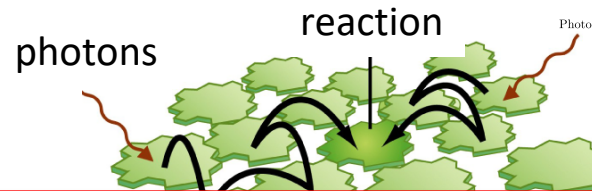
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XY model $\hat{H} = \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+)$

Magnetism



Transport of excitations



photosynthesis

Use control over artificial quantum matter

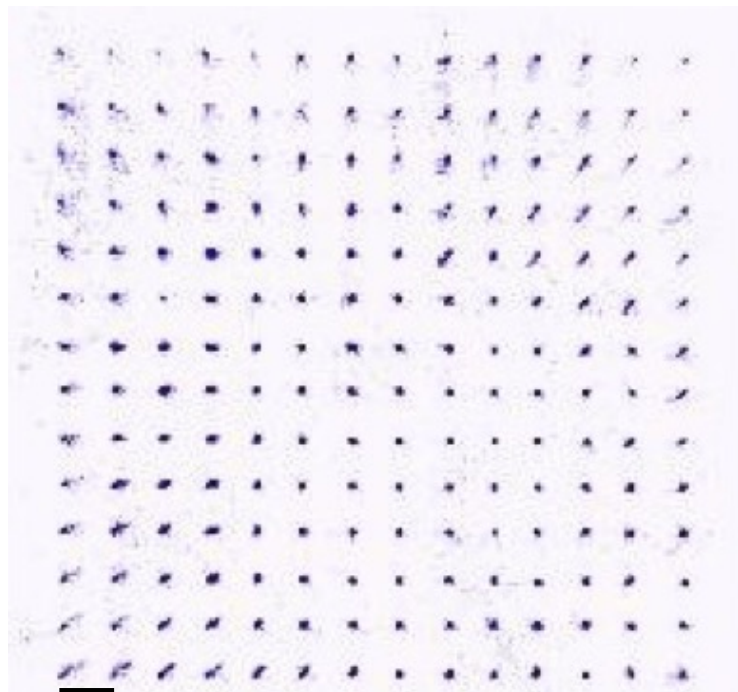
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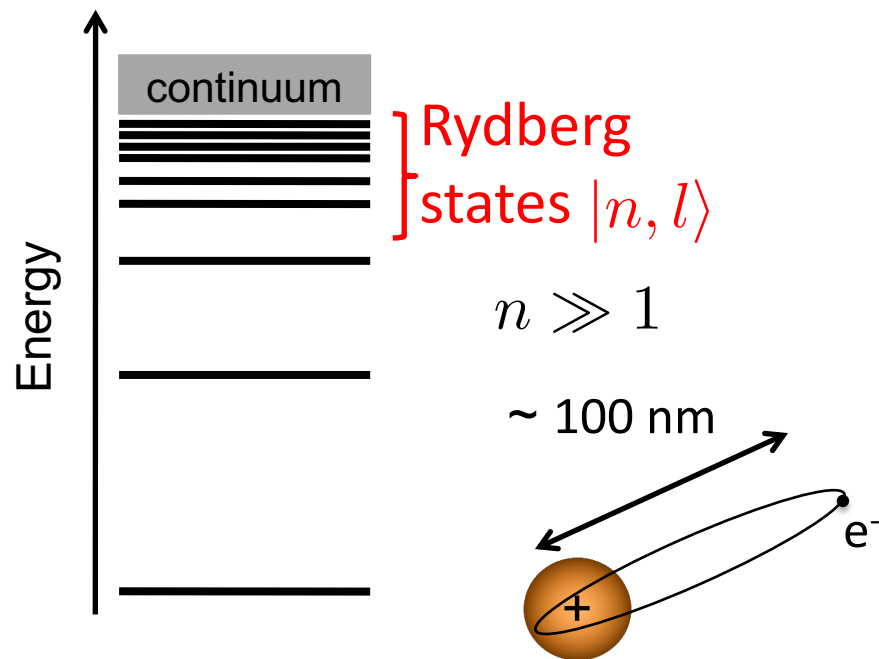
Our platform: arrays of interacting Rydberg atoms

Individual atoms in assembled
arrays of tweezers (~ 200 at.)



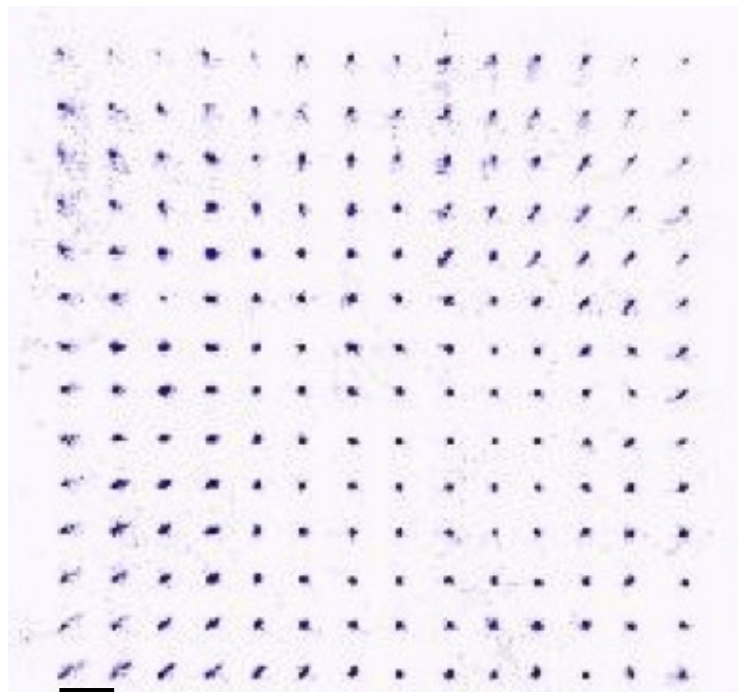
5 μm

Rydberg atoms



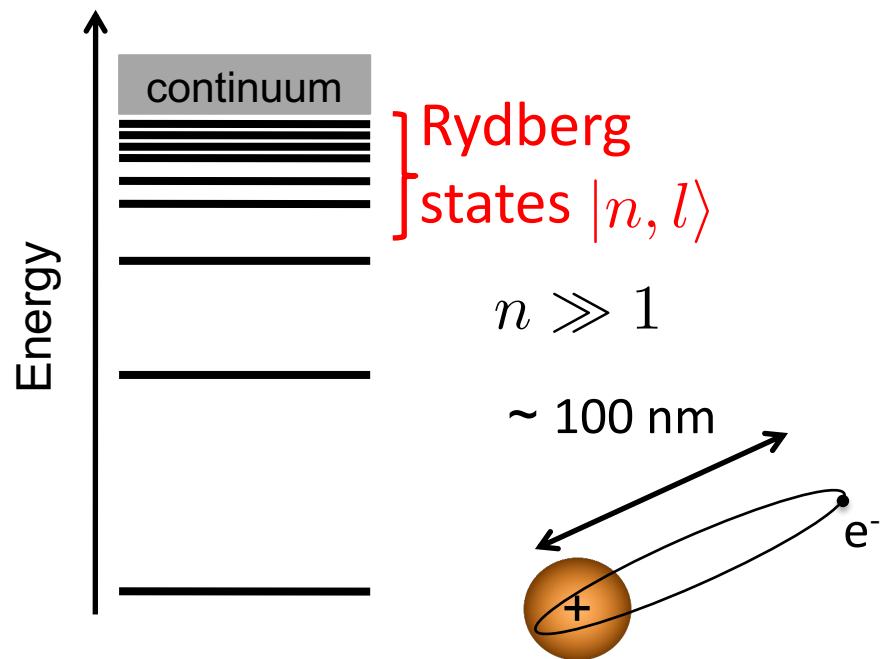
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5 μm

Rydberg atoms

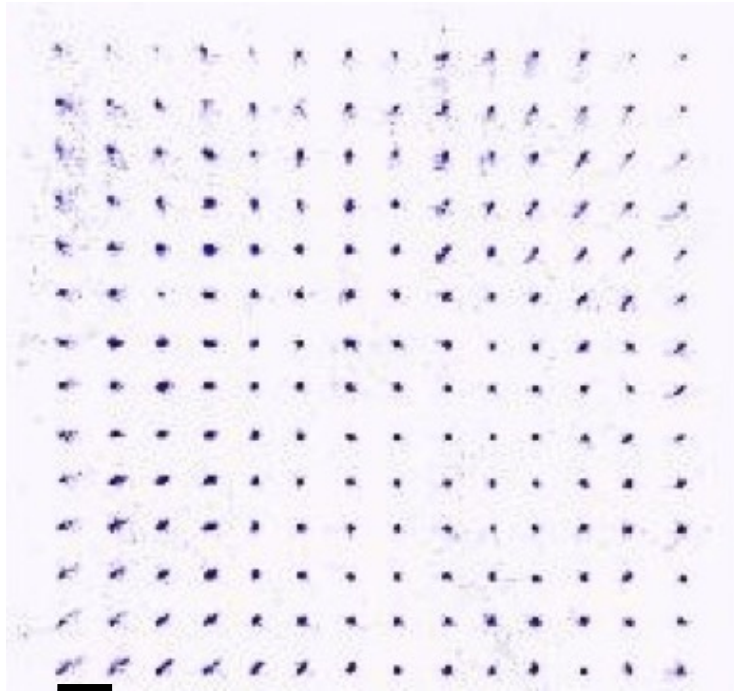


Lifetime $> \underline{100 \mu\text{s}}$

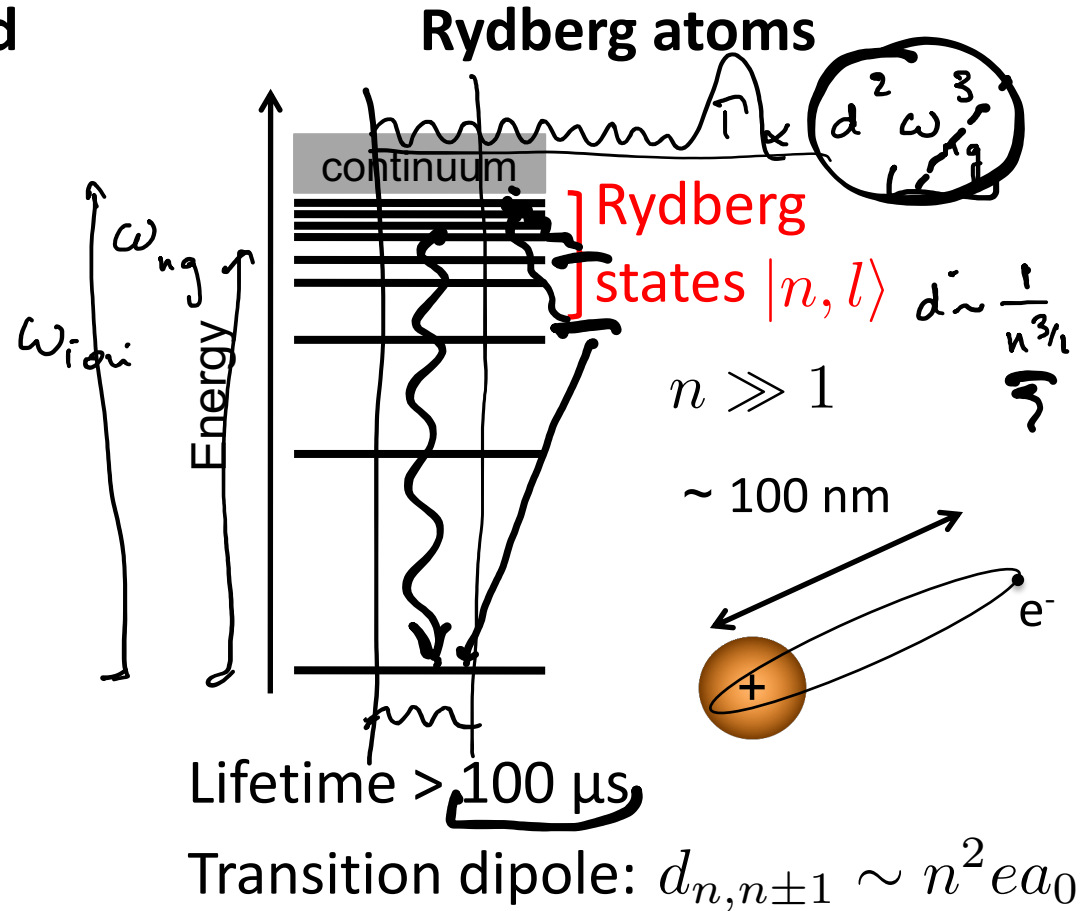
Transition dipole: $d_{n,n\pm 1} \sim n^2 ea_0$

Our platform: arrays of interacting Rydberg atoms

Individual atoms in assembled arrays of tweezers (~200 at.)



5 μm



\Rightarrow Large dipole-dipole interactions

$$n \sim 60, R = 10 \mu\text{m} \Rightarrow V_{\text{int}}/h \sim 1 - 10 \text{ MHz}$$

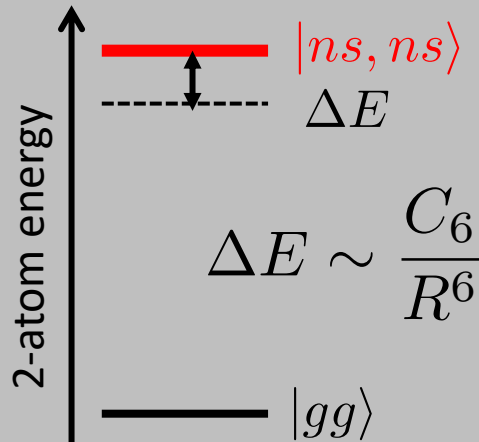
\Rightarrow timescales $< \mu\text{sec}$

Interactions between Rydberg atoms and spin models

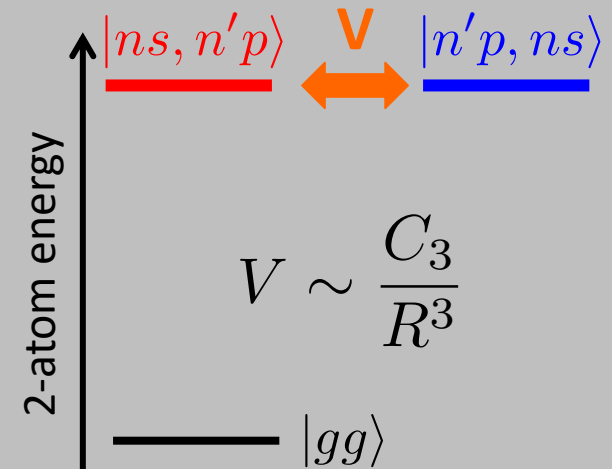


Browaeys & Lahaye, Nat.Phys. (2020)

van der Waals



Resonant dipole



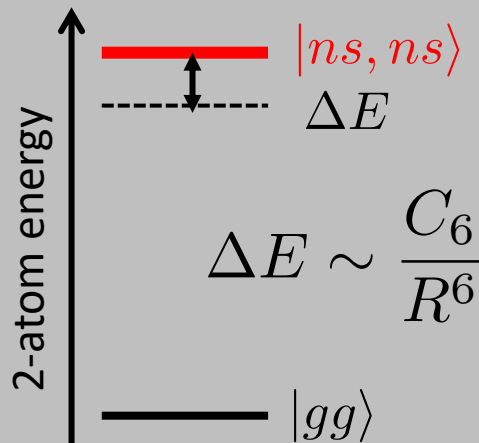
$C_6, C_3 \sim \left(d_{nn\pm 1}^2 \right)$
 $\Gamma_{nn\pm 1} \sim d^2$

Interactions between Rydberg atoms and spin models

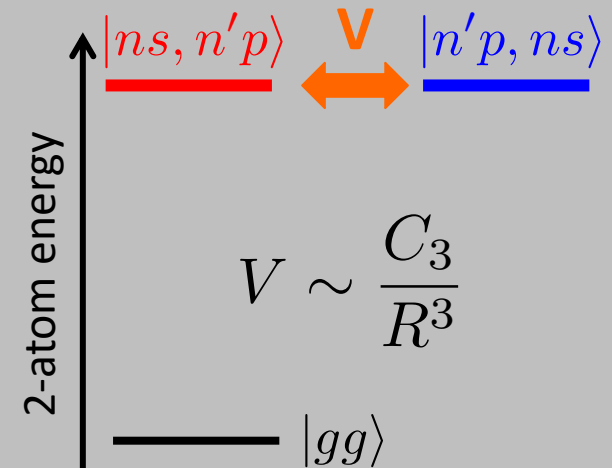


Browaeys & Lahaye, Nat.Phys. (2020)

van der Waals



Resonant dipole



Quantum Ising

$$\hat{H} = \sum_{i \neq j} J_{ij} \hat{\sigma}_z^{(i)} \hat{\sigma}_z^{(j)}$$

XY model

$$\hat{H} = \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+)$$

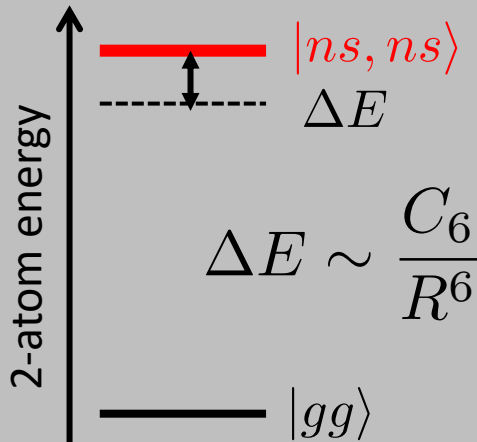
Outline

1. Quantum simulation and spin models
2. Simulation of the quantum Ising model using van der Waals interactions: quantum magnetism
3. Topological systems using resonant dipole interactions

From van der Waals interactions to Ising model...



van der Waals



$$\Delta E \sim \frac{C_6}{R^6}$$

$$C_6 \propto n^{11} \Rightarrow \text{switchable interaction}$$

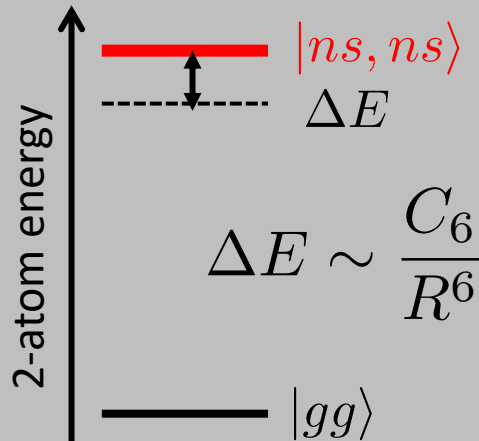
$ns\ n's$

$n = 5$ groundstate \rightarrow $n = 50$
 $C_6 \propto 10^{11}$

From van der Waals interactions to Ising model...



van der Waals



$C_6 \propto n^{11} \Rightarrow$ switchable interaction

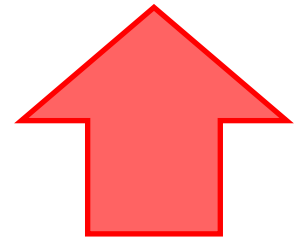
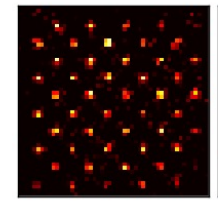
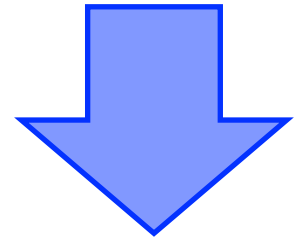
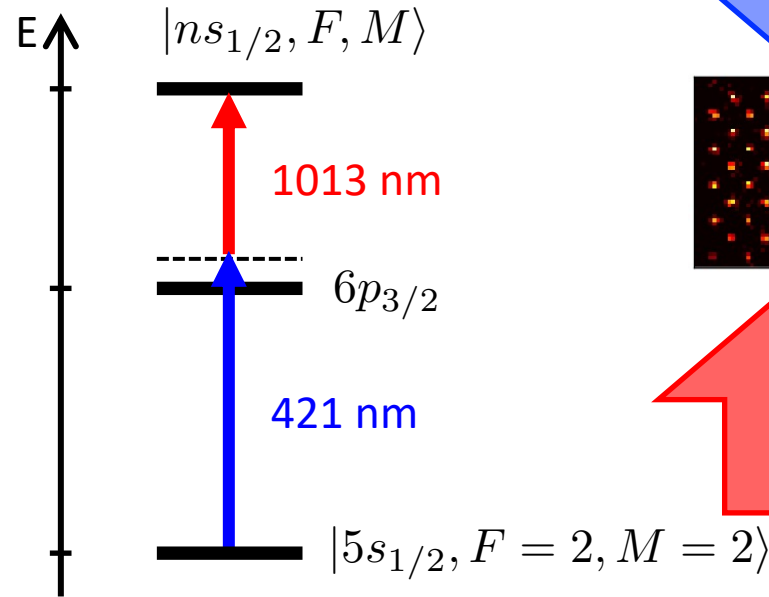
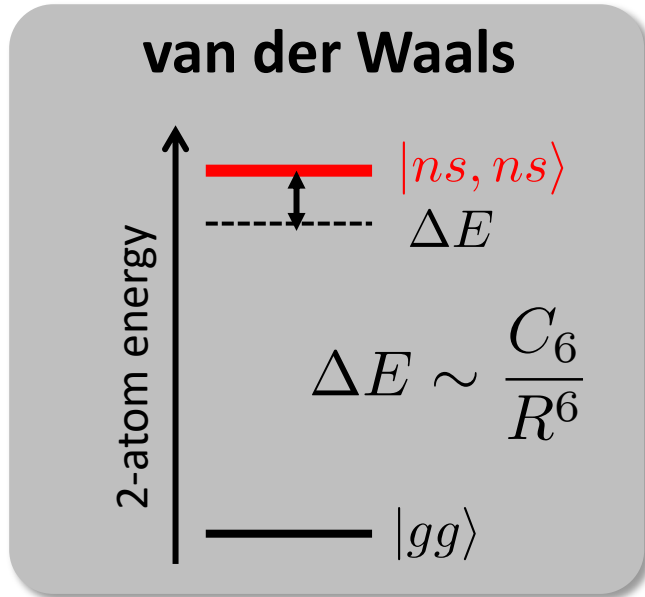
$$\hat{H}_{\text{int}} = \frac{C_6}{R^6} \hat{n}_1 \hat{n}_2 \sim J \underbrace{\hat{\sigma}_1^z \hat{\sigma}_2^z}_{n=0,1}$$

$$\hat{n} = \frac{1 + \hat{\sigma}_z}{2}$$

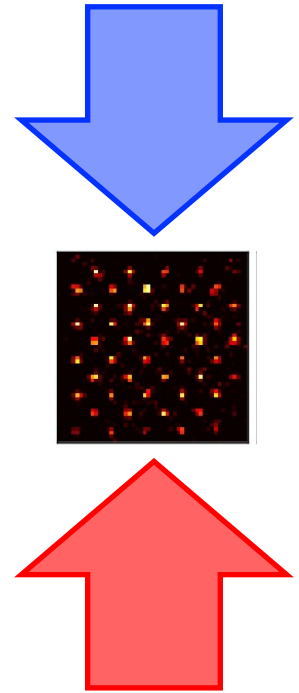
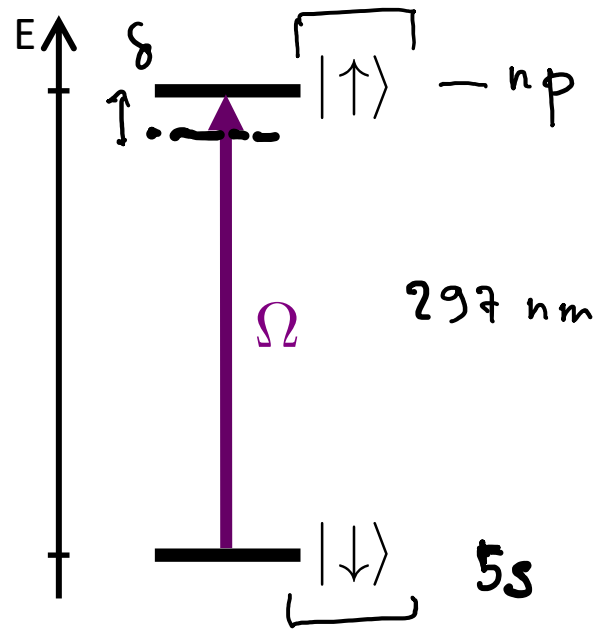
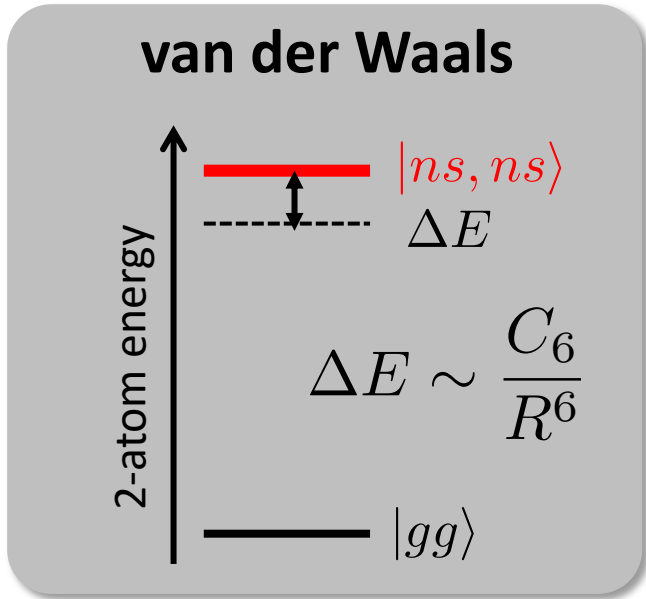
$$\text{AS: } \hat{n} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} = \frac{1}{2} \left[\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} + \mathbb{1} \right]$$

Rydberg occupation number

From van der Waals interactions to Ising model...



From van der Waals interactions to Ising model...



$$H_{\text{laser}} = \frac{\Omega}{2} \hat{\sigma}_x - \delta \hat{\sigma}_z \quad \text{with } \delta = \omega_L - \omega_0$$

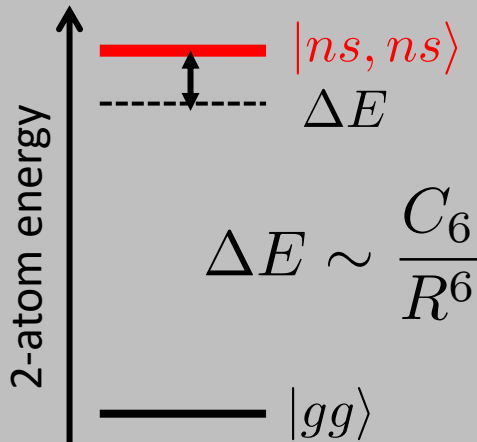
(RWA)

And $\hat{\sigma}_x \equiv \hat{\sigma}_+ + \hat{\sigma}_-$

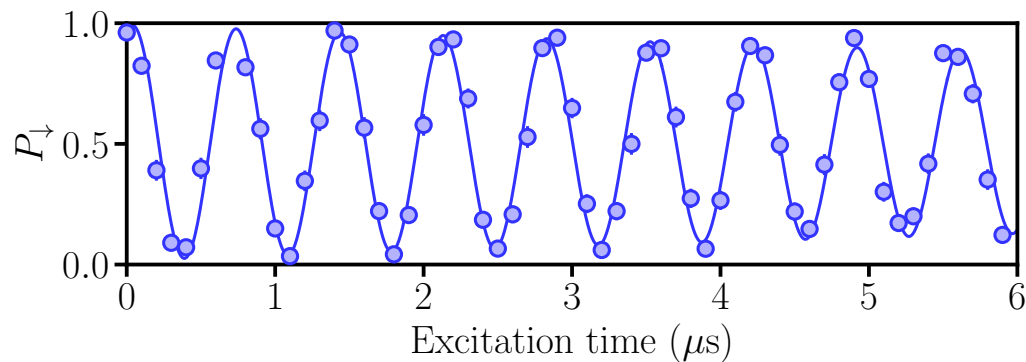
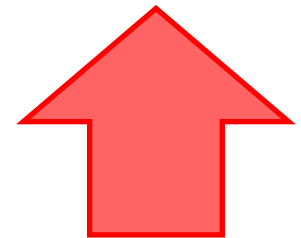
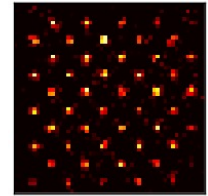
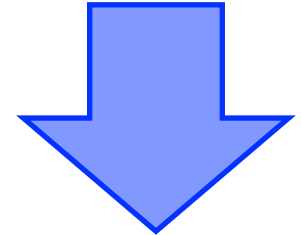
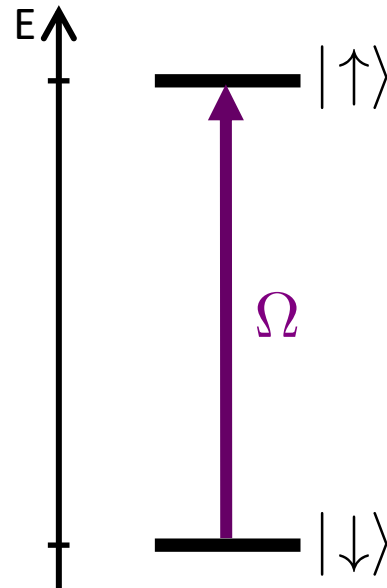
From van der Waals interactions to Ising model...



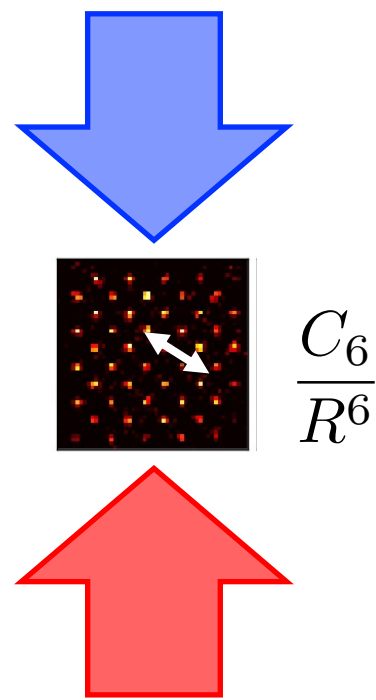
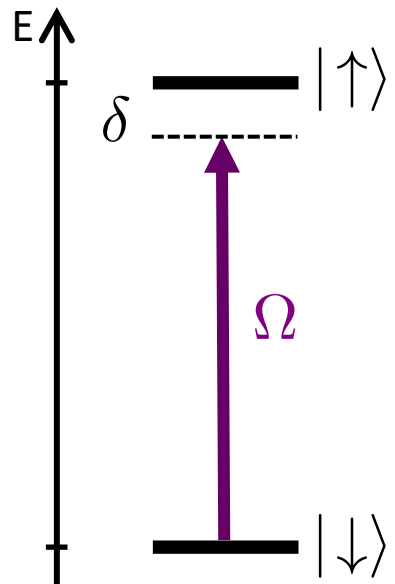
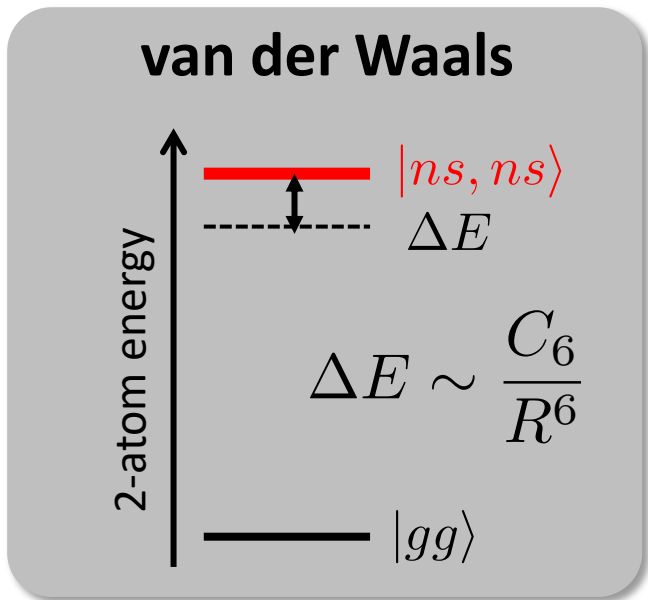
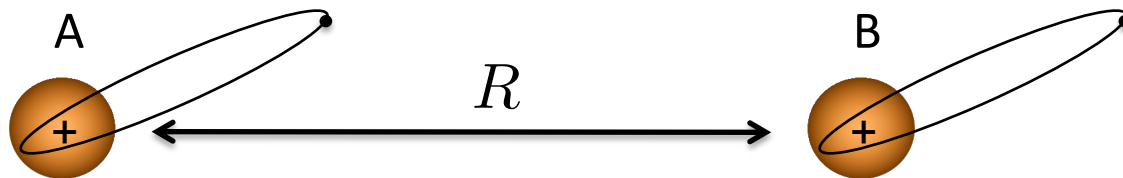
van der Waals



$$\Delta E \sim \frac{C_6}{R^6}$$



From van der Waals interactions to Ising model...



Quantum Ising-like model ($s=1/2$):

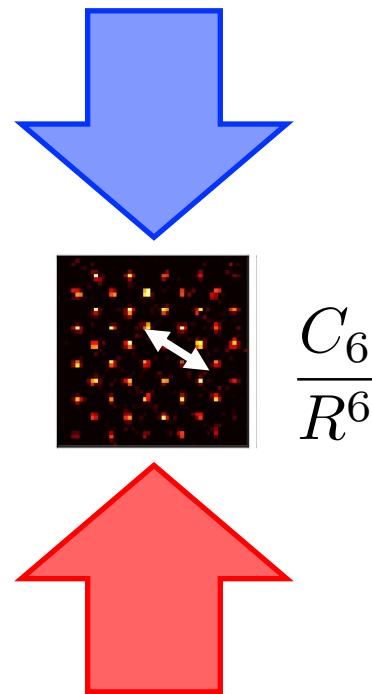
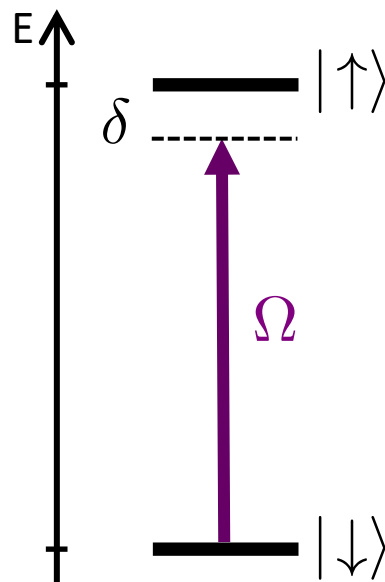
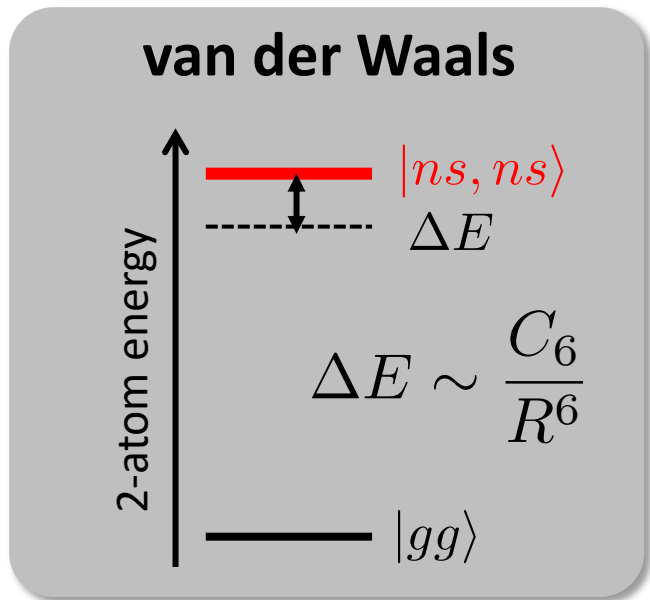
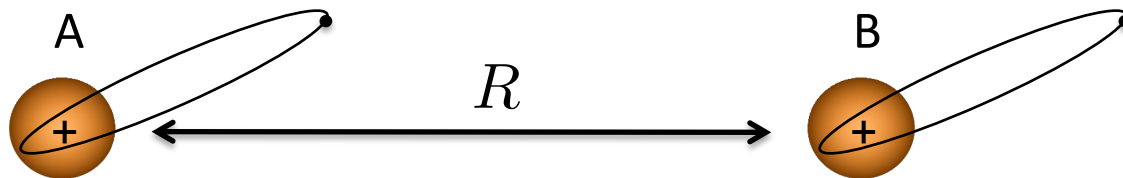
$$H = \frac{\hbar\Omega}{2} \sum_i \sigma_x^i + \hbar\delta \sum_i \hat{n}_i + \sum_{i<j} \frac{C_6}{R_{ij}^6} \hat{n}_i \hat{n}_j$$

Ising-interaction.

Transverse B **Longitudinal B** **Spin-spin interaction**

$[\sigma_x, \hat{n}_i \hat{n}_j] \neq 0$
 \Downarrow
 "quantum"

From van der Waals interactions to Ising model...



Quantum Ising-like model ($s=1/2$):

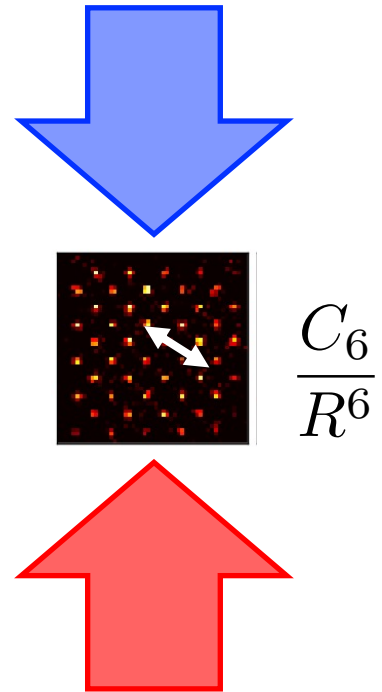
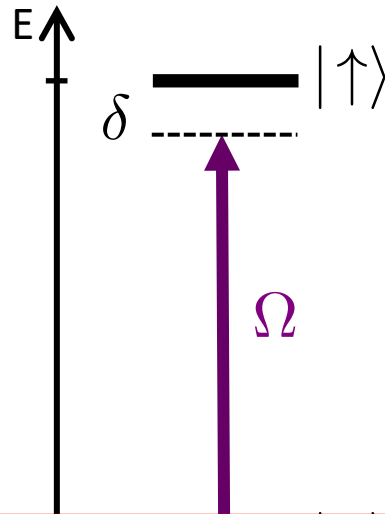
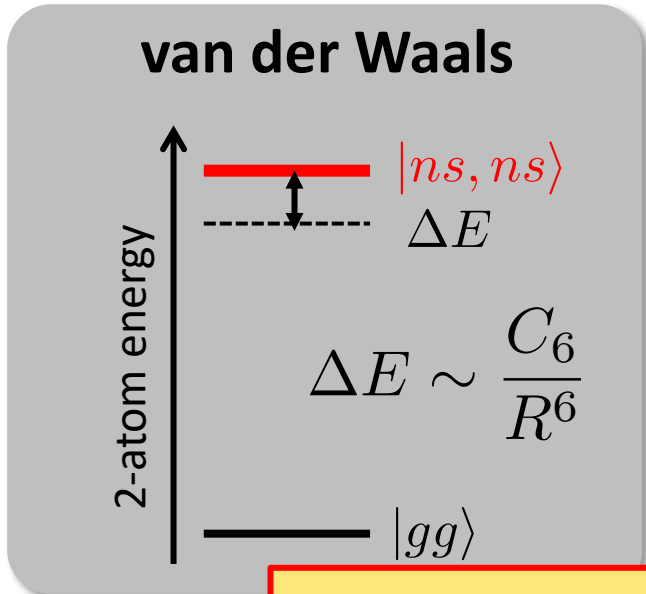
$$H = \frac{\hbar\Omega}{2} \sum_i \sigma_x^i + \hbar\delta \sum_i \hat{n}_i + \sum_{i<j} \frac{C_6}{R_{ij}^6} \hat{n}_i \hat{n}_j$$

Experiment^t.

$$\frac{C_6/a^6}{\Omega} = [0 - 20]$$

Transverse B **Longitudinal B** **Spin-spin interaction**

From van der Waals interactions to Ising model...



Quantum Ising

$$H = \frac{\hbar\Omega}{2} \sum_i \sigma_i^x$$

Transverse

Equilibrium: preparation of ground states

Out-of-equilibrium: sudden variation ("quench") of parameters

Experiment.

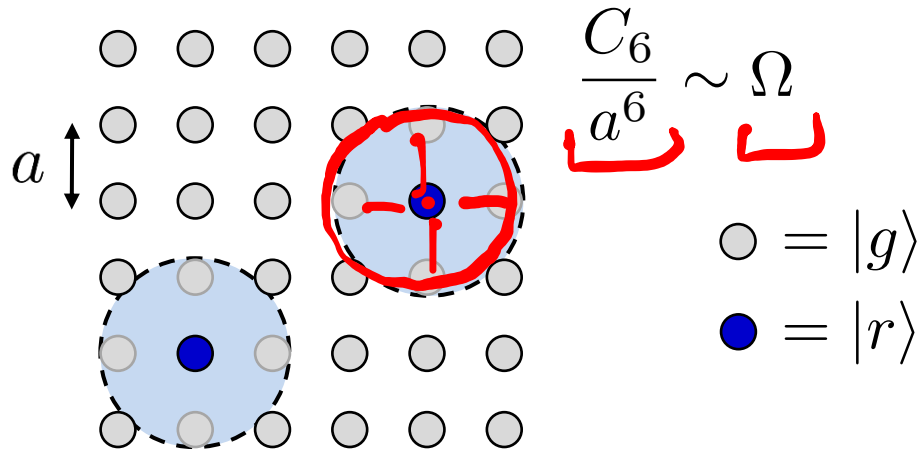
$$= [0 - 20]$$

Outline

1. Quantum simulation and spin models
2. Simulation of the quantum Ising model using van der Waals interactions: quantum magnetism
 - Preparation of ground states
 - Out-of-equilibrium situations
3. Topological systems using resonant dipole interactions

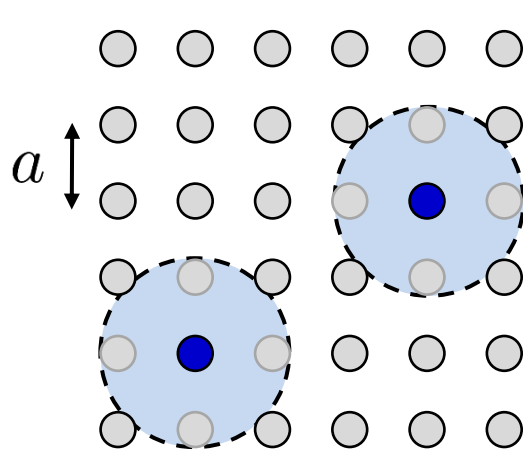
2D Ising anti-ferromagnet on a square

Nearest neighb. interaction



2D Ising anti-ferromagnet on a square

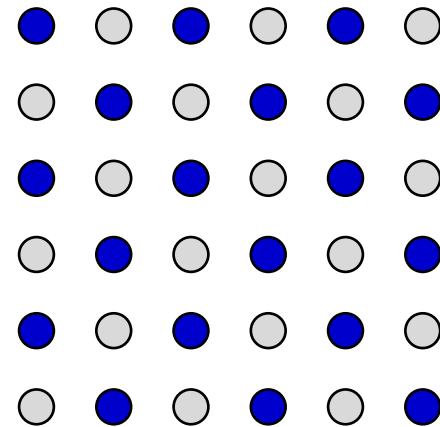
Nearest neighb. interaction



$$\frac{C_6}{a^6} \sim \Omega$$

$$\begin{aligned} \circ &= |g\rangle \\ \bullet &= |r\rangle \end{aligned}$$

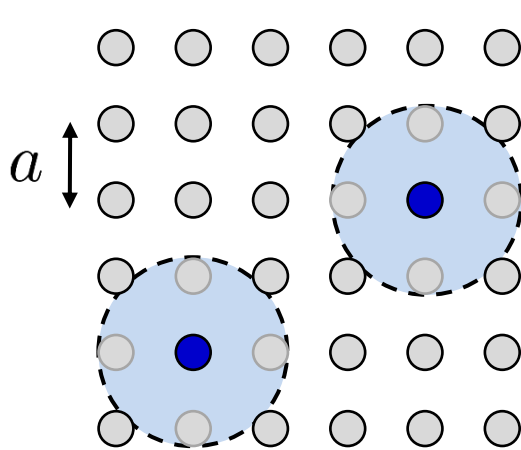
Anti-ferromagnetic ground state



2D Ising anti-ferromagnet on a square

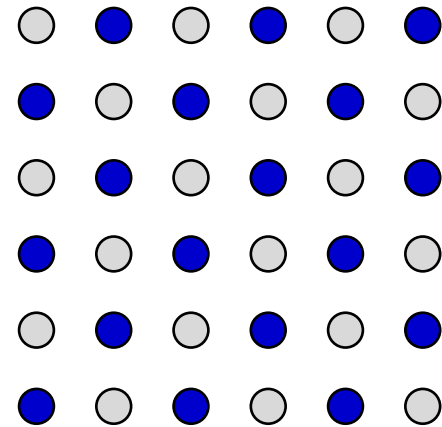
Nearest neighb. interaction

Anti-ferromagnetic ground state



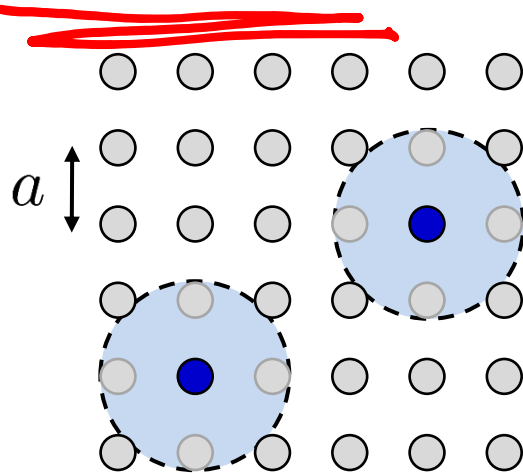
$$\frac{C_6}{a^6} \sim \Omega$$

$$\begin{aligned} \circ &= |g\rangle \\ \bullet &= |r\rangle \end{aligned}$$



2D Ising anti-ferromagnet on a square

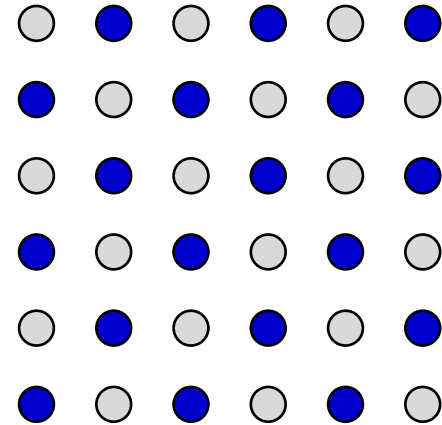
Nearest neighb. interaction



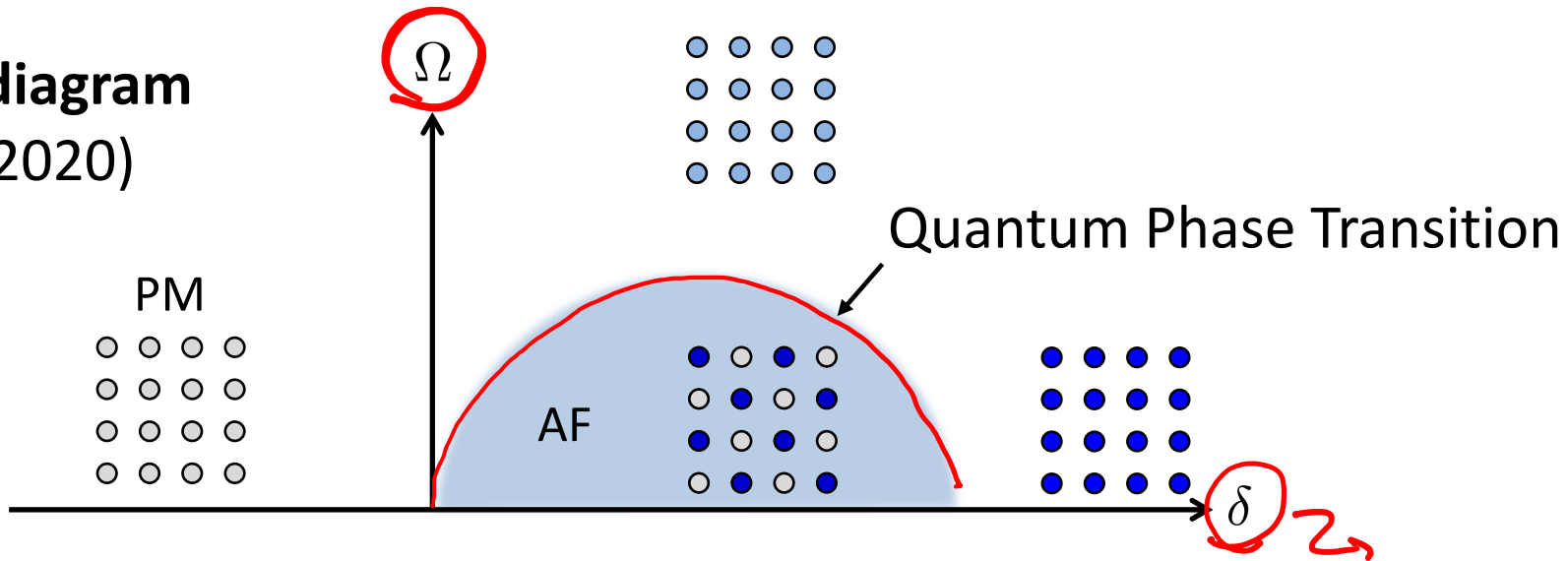
$$\frac{C_6}{a^6} \sim \Omega$$

○ = $|g\rangle$
● = $|r\rangle$

Anti-ferromagnetic ground state



2D phase diagram
(1970 - 2020)



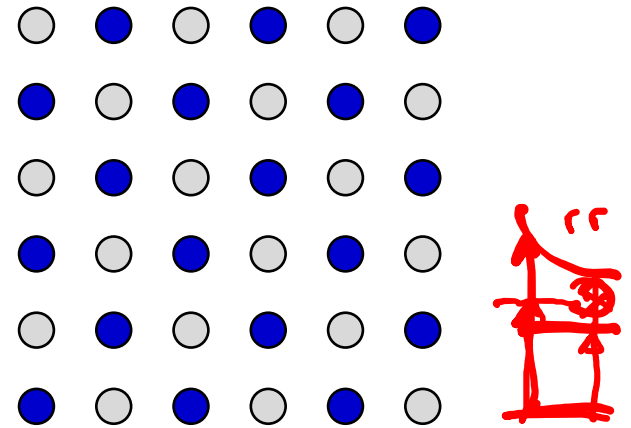
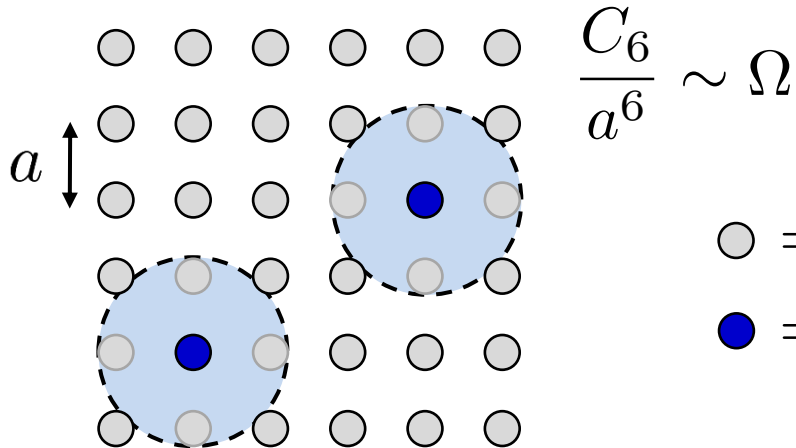
Known by Quantum Monte-Carlo

Never implemented and measured in 2D...!!!

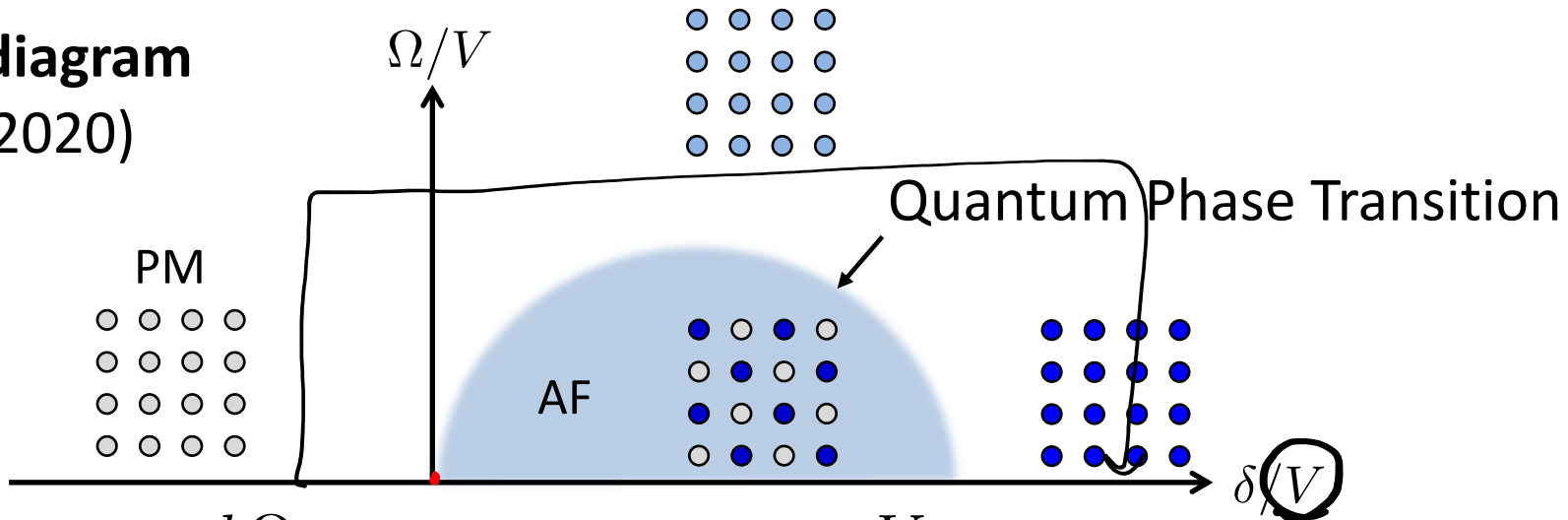
2D Ising anti-ferromagnet on a square

Nearest neighb. interaction

Anti-ferromagnetic ground state



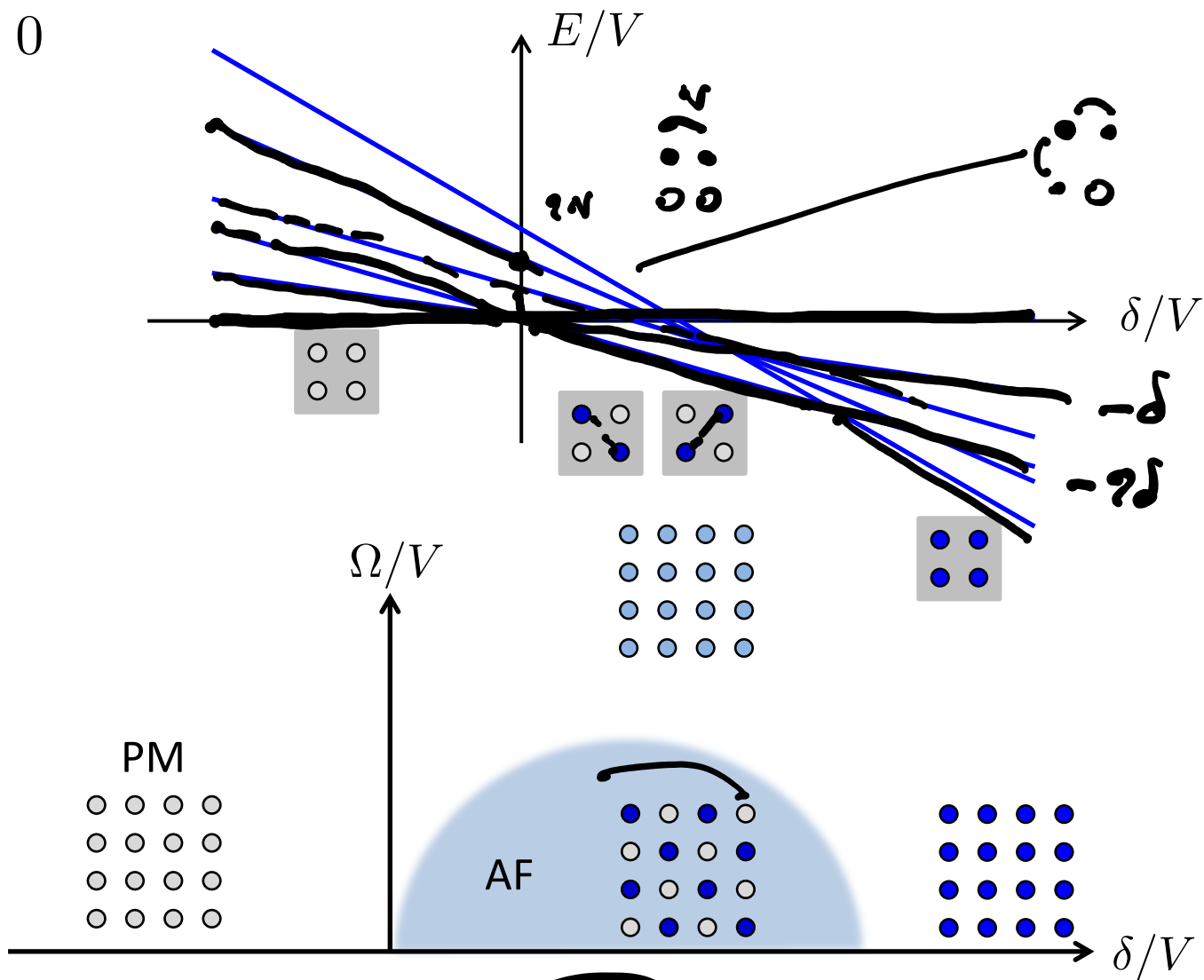
2D phase diagram
(1970 - 2020)



$$H = \frac{\hbar\Omega}{2} \sum_i \sigma_x^i - \hbar\delta \sum_i \hat{n}_i + \frac{V}{2} \sum_i \hat{n}_i \hat{n}_{i+1}$$

2D Ising anti-ferromagnet on a square

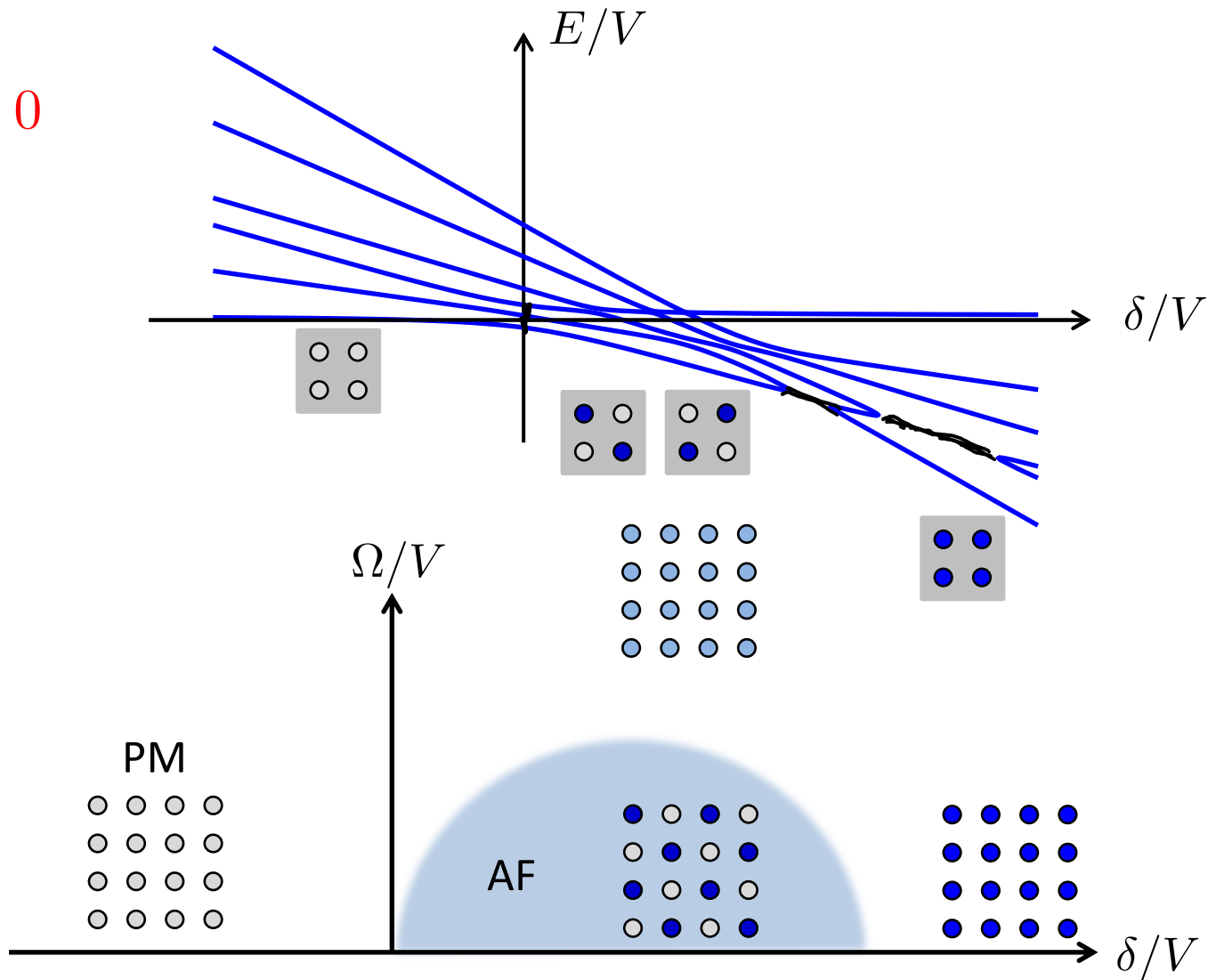
$\Omega/V = 0$



$$H = -\hbar\delta \sum_i \hat{n}_i + \frac{V}{2} \sum_i \hat{n}_i \hat{n}_{i+1}$$

2D Ising anti-ferromagnet on a square

$\Omega/V \neq 0$



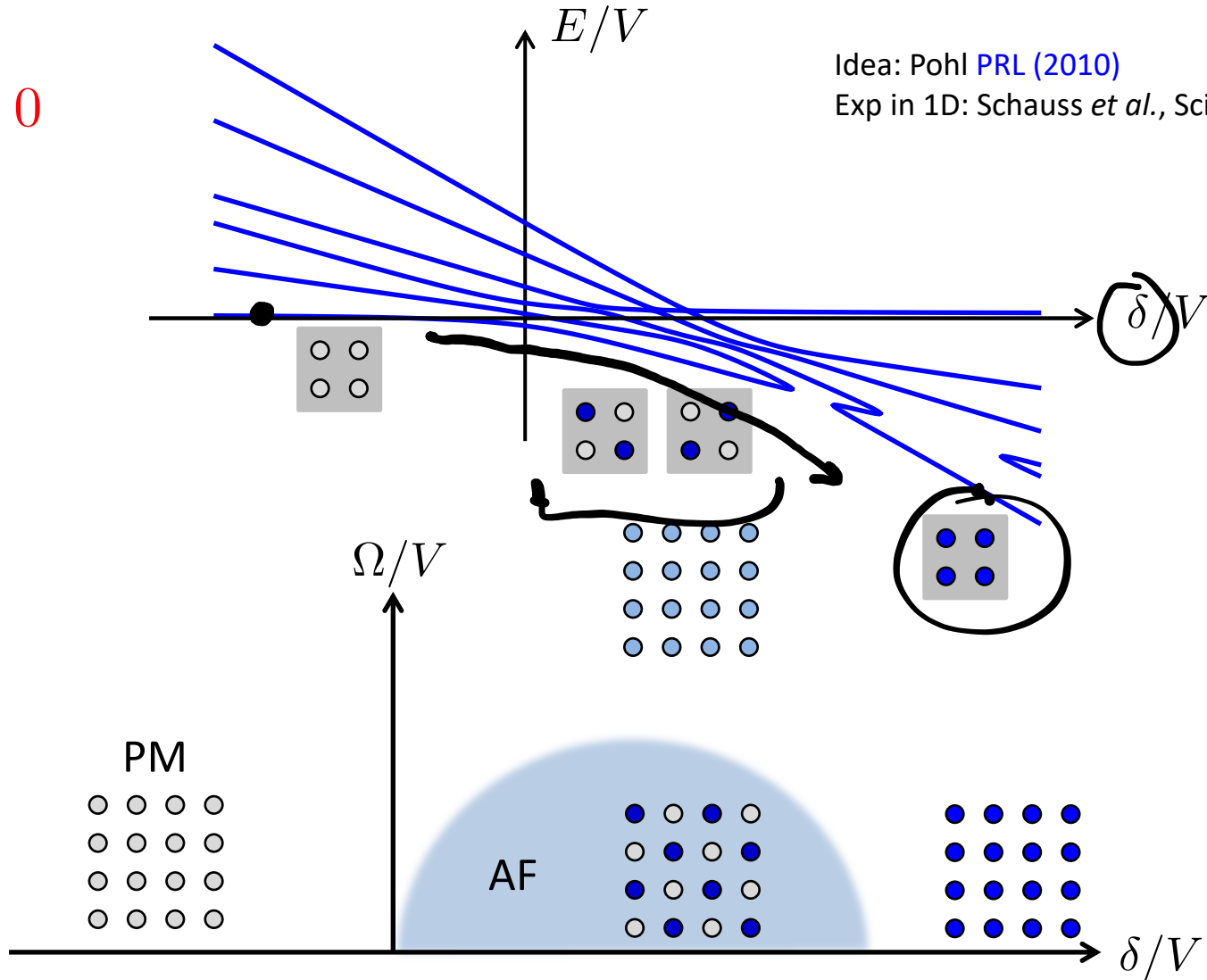
$$H = \frac{\hbar\Omega}{2} \sum_i \sigma_x^i - \hbar\delta \sum_i \hat{n}_i + \frac{V}{2} \sum_i \hat{n}_i \hat{n}_{i+1}$$

Adiabatic preparation of a 2D Ising anti-ferromagnet

$\Omega/V \neq 0$

Idea: Pohl [PRL \(2010\)](#)

Exp in 1D: Schauss *et al.*, [Science \(2015\)](#)



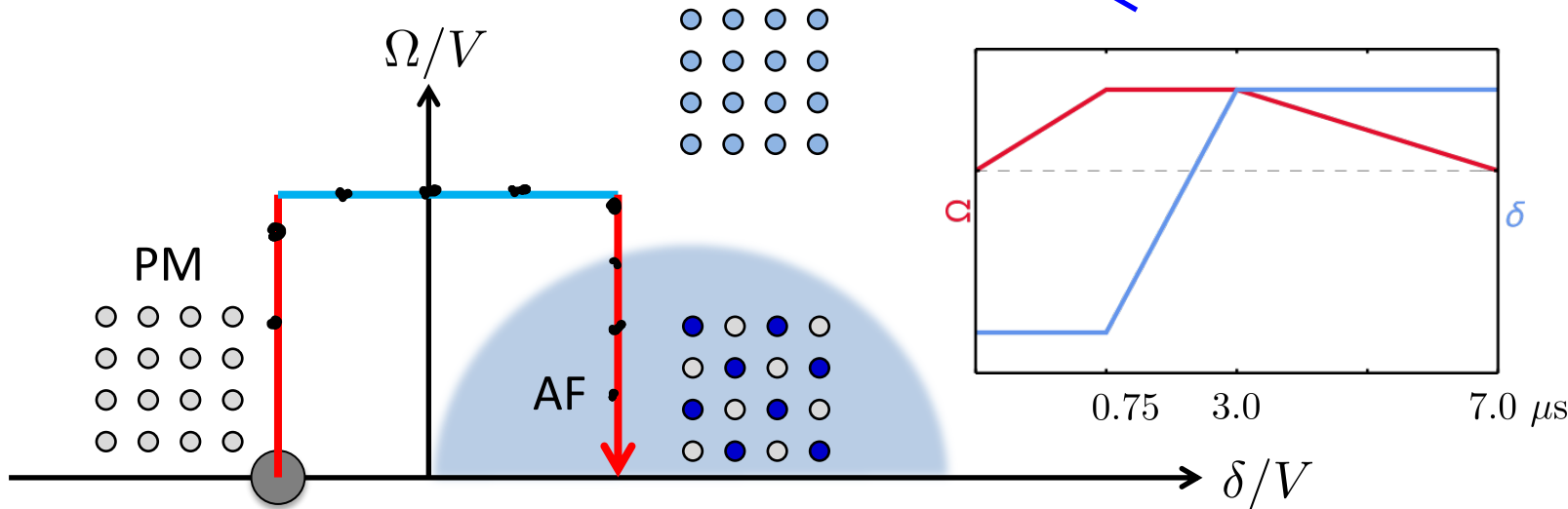
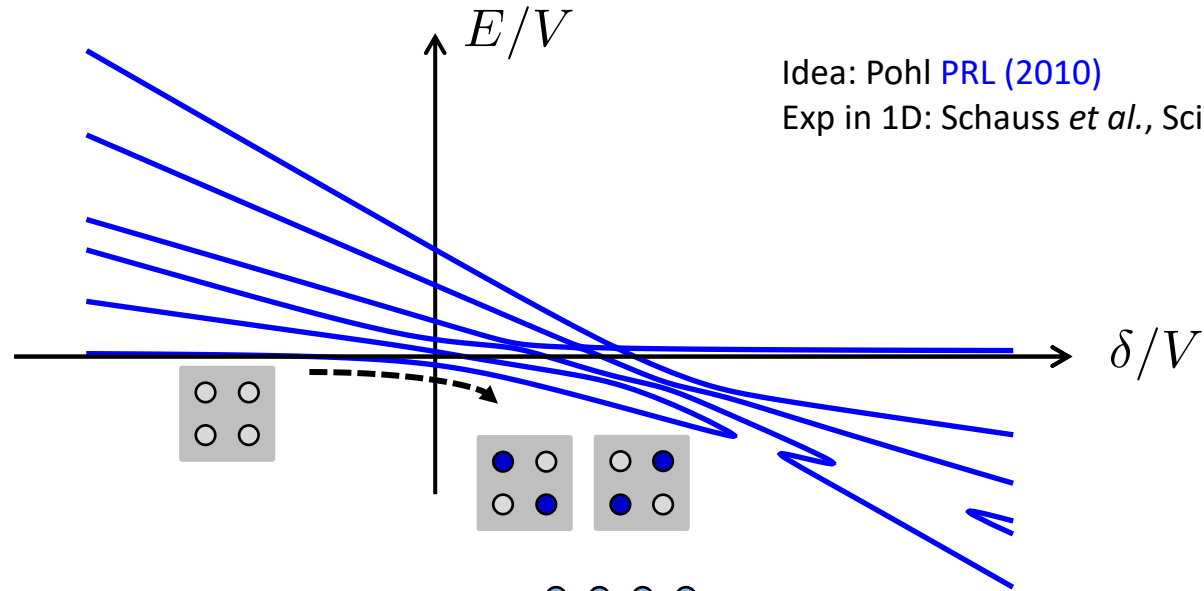
$$H = \sum_i \left(\frac{\hbar\Omega(t)}{2} \sigma_x^i - \hbar\delta(t) \hat{n}_i \right) + \sum_{i<j} \frac{C_6}{R_{ij}^6} \hat{n}_i \hat{n}_j$$

Adiabatic preparation of a 2D Ising anti-ferromagnet

$$\Omega/V \neq 0$$

Idea: Pohl [PRL \(2010\)](#)

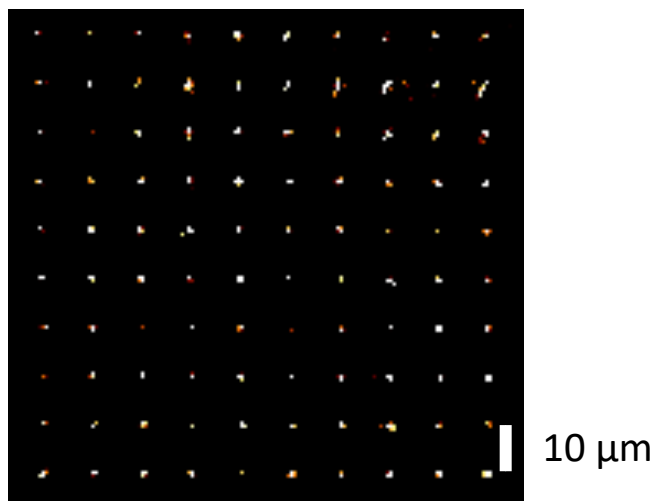
Exp in 1D: Schauss *et al.*, [Science \(2015\)](#)



$$H = \sum_i \left(\frac{\hbar\Omega(t)}{2} \sigma_x^i - \hbar\delta(t) \hat{n}_i \right) + \sum_{i<j} \frac{C_6}{R_{ij}^6} \hat{n}_i \hat{n}_j$$

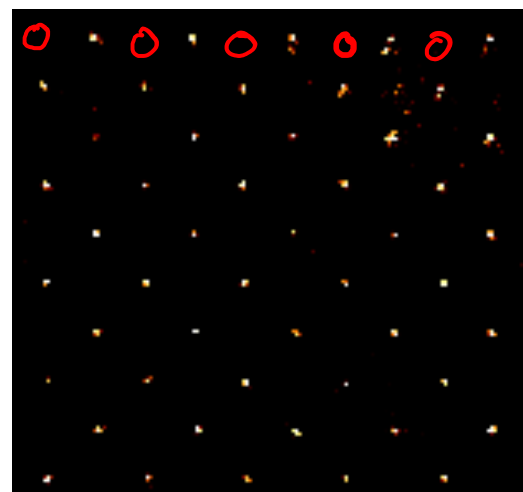
Preparation of a 2D Ising anti-ferromagnet on a square

10 × 10 square array

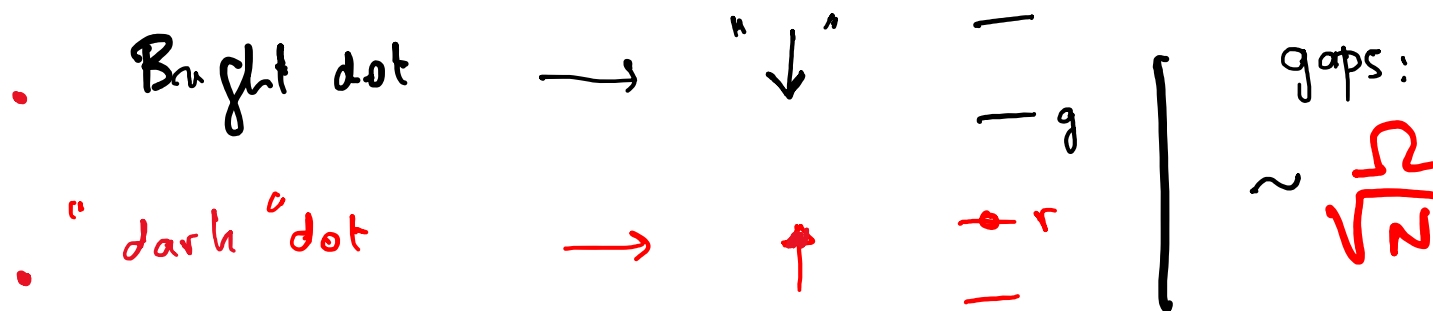


sweep
 $n=75s$

Scholl, arXiv:2012.12268



Missing atoms = Rydberg



1D: Pohl [PRL 2010](#); Bloch [Science 2015](#); Lukin [Nature 2017, 2019](#);

2D: Lienhard [PRX 2018](#), Bakr [PRX 2018](#); Lukin [arXiv:2012.12281](#)

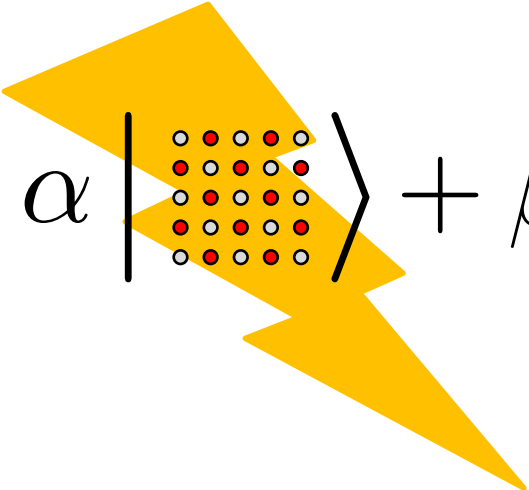
Seeing the many-body wavefunction...

At the end of experiment:

$$|\Psi\rangle = \alpha \left| \begin{array}{ccccc} \circ & \bullet & \circ & \bullet & \circ \\ \bullet & \circ & \bullet & \circ & \bullet \\ \circ & \bullet & \circ & \bullet & \circ \\ \bullet & \circ & \bullet & \circ & \bullet \\ \circ & \bullet & \circ & \bullet & \circ \end{array} \right\rangle + \beta \left| \begin{array}{ccccc} \circ & \bullet & \circ & \circ & \circ \\ \circ & \bullet & \bullet & \circ & \bullet \\ \circ & \bullet & \circ & \bullet & \circ \\ \bullet & \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \bullet & \circ \end{array} \right\rangle + \gamma \left| \begin{array}{ccccc} \circ & \bullet & \circ & \bullet & \circ \\ \bullet & \circ & \bullet & \circ & \bullet \\ \circ & \circ & \bullet & \circ & \circ \\ \circ & \circ & \bullet & \circ & \bullet \\ \circ & \bullet & \circ & \bullet & \bullet \end{array} \right\rangle + \dots$$

Seeing the many-body wavefunction...

At the end of experiment:

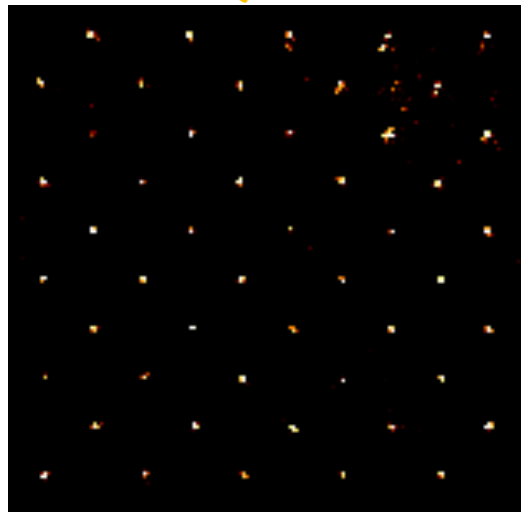
$$|\Psi\rangle = \alpha \left| \begin{array}{cccc} \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \end{array} \right\rangle + \beta \left| \begin{array}{cccc} \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \end{array} \right\rangle + \gamma \left| \begin{array}{cccc} \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \\ \circ & \bullet & \circ & \circ \end{array} \right\rangle + \dots$$


Seeing the many-body wavefunction...

At the end of experiment:

$$|\Psi\rangle = \alpha \left| \begin{array}{cccc} \circ & \bullet & \circ & \circ \\ \bullet & \bullet & \bullet & \circ \\ \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \end{array} \right\rangle + \beta \left| \begin{array}{cccc} \circ & \bullet & \circ & \circ \\ \bullet & \bullet & \circ & \bullet \\ \bullet & \bullet & \bullet & \circ \\ \bullet & \bullet & \circ & \bullet \end{array} \right\rangle + \gamma \left| \begin{array}{cccc} \circ & \bullet & \circ & \circ \\ \bullet & \bullet & \circ & \bullet \\ \bullet & \bullet & \bullet & \circ \\ \bullet & \bullet & \circ & \bullet \end{array} \right\rangle + \dots$$

$$|\Psi_f\rangle =$$

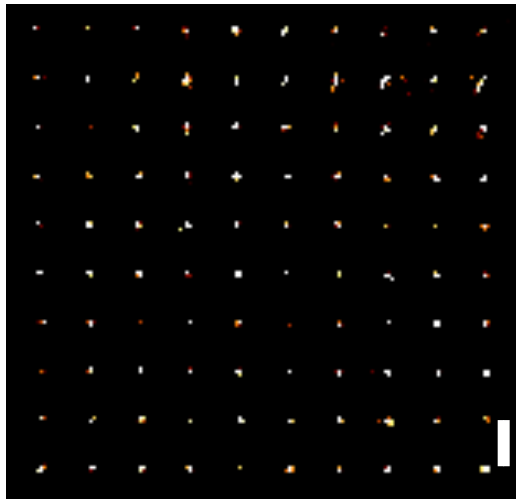


probability $|\alpha|^2$

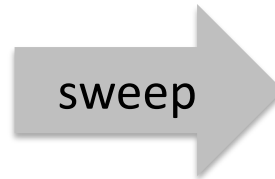
Preparation of a 2D Ising anti-ferromagnet on a square

Scholl, arXiv:2012.12268

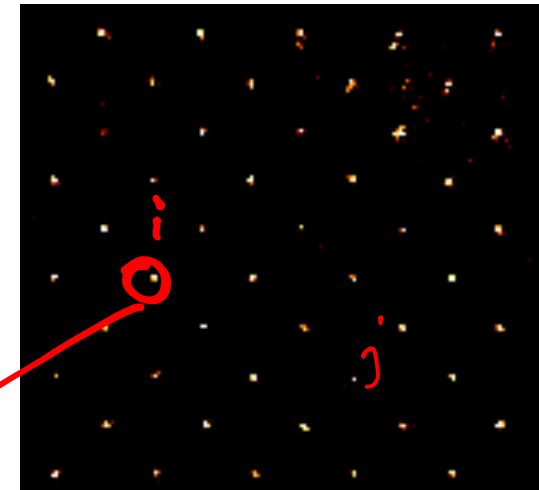
10 × 10 square array



10 μm



$n=75s$



Missing atoms = Rydberg

Perfect AF (Néel) ordering!
(proba < 1%)

σ_i^z σ_j^z

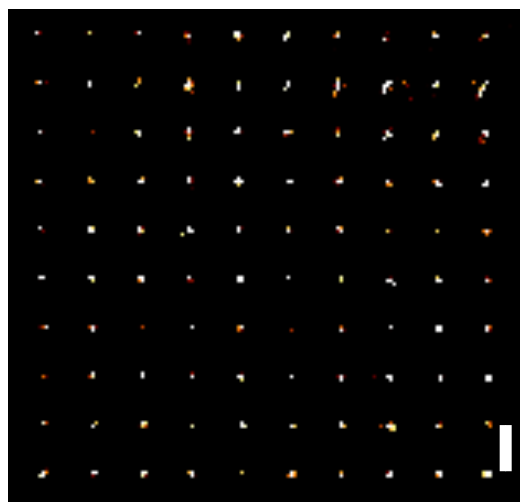
\uparrow
 \downarrow

1D: Pohl [PRL 2010](#); Bloch [Science 2015](#); Lukin [Nature 2017, 2019](#);

2D: Lienhard [PRX 2018](#), Bakr [PRX 2018](#); Lukin [arXiv:2012.12281](#)

Preparation of a 2D Ising anti-ferromagnet on a square

10 × 10 square array

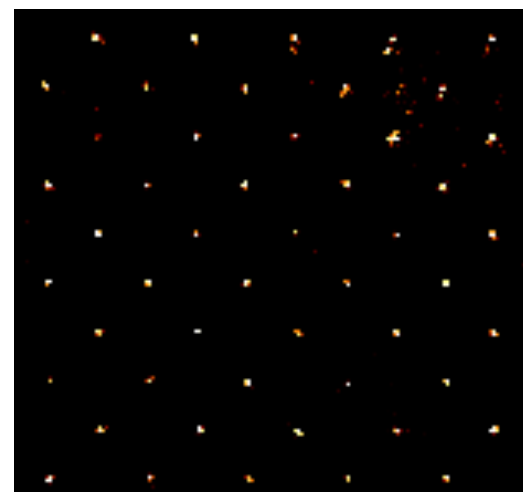


10 μm

sweep

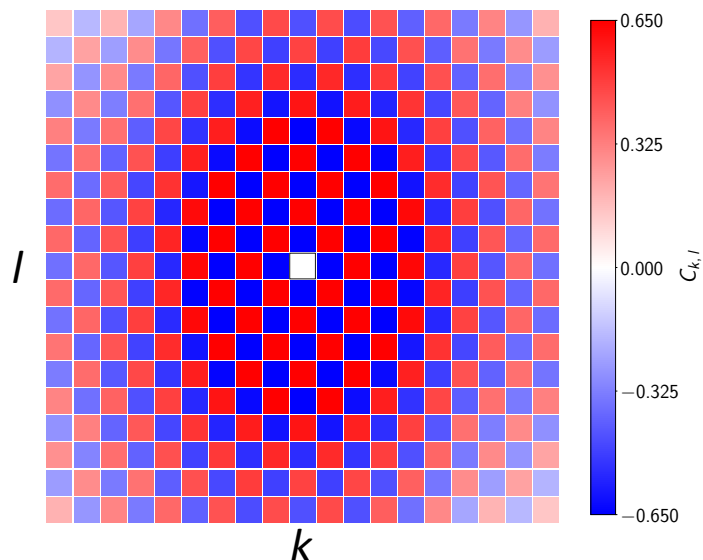
$n=75s$

Scholl, arXiv:2012.12268



$$C_{kl} \sim \langle n_k n_l \rangle - \langle n_k \rangle \langle n_l \rangle \sim \langle \sigma_k^z \sigma_l^z \rangle$$

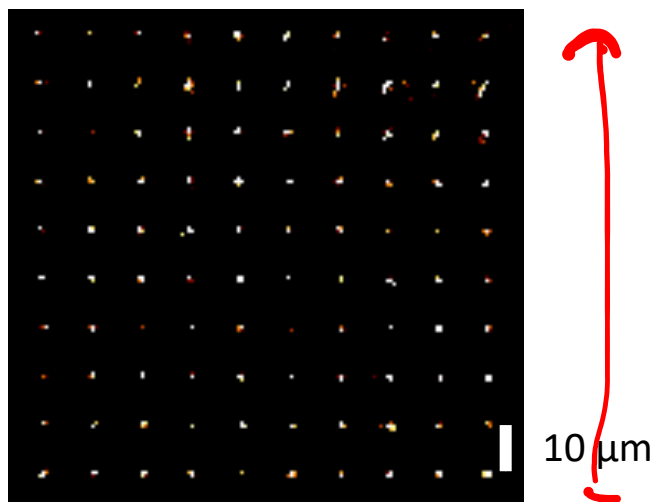
Missing atoms = Rydberg



Also: Lukin arXiv:2012.12281

Preparation of a 2D Ising anti-ferromagnet on a square

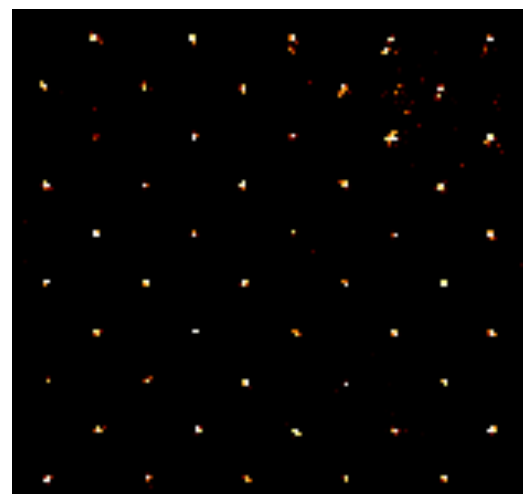
10 × 10 square array



sweep

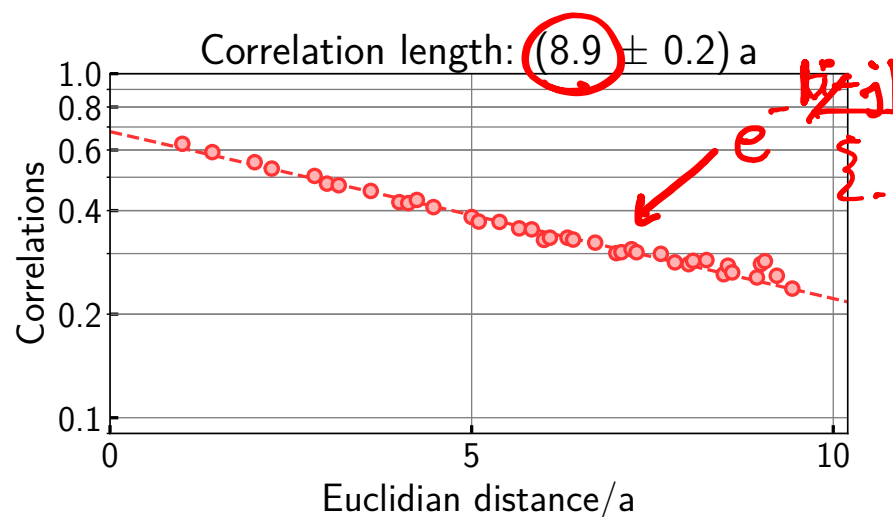
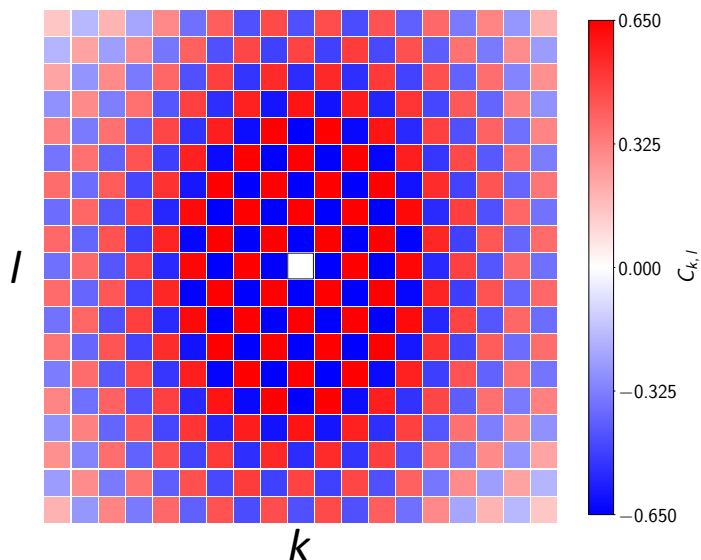
$n=75s$

Scholl, arXiv:2012.12268



Missing atoms = Rydberg

$$C_{kl} \sim \langle n_k n_l \rangle - \langle n_k \rangle \langle n_l \rangle$$

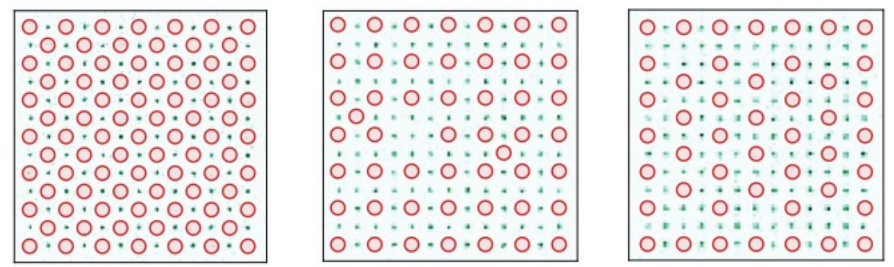
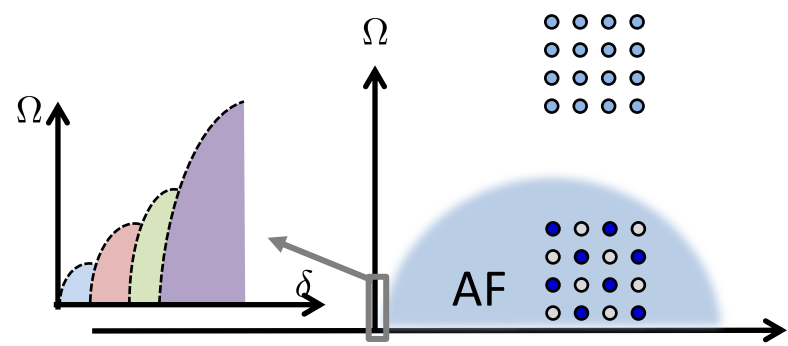


Also: Lukin arXiv:2012.12281

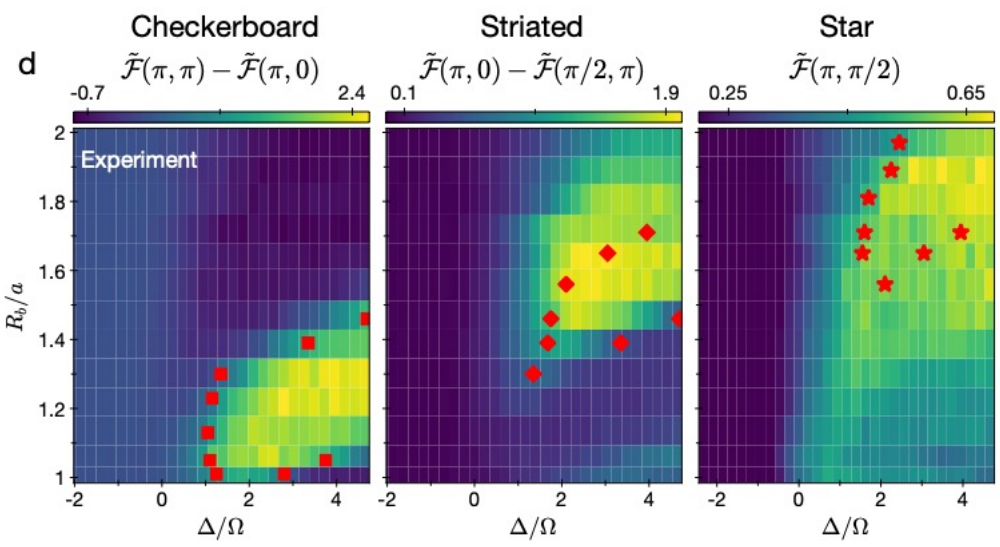
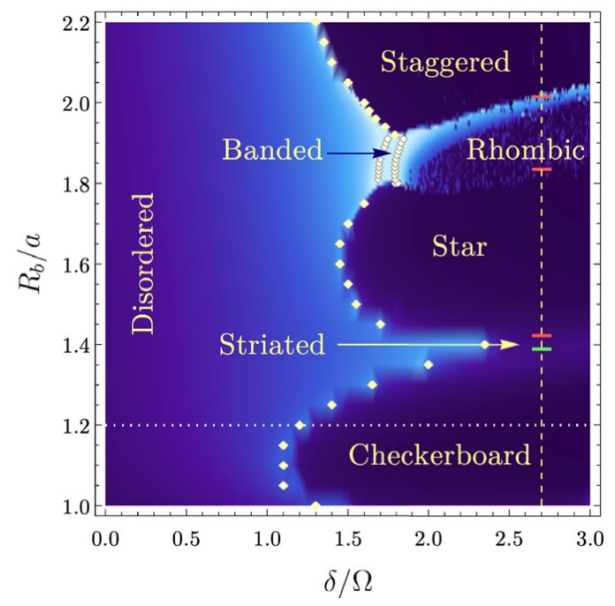
2D Ising anti-ferromagnet on a square beyond NN interactions

Lukin arXiv:2012.12281

Samajdar *et al.* PRL (2020)



Vary $(C_6/a^6)/\Omega$



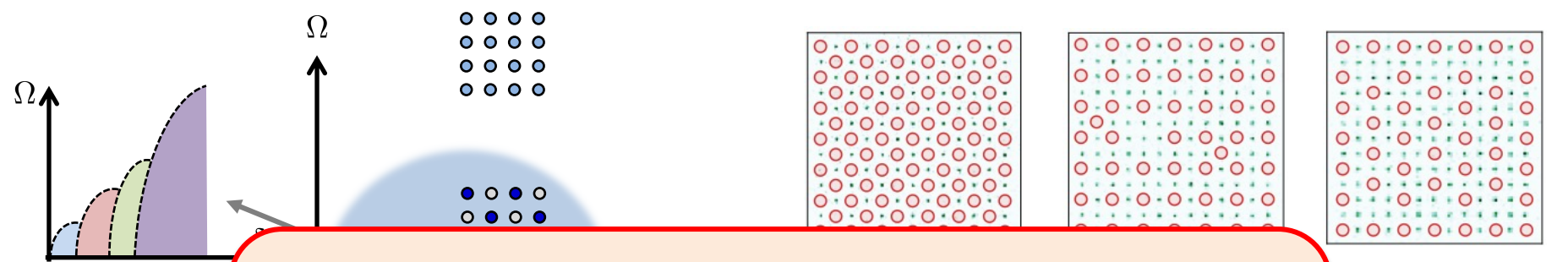
Order parameters:

$$\mathcal{F}(\mathbf{k}) = \frac{1}{\sqrt{N}} \sum_i n_i e^{i\mathbf{k} \cdot \mathbf{x}_i}$$

2D Ising anti-ferromagnet on a square beyond NN interactions

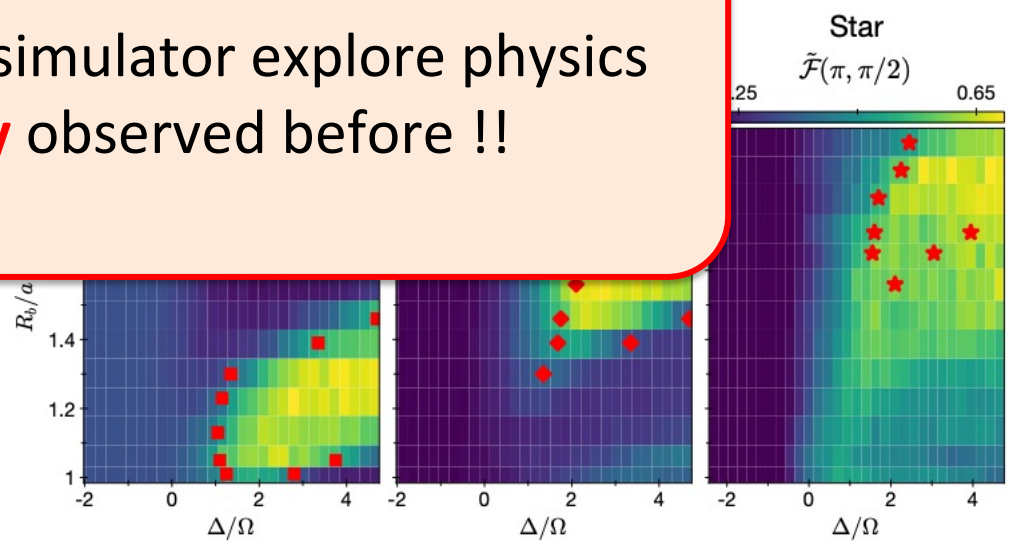
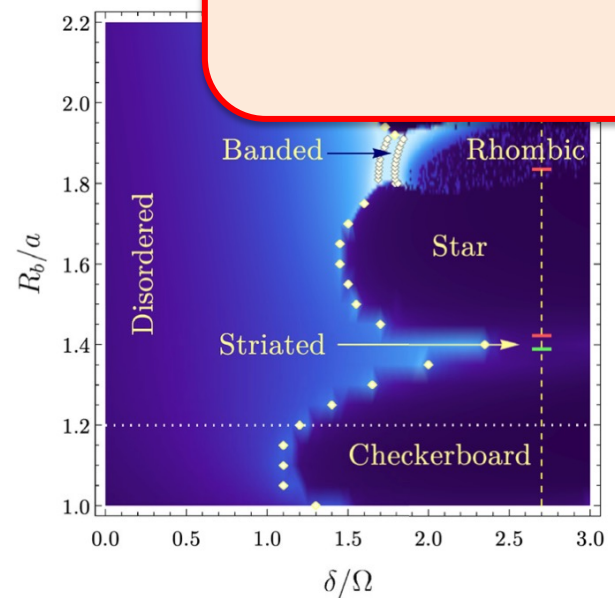
Lukin arXiv:2012.12281

Samajdar *et al.* PRL (2020)



Rydberg quantum simulator explore physics **never directly** observed before !!

Vary (C_6)

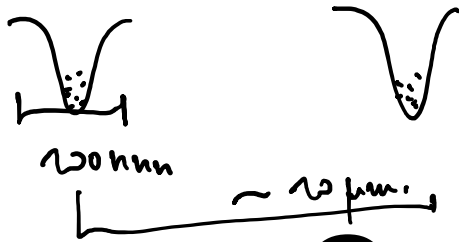


Order parameters:

$$\mathcal{F}(\mathbf{k}) = \frac{1}{\sqrt{N}} \sum_i n_i e^{i\mathbf{k} \cdot \mathbf{x}_i}$$

Role of Shot-to-shot fluctuations: in positions of the atoms.

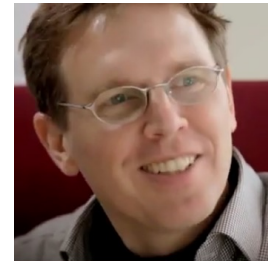
$$J \sigma_i^z \sigma_j^z$$



Questions ?

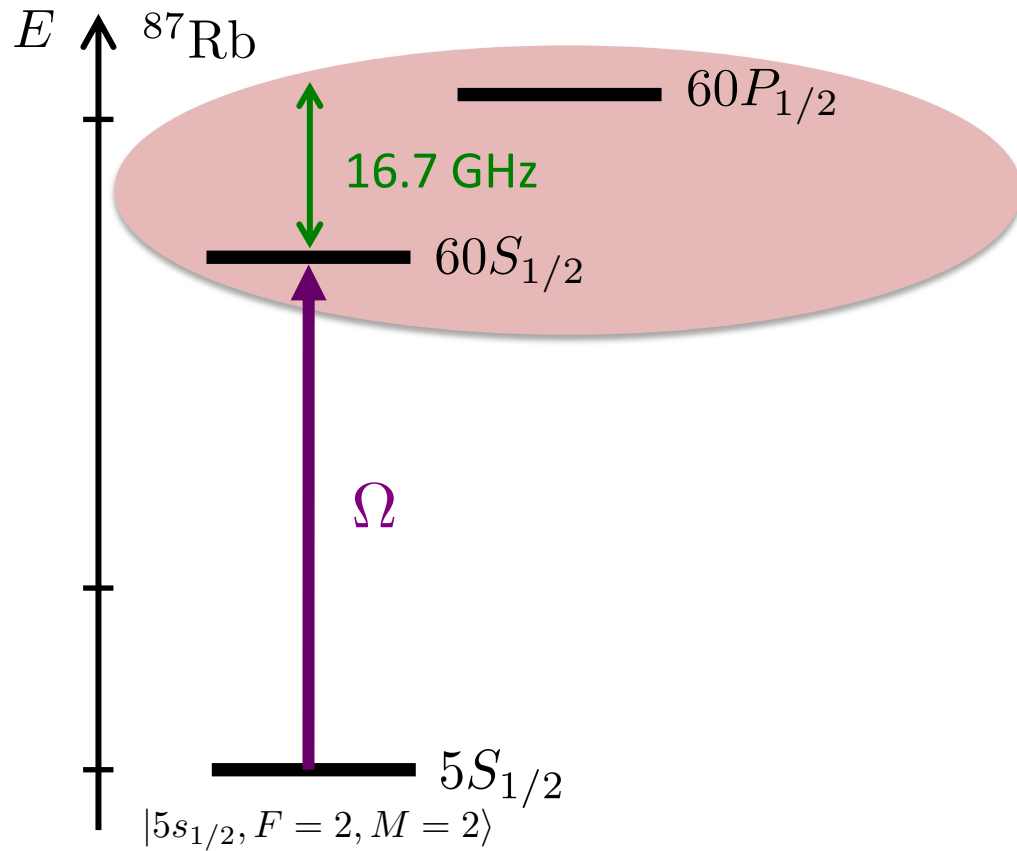
Outline

1. Quantum simulation and spin models
2. Simulation of Ising model using van der Waals interactions
3. Topological systems using resonant dipole interactions

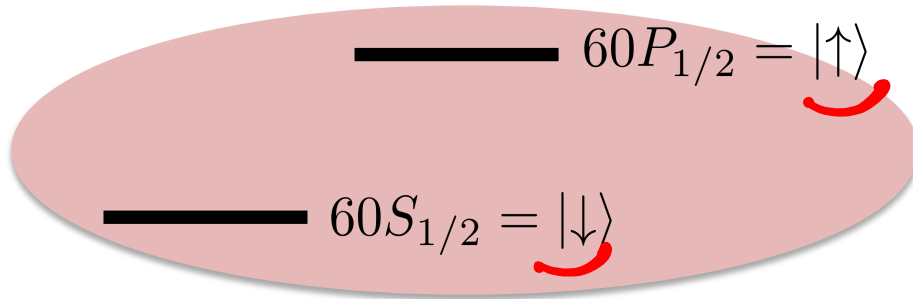


H.-P. Büchler
S. Weber, N. Lang

Resonant dipole-dipole interaction between Rydberg atoms

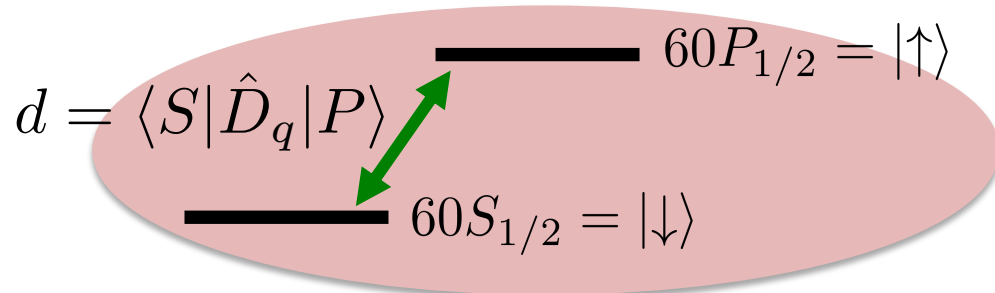


Resonant dipole-dipole interaction between Rydberg atoms



Mapping on
spin $\frac{1}{2}$ system

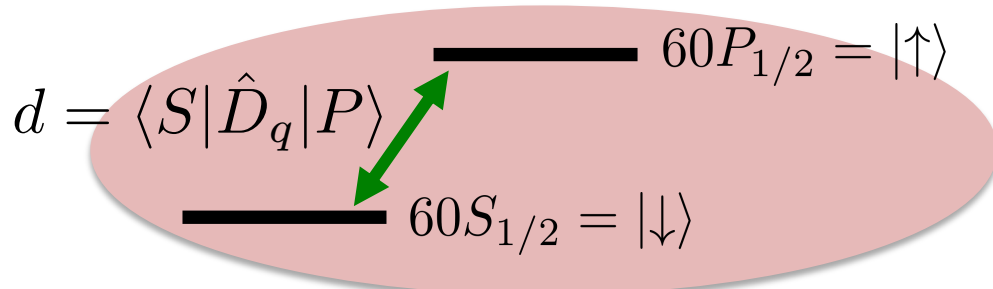
Resonant dipole-dipole interaction between Rydberg atoms



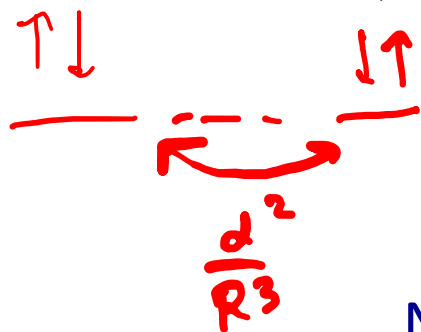
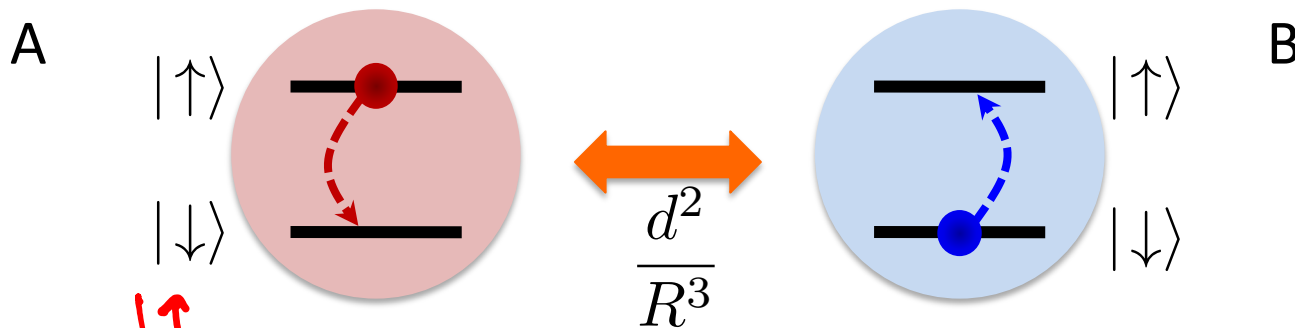
Mapping on
spin $\frac{1}{2}$ system



Resonant dipole-dipole interaction between Rydberg atoms



Mapping on spin $\frac{1}{2}$ system



$$\hat{H} = \frac{d^2}{4\pi\epsilon_0 R^3} (\hat{\sigma}_A^+ \hat{\sigma}_B^- + \hat{\sigma}_A^- \hat{\sigma}_B^+)$$

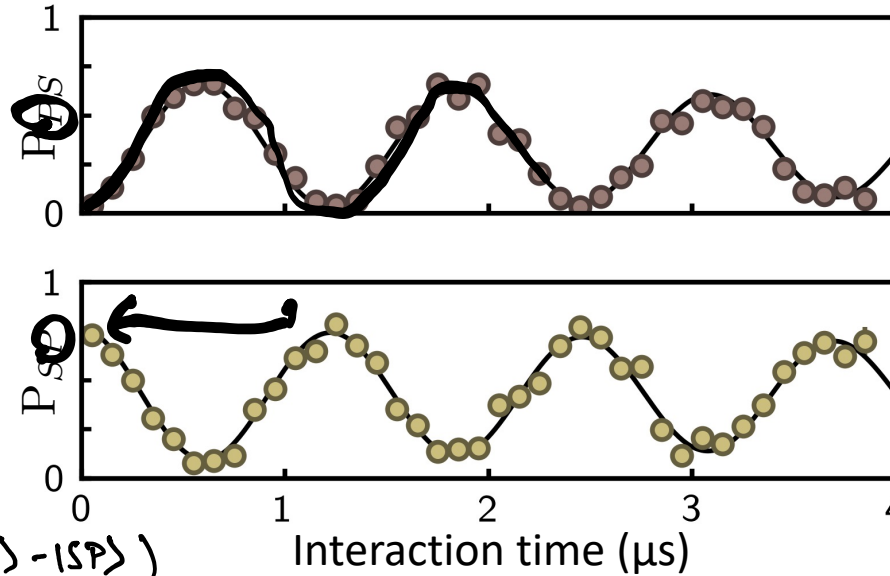
Non radiative “exchange” of excitation

Observation of resonant dip.-dip. interaction with 2 atoms

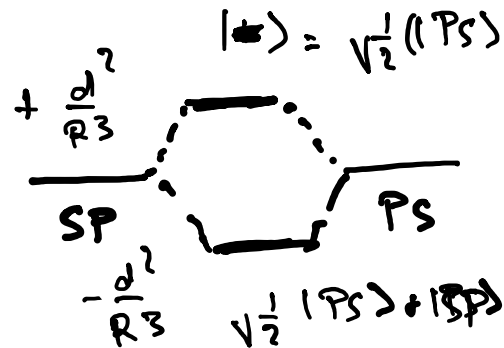
Prepare $|\uparrow\downarrow\rangle$ using microwaves + addressing beam

$R = 30 \mu\text{m}$

Frequency: $\frac{2C_3}{R^3}$



Barredo PRL (2015)
de Léséleuc, PRL (2017)



$$|\psi(0)\rangle = |PS\rangle = \frac{1}{\sqrt{2}}(|+\rangle + |-\rangle)$$

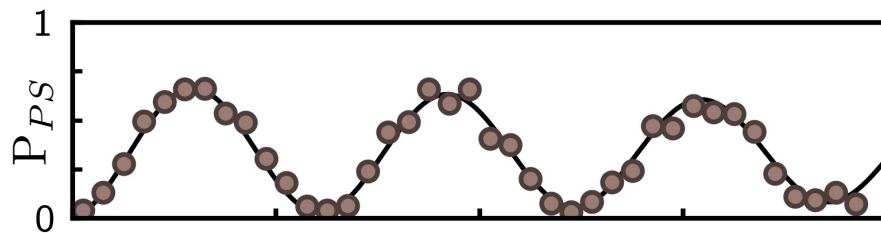
$$|\psi(t)\rangle = \frac{1}{\sqrt{2}} \left(e^{-i\frac{d^2}{R^3}t/4} |+\rangle + e^{+i\frac{d^2}{R^3}t/4} |-\rangle \right)$$

$$|\langle PS | \psi(t) \rangle|^2 = P_{PS} = \cos^2\left(\frac{d^2}{R^3}t/4\right)$$

Observation of resonant dip.-dip. interaction with 2 atoms

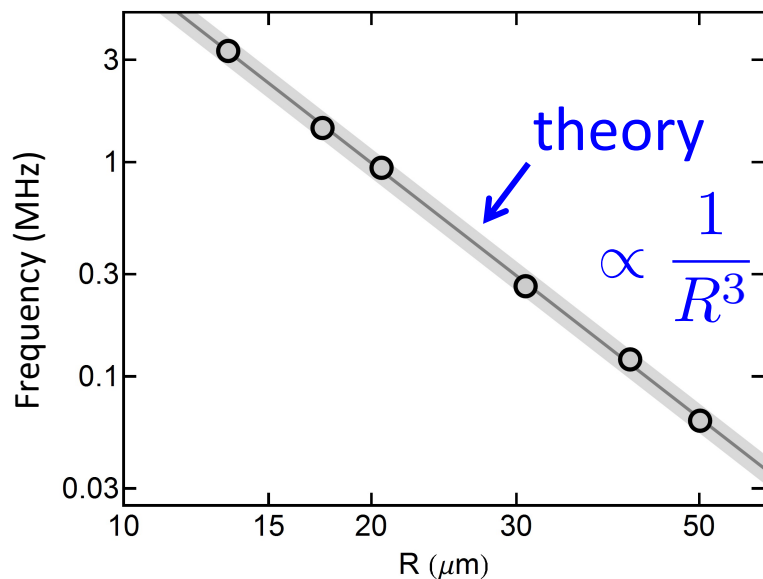
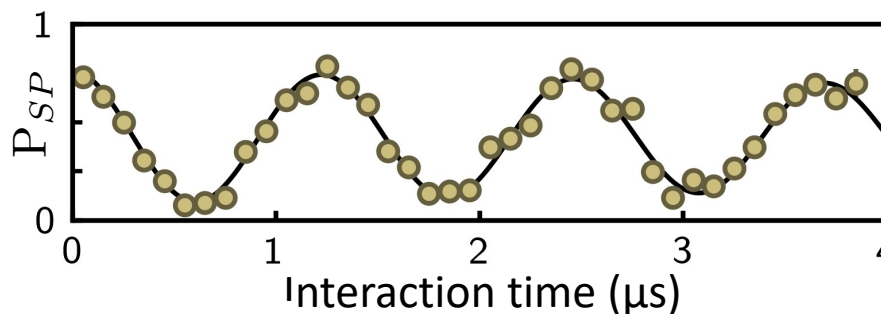
Prepare $|\uparrow\downarrow\rangle$ using microwaves + addressing beam

$R = 30 \mu\text{m}$



Barredo PRL (2015)
de Léséleuc, PRL (2017)

Frequency: $\frac{2C_3}{R^3}$



Thickness:

Paper sheet $\sim 100 \mu\text{m}$

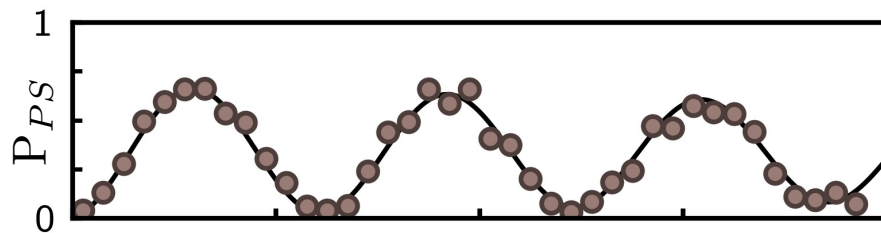
Hair $\sim 50 - 100 \mu\text{m}$

Observation of resonant dip.-dip. interaction with 2 atoms

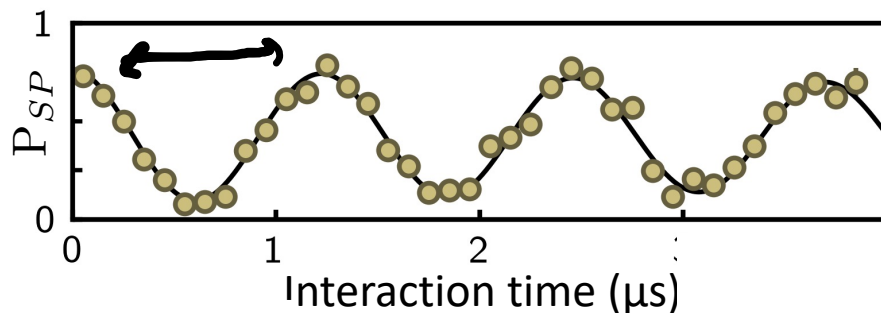
Prepare $|\uparrow\downarrow\rangle$ using microwaves + addressing beam

$R = 30 \mu\text{m}$

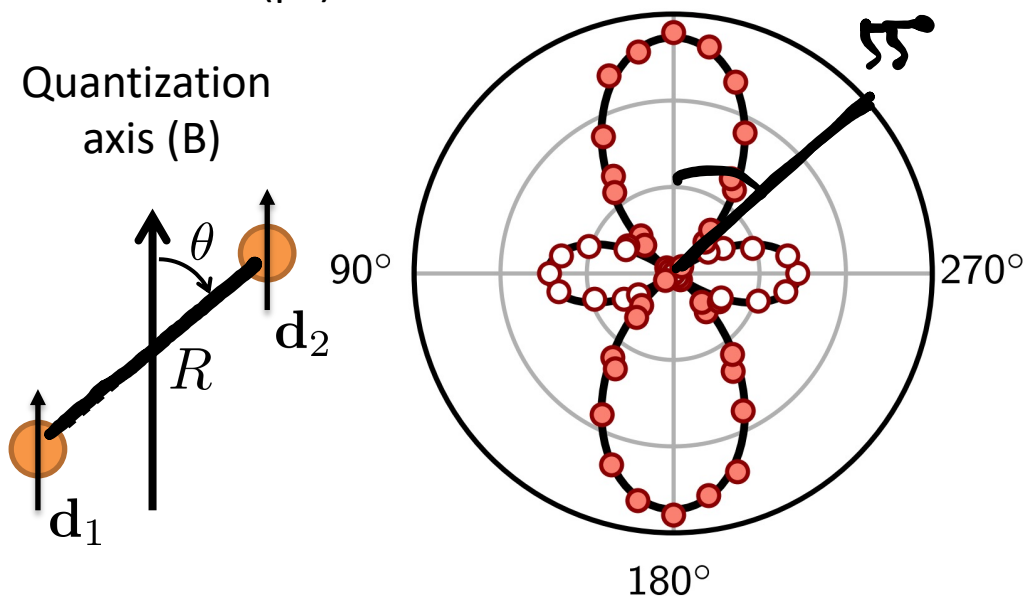
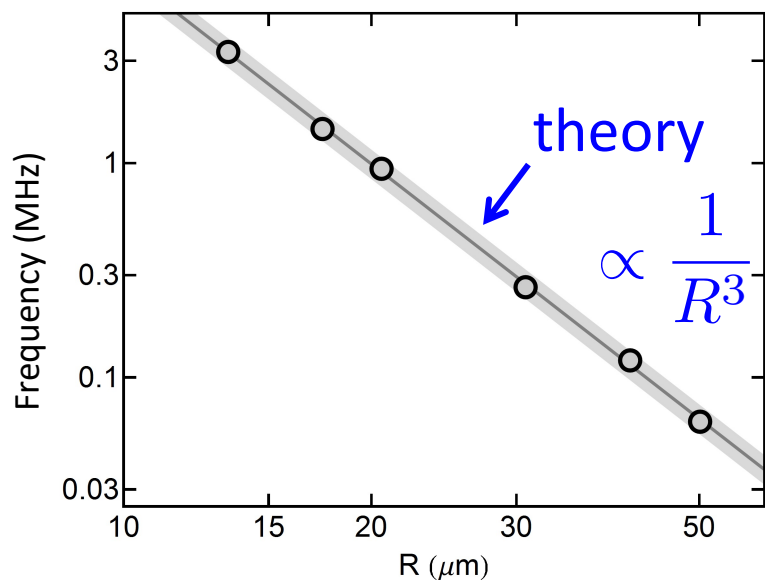
Frequency: $\frac{2C_3}{R^3}$



Barredo PRL (2015)
de Léséleuc, PRL (2017)



$C_3(\theta) \propto 1 - 3 \cos^2 \theta$

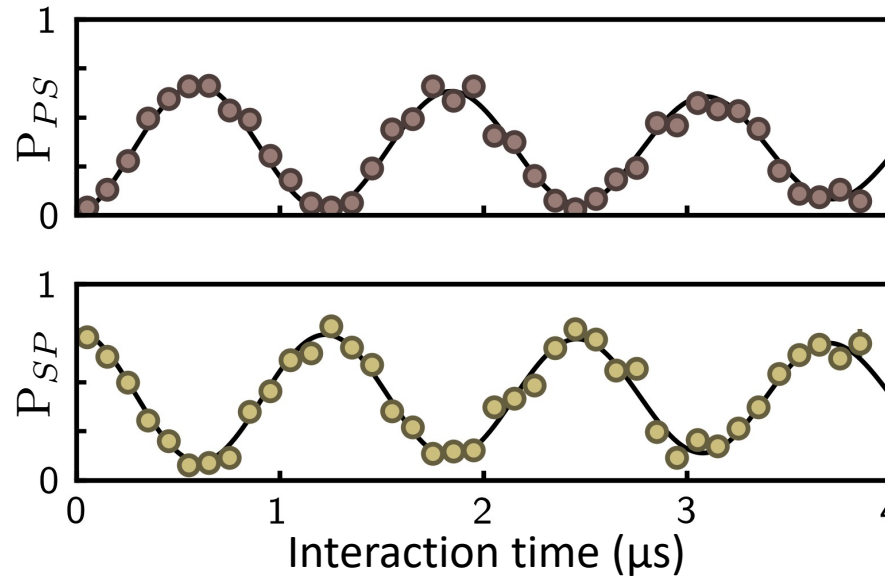


Observation of resonant dip.-dip. interaction with 2 atoms

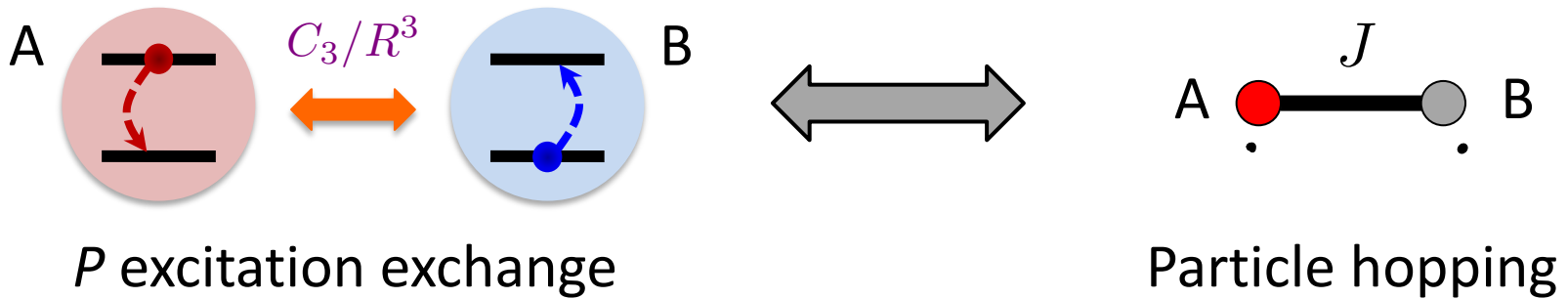
Prepare $|\uparrow\downarrow\rangle$ using microwaves + addressing beam

$R = 30 \mu\text{m}$

Frequency: $\frac{2C_3}{R^3}$

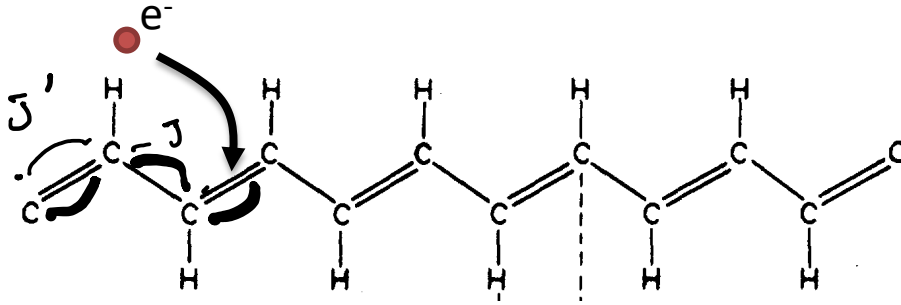


Barredo PRL (2015)
de Léséleuc, PRL (2017)



$$J|A\rangle\langle B|$$

The Su-Schrieffer-Heeger model

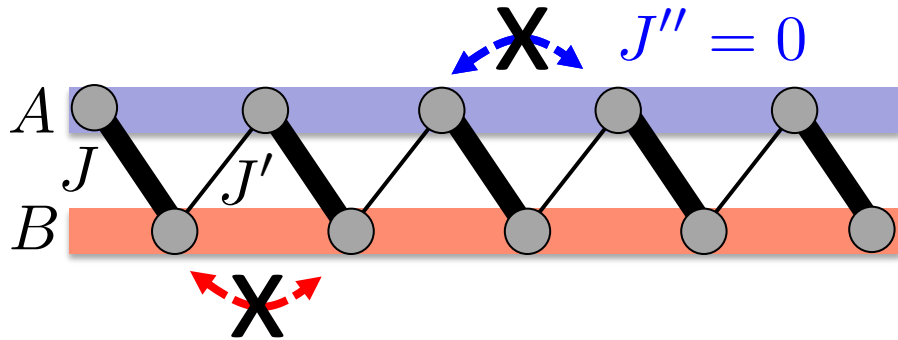


Electronic transport in
polyacetylene

PRL **42**, 1698 (1979)

Now, considered as simplest example of **topological** model

The Su-Schrieffer-Heeger model

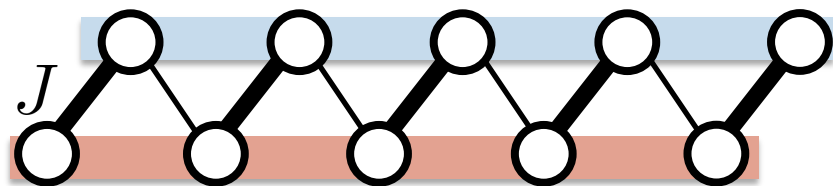


Model: tight-binding
dimerization: $J > J'$

Sub-lattice symmetry \Rightarrow symmetric **single particle** spectrum

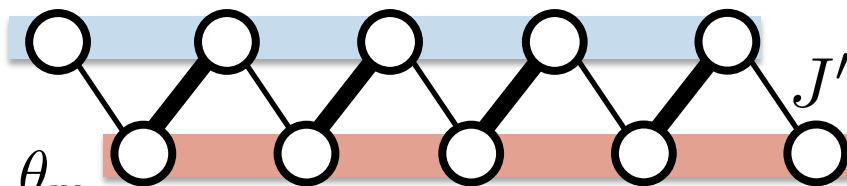
Implementation of SSH spin chain with Rydberg atoms

Science **365**, 775 (2019)



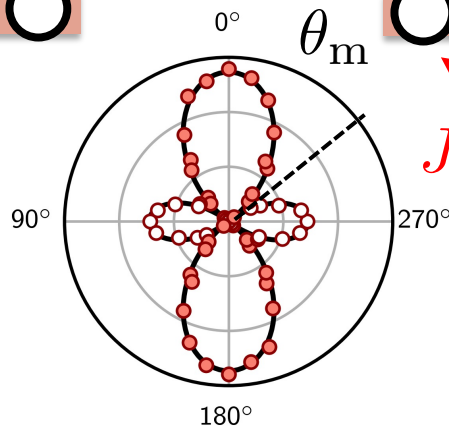
$$J''' = 0$$

Normal



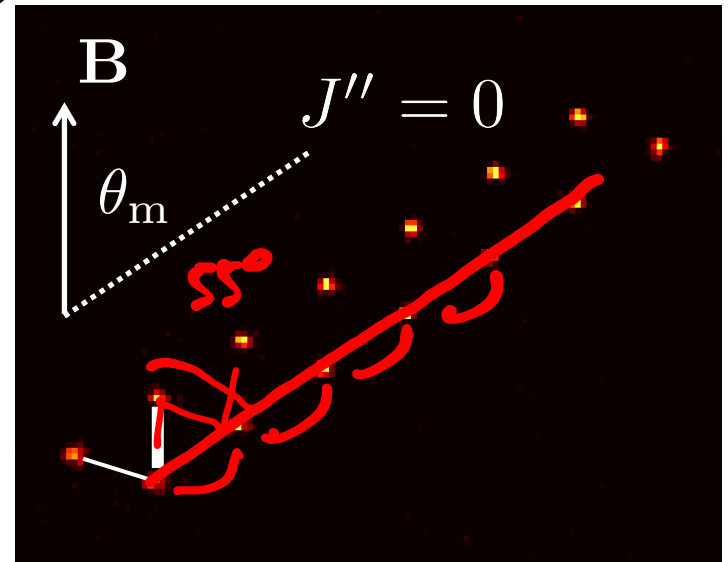
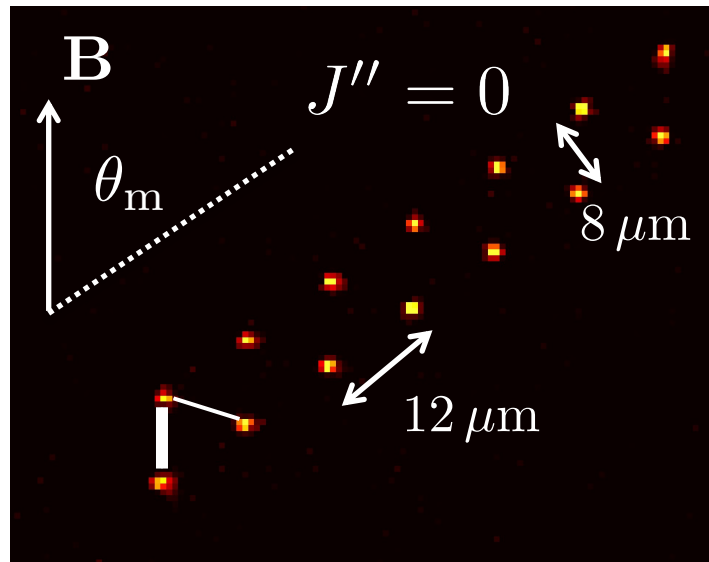
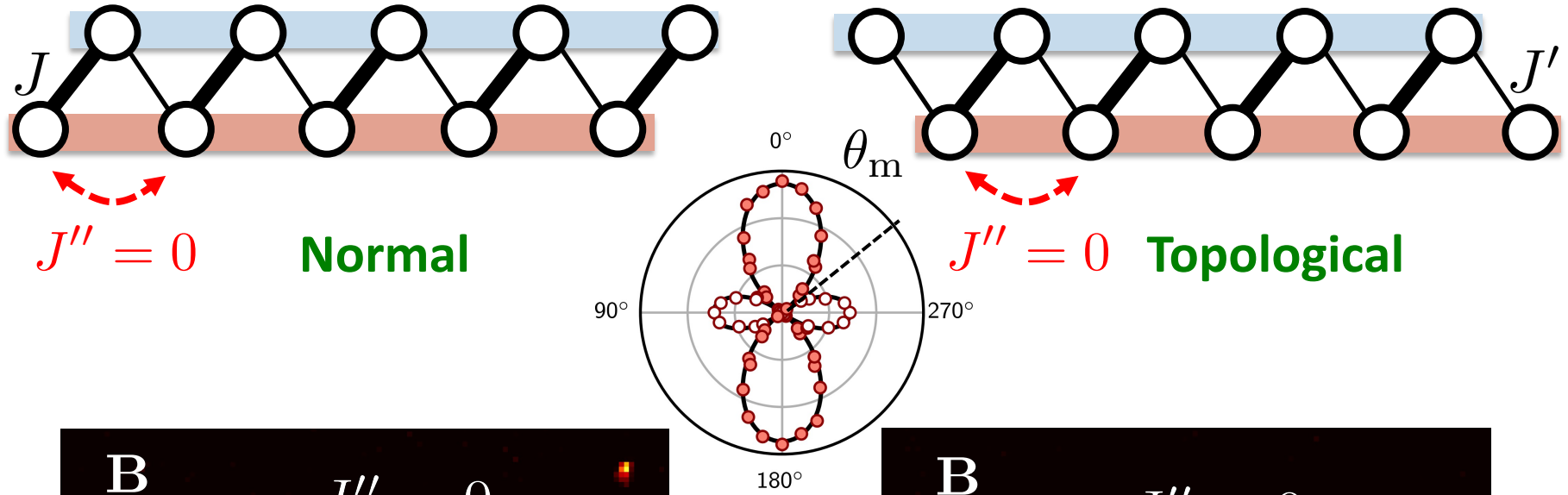
$$J''' = 0$$

Topological



Implementation of SSH spin chain with Rydberg atoms

Science **365**, 775 (2019)



$$J/h = 2.4 \text{ MHz} \quad J'/h = -0.9 \text{ MHz}$$

Conclusion

Rydberg interactions are strong & controllable

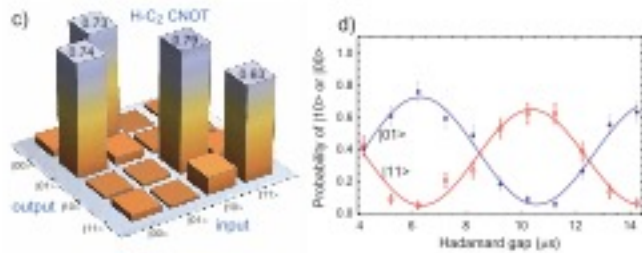
1. Resonant interaction
2. Van der Waals

$$R = 10 \mu\text{m} \Rightarrow V_{\text{int}}/h \sim 1 - 10 \text{ MHz}$$
$$\Rightarrow \text{timescales} < \mu\text{sec}$$

Control over interaction useful for many-body physics & quantum simulation

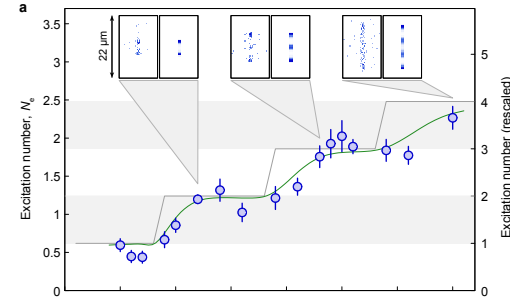
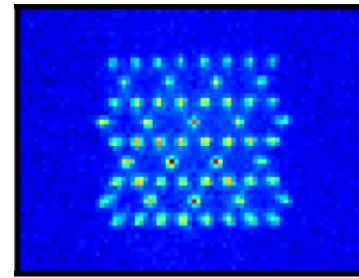
New / other directions: ... a few examples

QIP: entanglement and gates



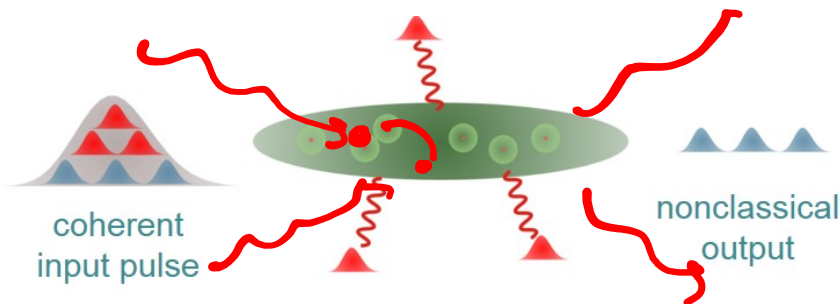
Saffman RMP **82**, 2313 (2010)
Saffman, Biedermann, Lukin...

Many-body physics Quantum simulation



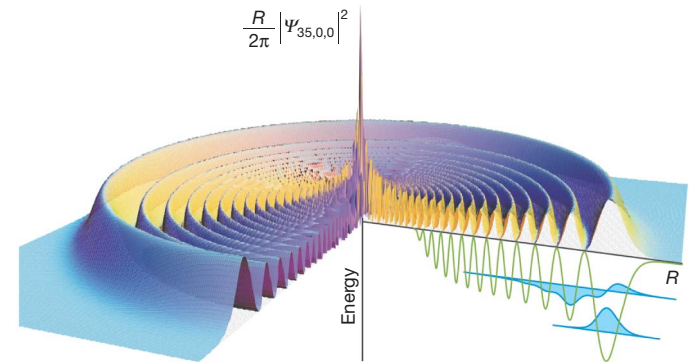
Browaeys, Lukin, Bloch, Pillet, Weidemuller, Morsch...

Non-linear classical & quantum optics



Adams, Hofferbert, Firstenberg, Lukin, Vuletic...

Exotic long-range molecules



Pfau-Löw, Ott, Shaeffer ...

Platform mature enough to envision applications...

Startups recently created to develop industry graded simulators



Applications: scientific computing, optimization in finance and industry...

