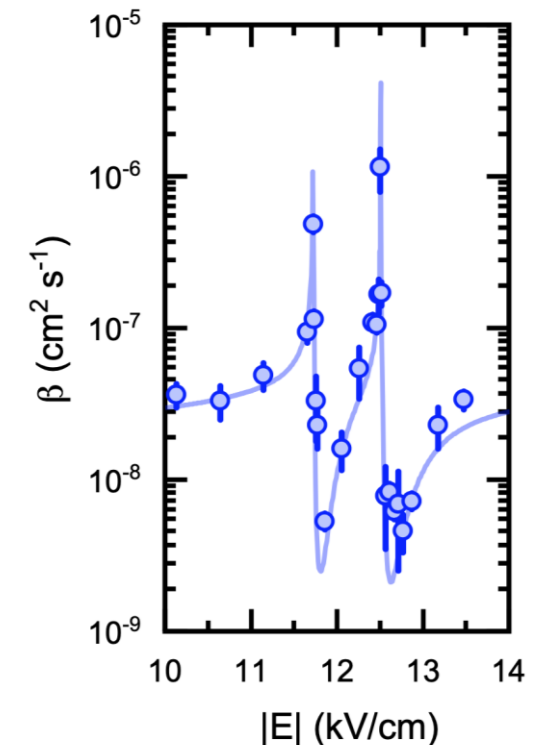
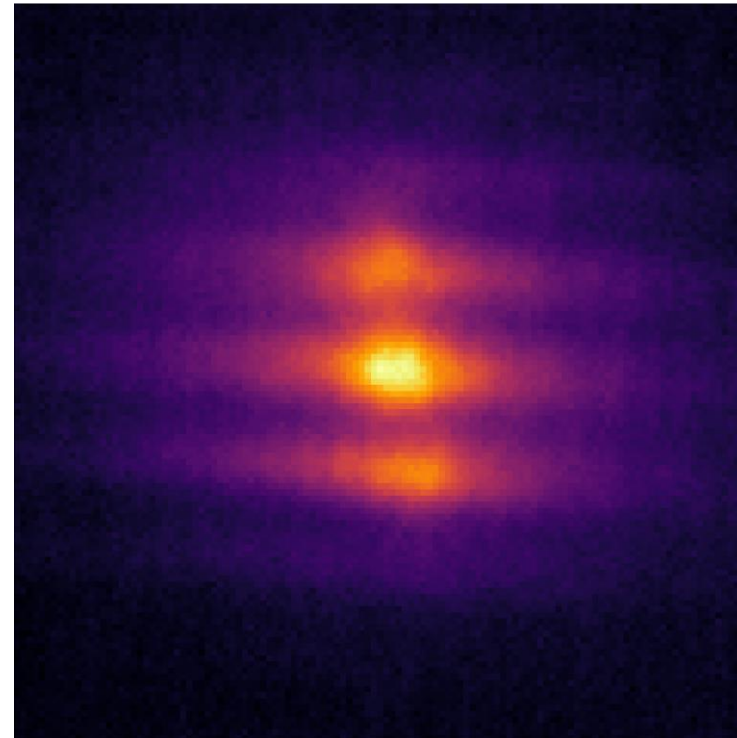
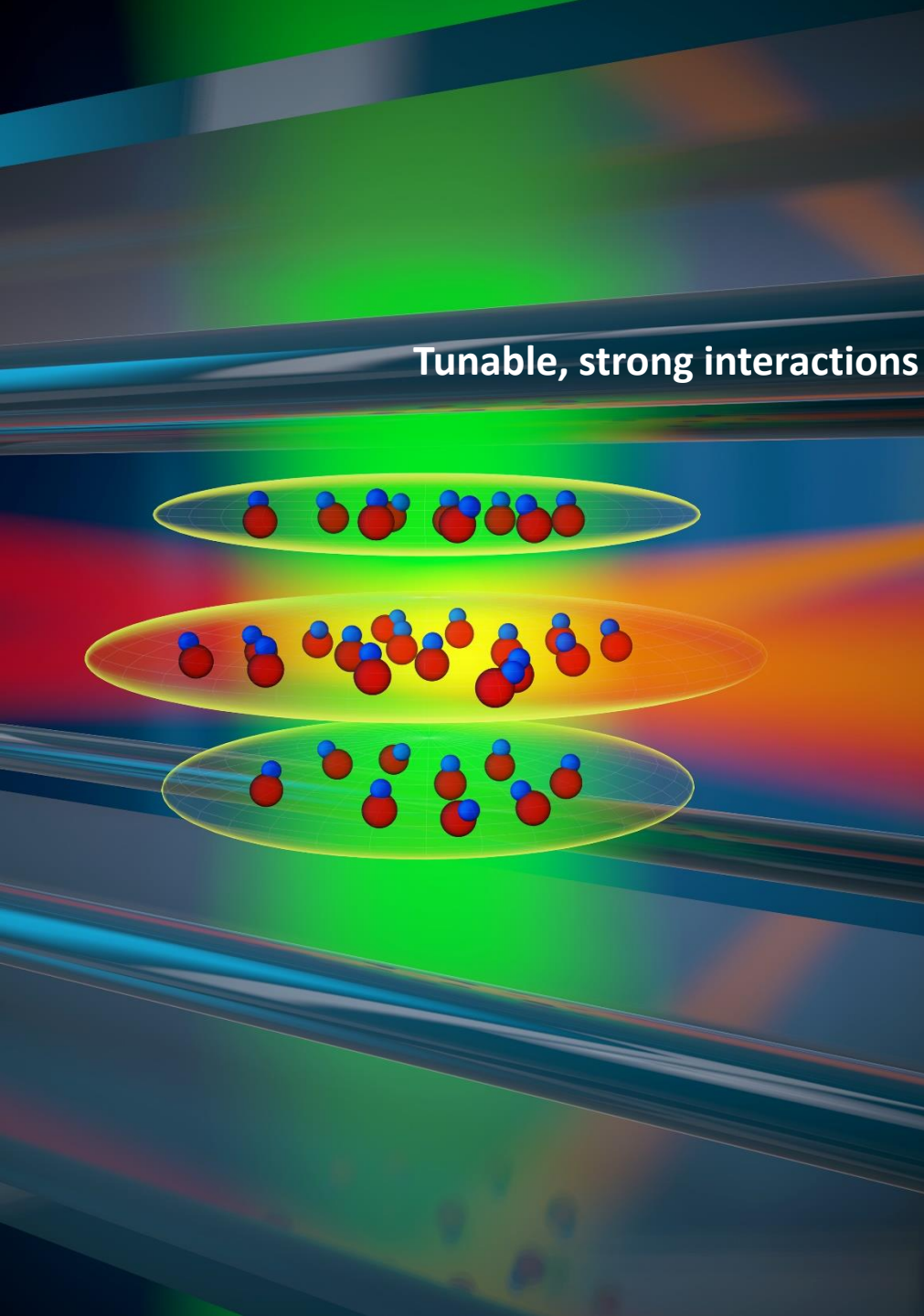


Quantum gas of molecules

Jun Ye

2021 Boulder Summer School for
Condensed Matter and Materials Physics

July 5, 2021



Ultracold Atomic Matter

Precise control of quantum systems

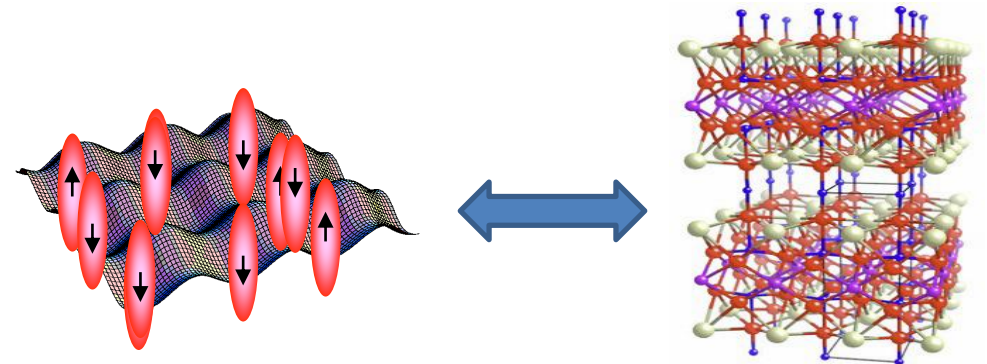
- Clocks, quantum information, sensors

Probe complexities & strong correlations

- Superconductivity & Superfluidity
- Quantum magnetism
- Quantum chemistry

Universality & scaling

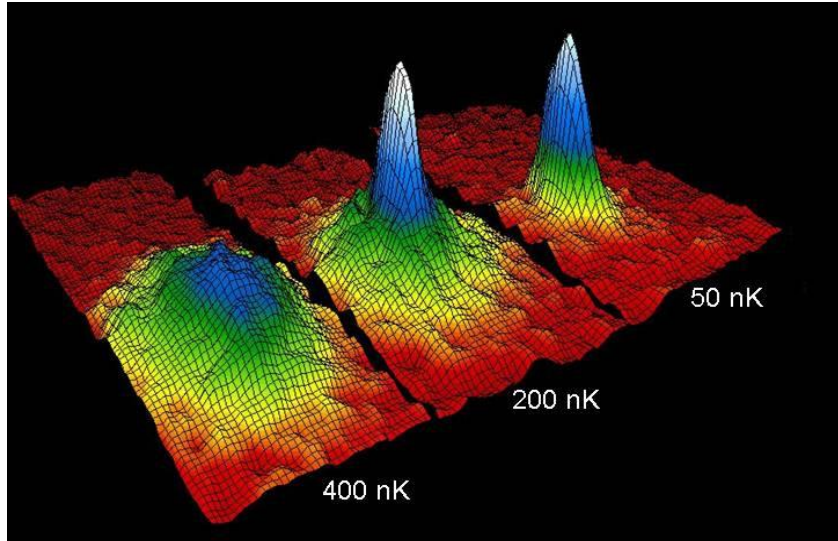
- Range of interactions
- Few to many-body



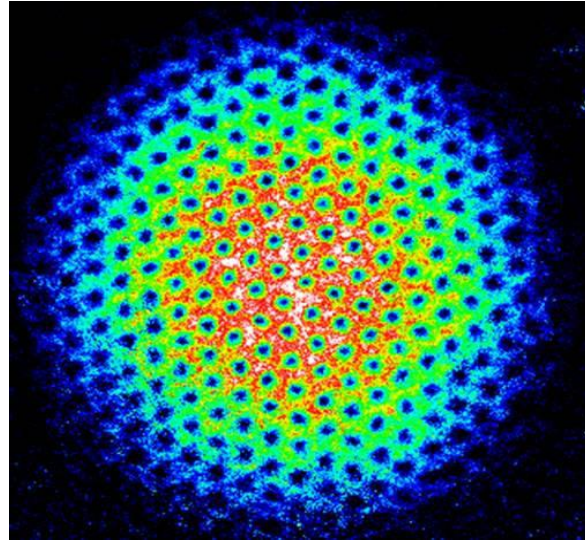
Atoms $\leftrightarrow$ Electrons

Optical lattice $\leftrightarrow$ Ionic Crystal

Quantum atomic gases



Bose-Einstein condensate



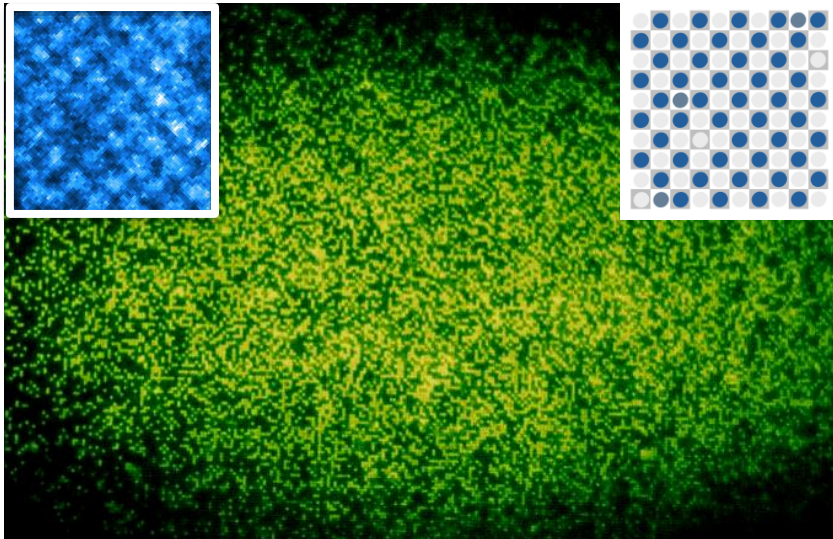
Superfluidity

$$T = 100 \text{ nK}$$

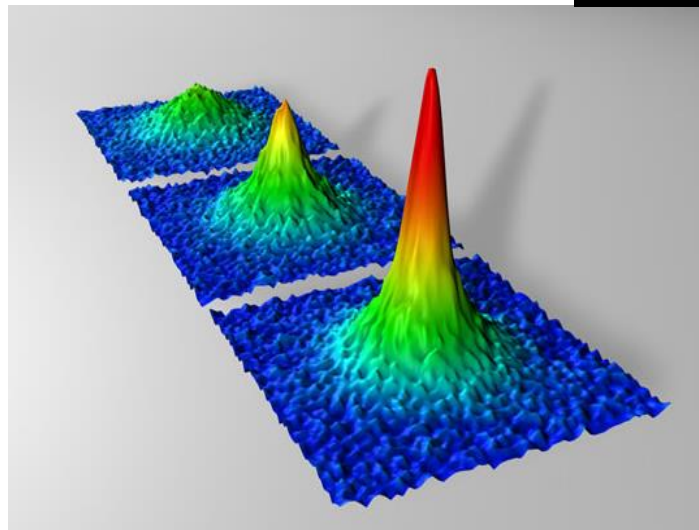
$$N = 10^6 \text{ atoms}$$

$$n = 10^{13} \text{ cm}^{-3}$$

Control atomic interaction
Control atomic motion



Magnetic ordering, transport

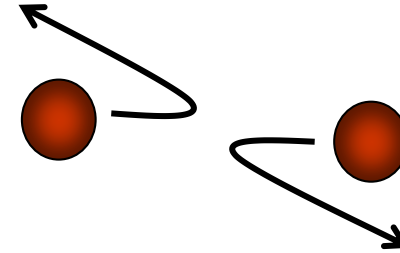


Fermi superfluidity

Why cold molecules?

- **Atoms:**

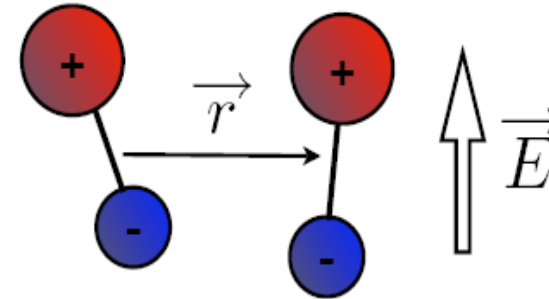
contact interaction
isotropic



- **Polar molecules:**

dipole-dipole interaction

tunable
strong
long-range
anisotropic

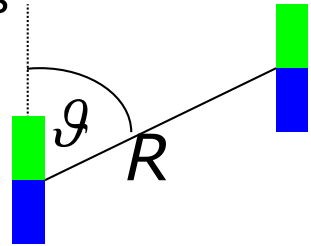


$$\frac{d^2}{r^3} (1 - 3 \cos^2 \theta)$$

Dipolar quantum systems

- Strongly correlated quantum material
- Dynamics with tunable, long-range interactions

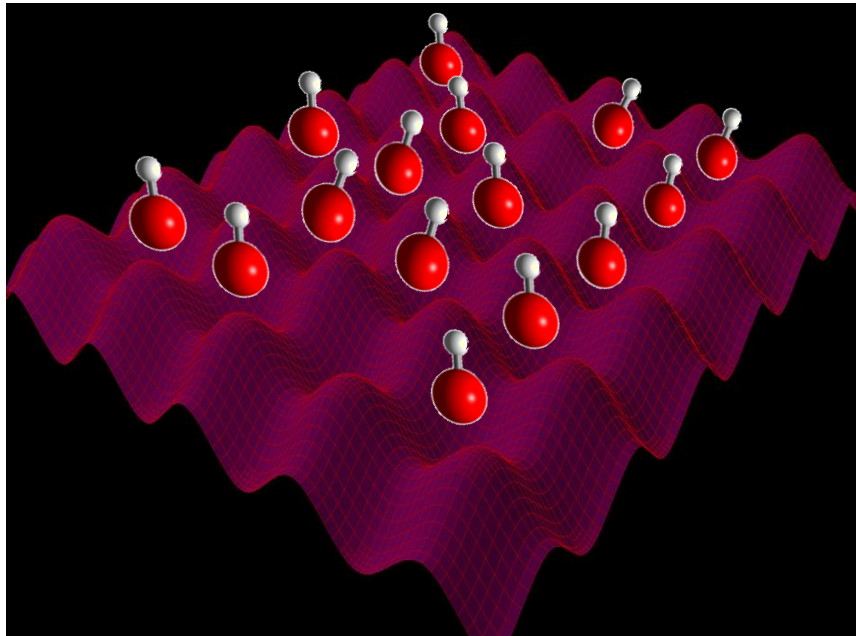
Atomic magnetic
dipoles



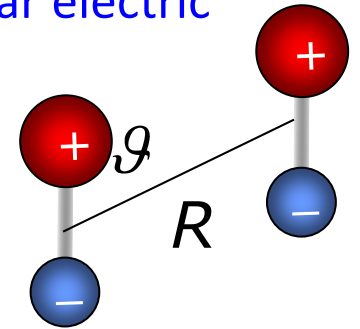
$$\frac{(\text{Debye})^2}{(\text{Bohr magneton})^2} \cdot c^2 = 10^4$$

Tunable by angle & strength (E)

Stuttgart, Stanford, Innsbruck, Florence, Paris, ...



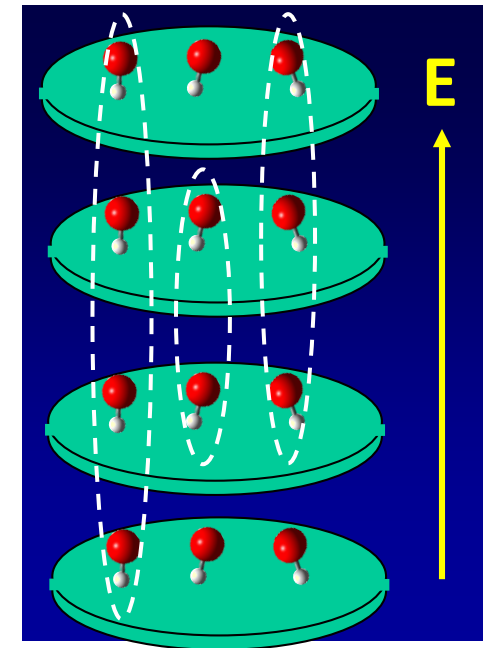
Molecular electric
dipoles



Quantum
metrology,

Quantum
information

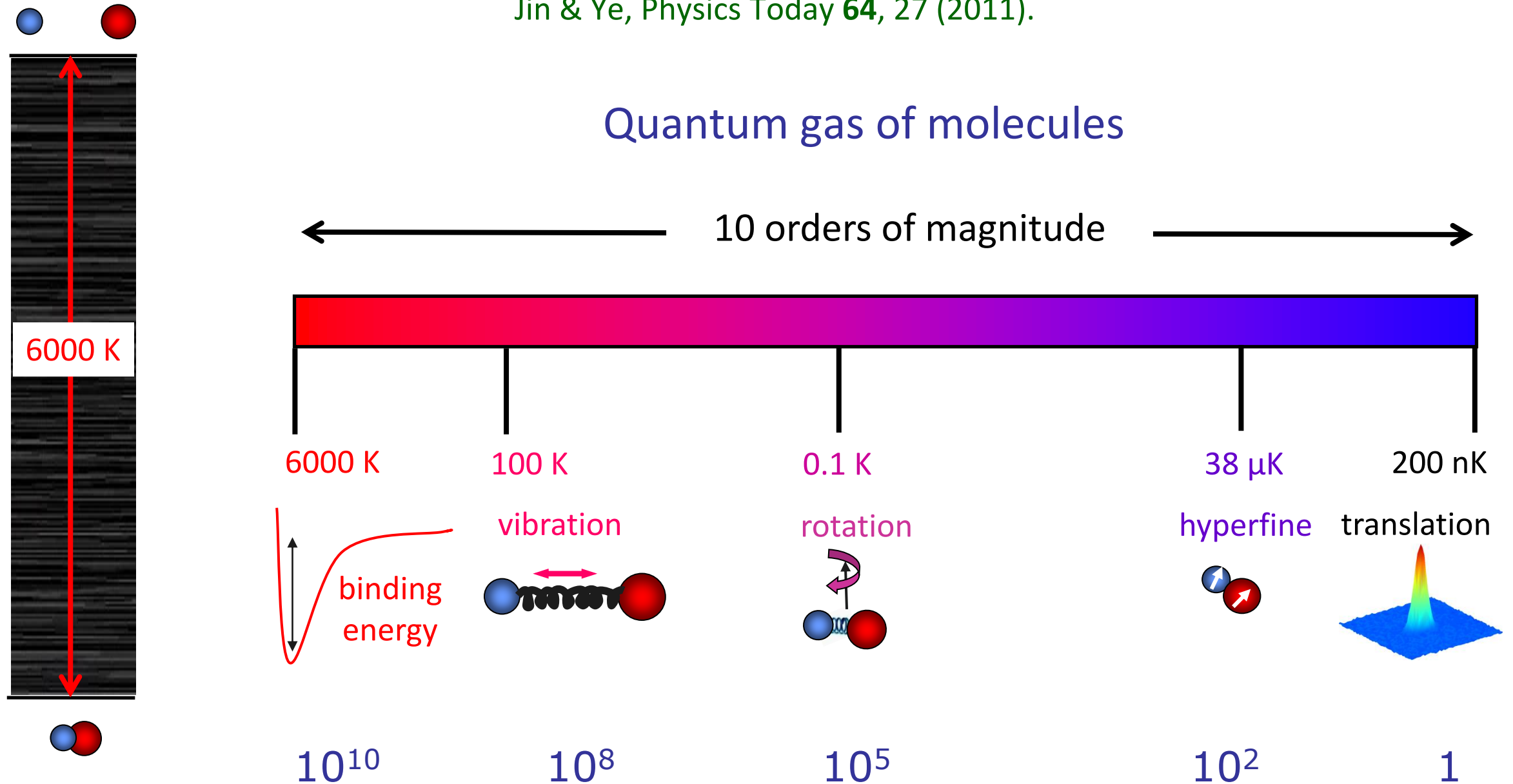
Chemistry



Molecules are complex

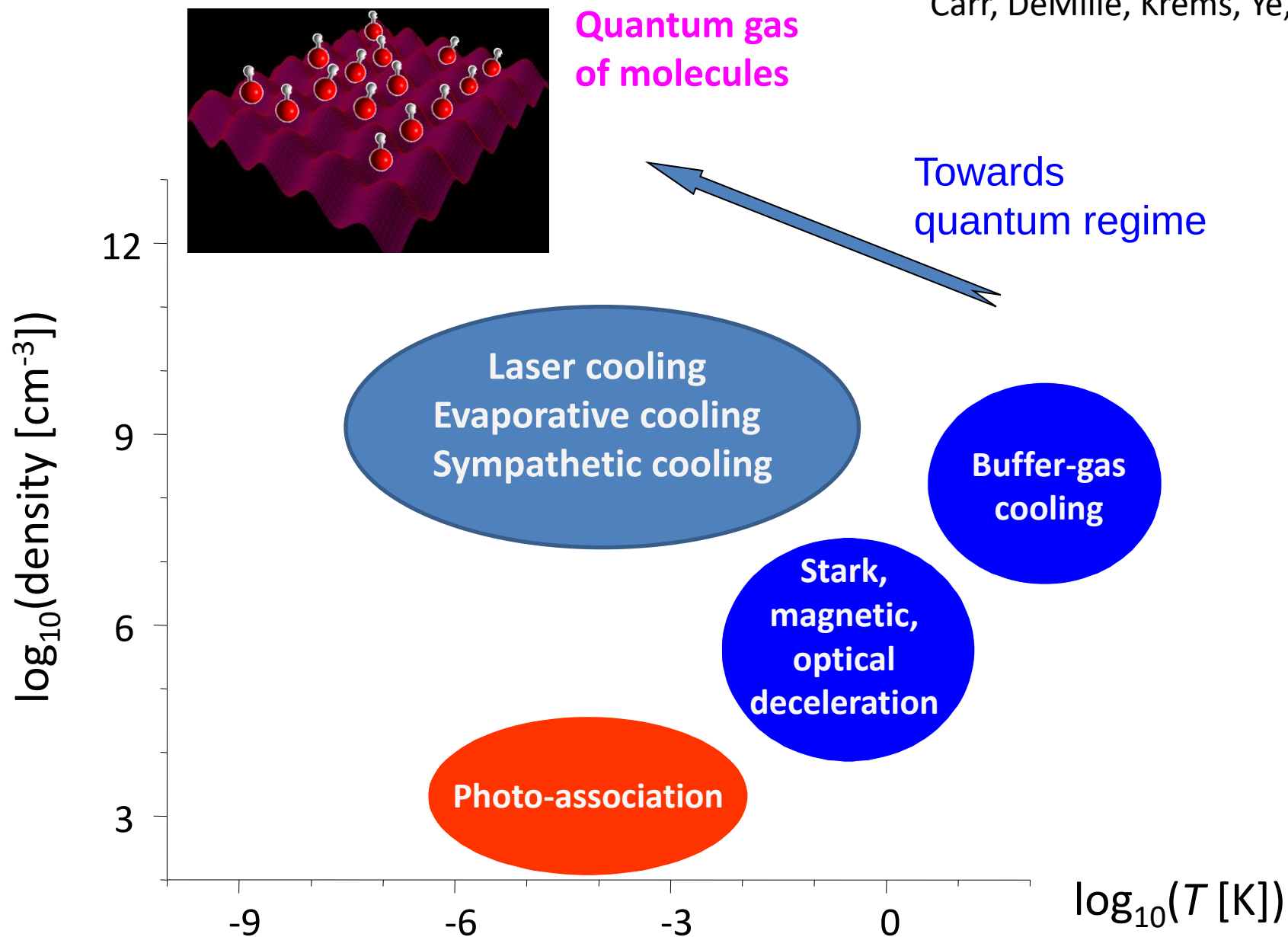
Jin & Ye, Physics Today **64**, 27 (2011).

Quantum gas of molecules



Technology for making cold molecules

Carr, DeMille, Krems, Ye, New. J. Phys. 2009.

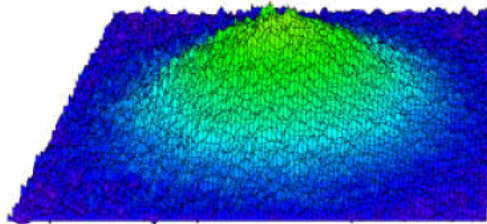


Ultracold polar molecules

Ni, Ospelkaus, de Miranda, Pe'er, Neyenhuis, Zirbel, Kotochigova, Julienne, Jin, & Ye,
Science **322**, 231 (2008).

Innsbruck, Durham, MIT, Hong Kong, USTC, MPQ, Harvard, Singapore, ...

^{40}K Fermions



Temperature ~ 200 nK

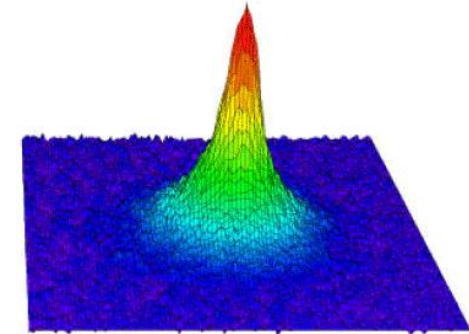
Density $\sim 10^{12}/\text{cm}^3$

$T/T_F \sim 1.4$

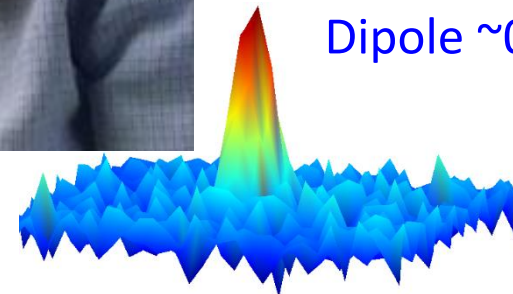
Deborah Jin
(1968 – 2016)



^{87}Rb Bosons



KRb molecules
Dipole ~ 0.5 Debye



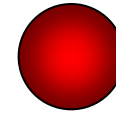
Feshbach molecules

Start with ultracold atoms.

^{40}K



^{87}Rb



Control the interaction

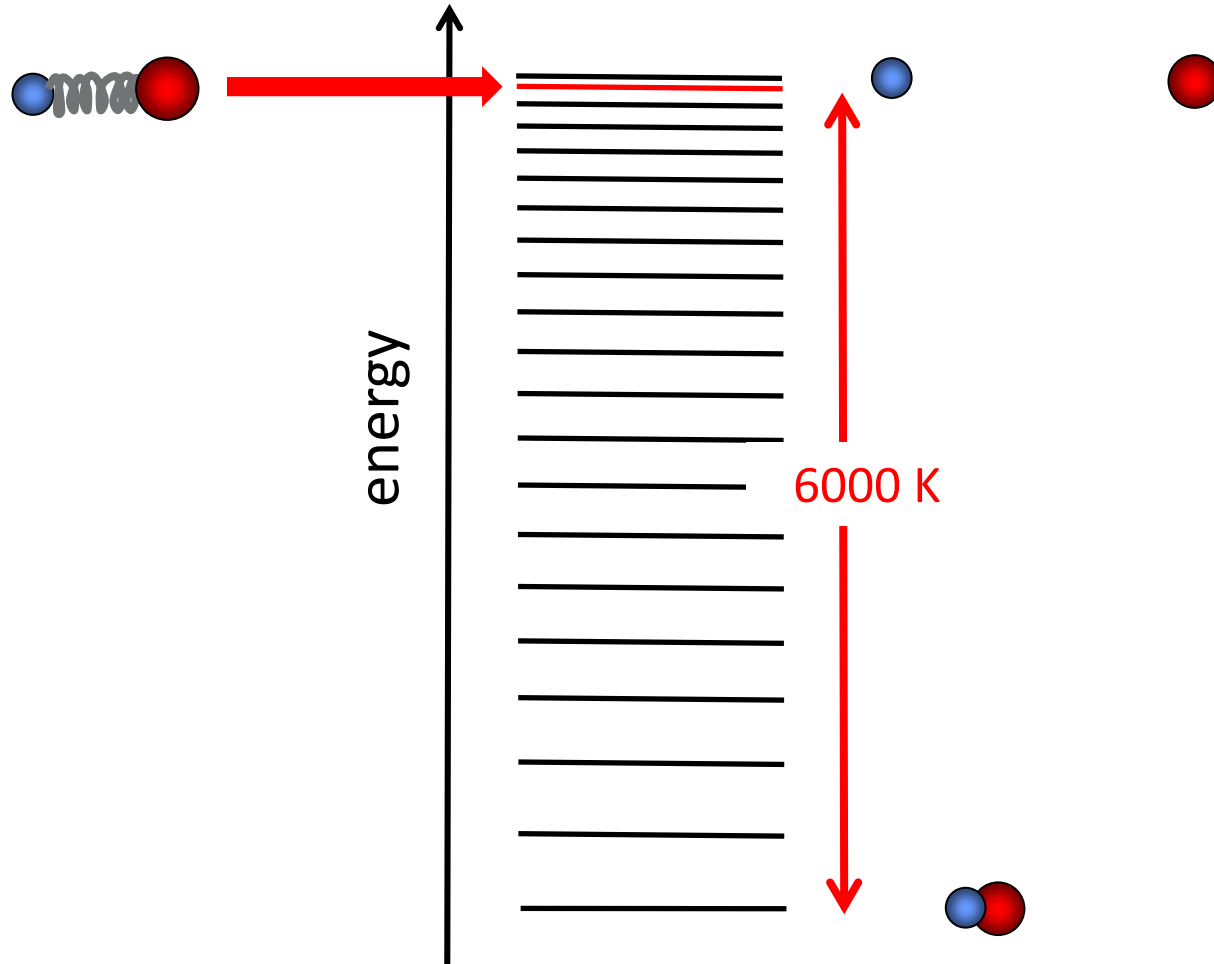


Make large, floppy molecules

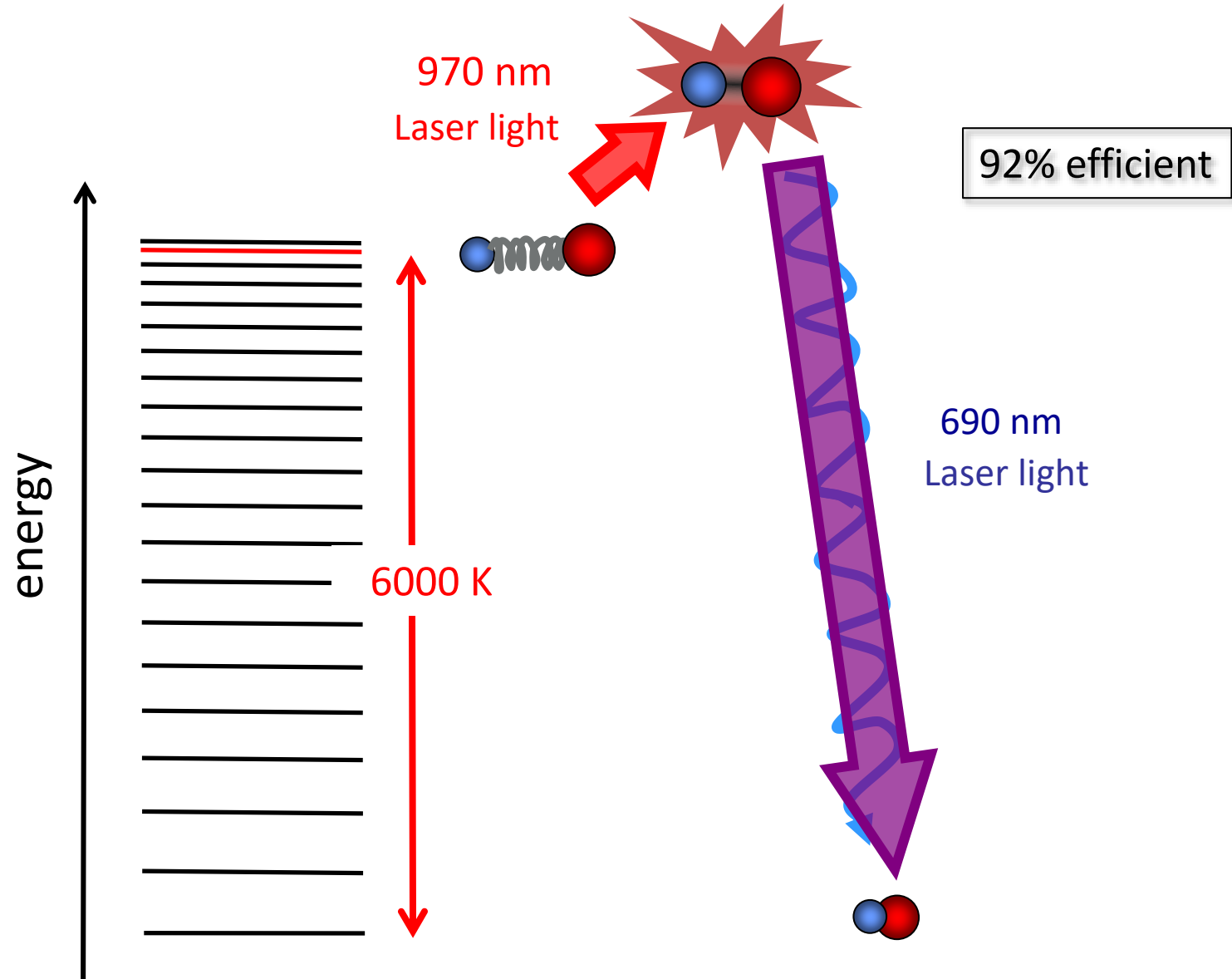
Weakly bound molecules

Zirbel et al., PRL **100**, 143201 (2008).

- no dipole moment
- losses

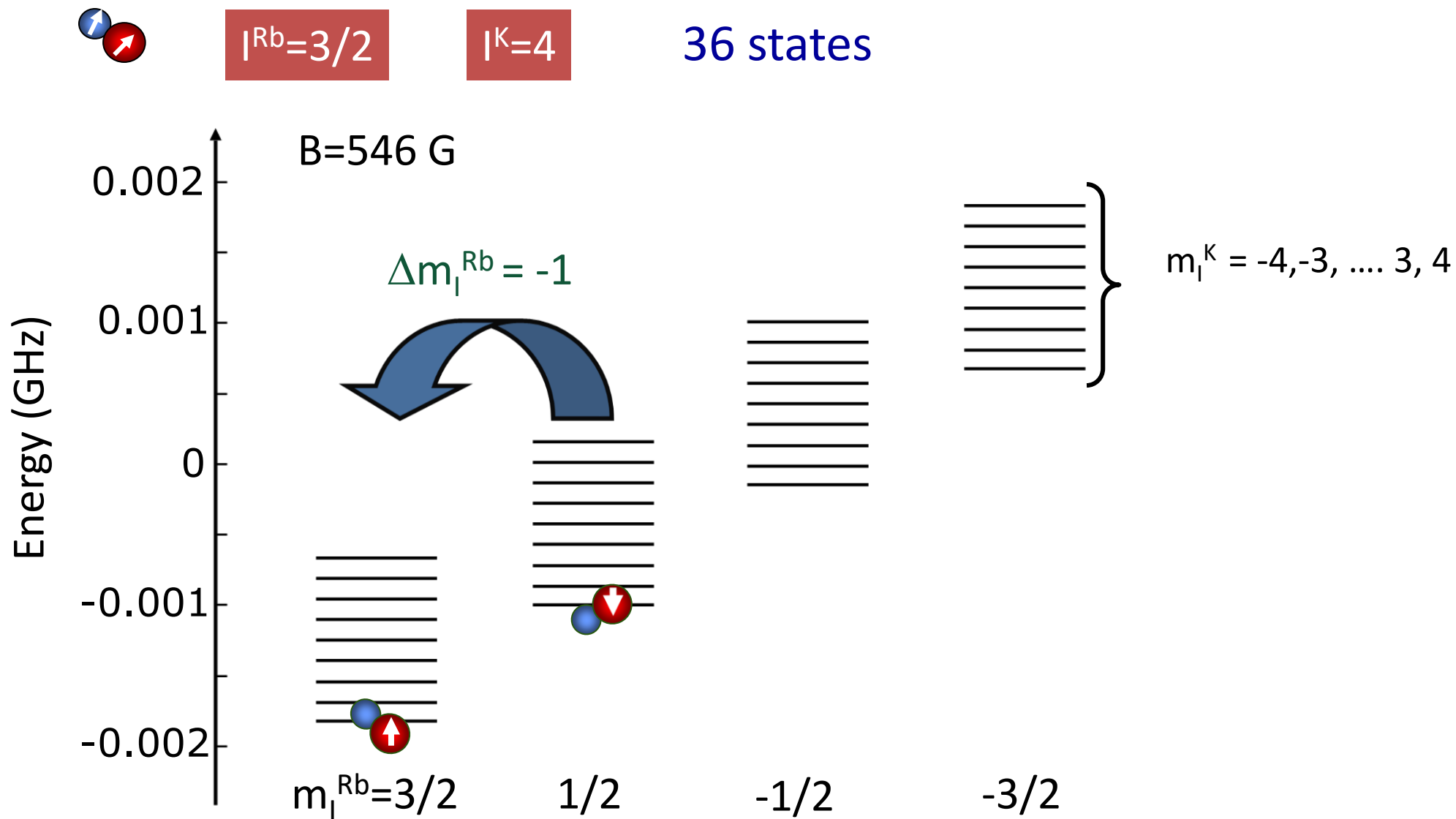


Transfer the molecules to the ground state



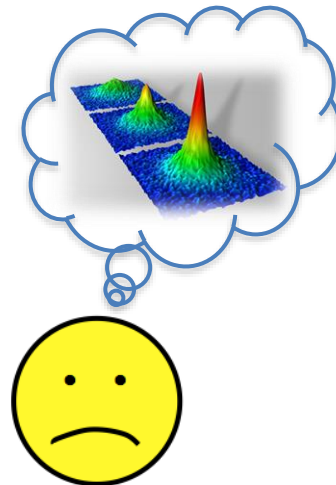
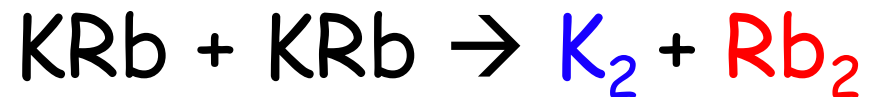
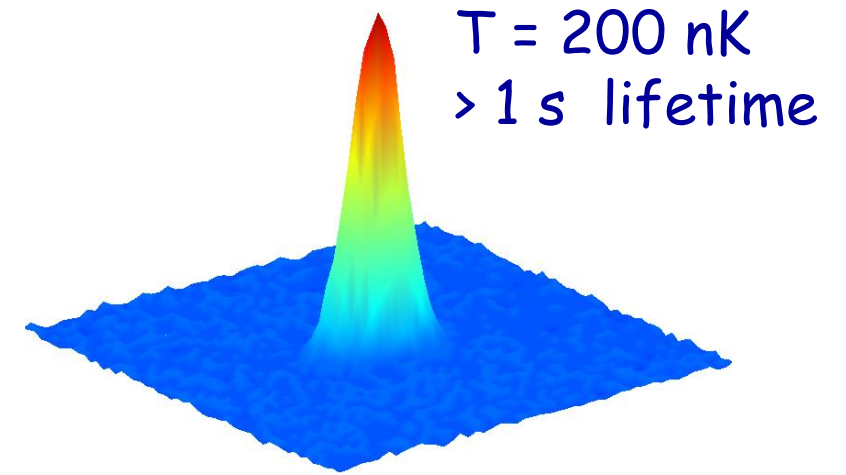
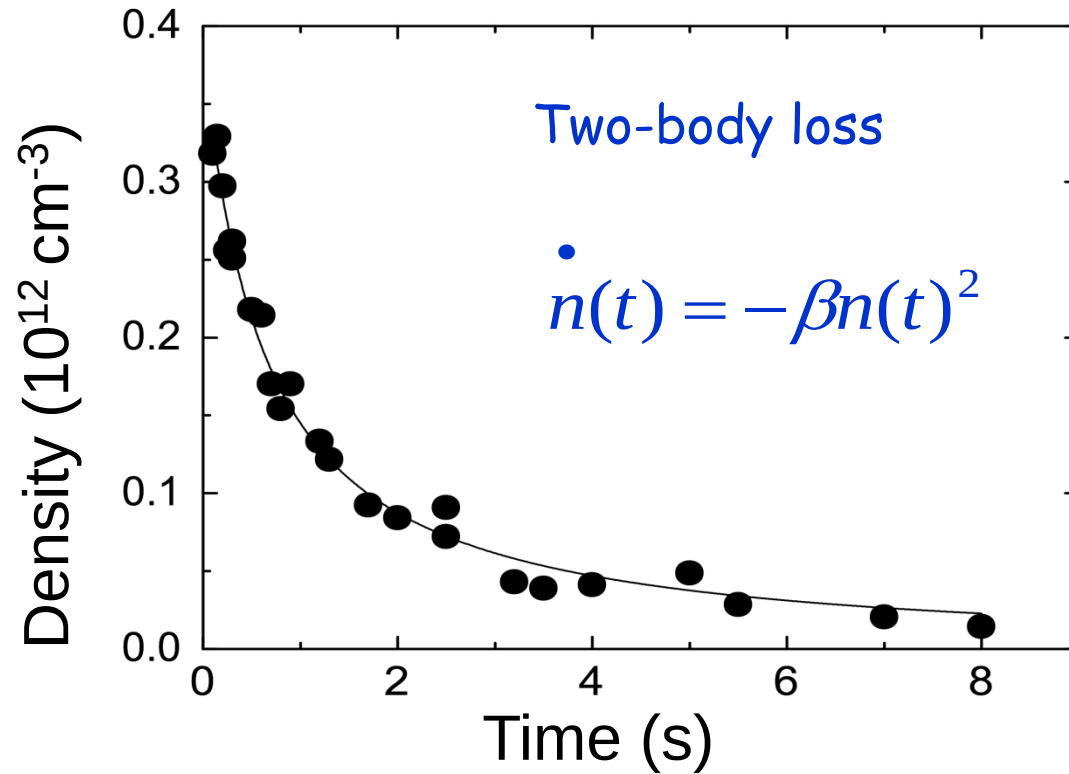
Light carries away the binding energy (& preserves the entropy)

Hyperfine structure for $^1\Sigma$ ($v=0, N=0$)



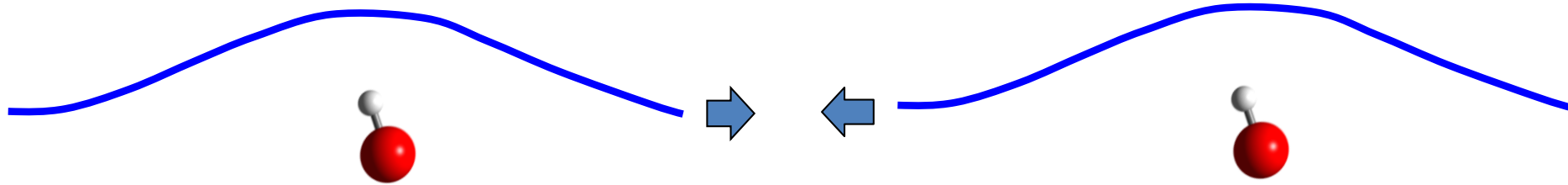
Chemistry near absolute zero

Molecules in the lowest energy state
(electronic, vibrational, rotational, hyperfine)

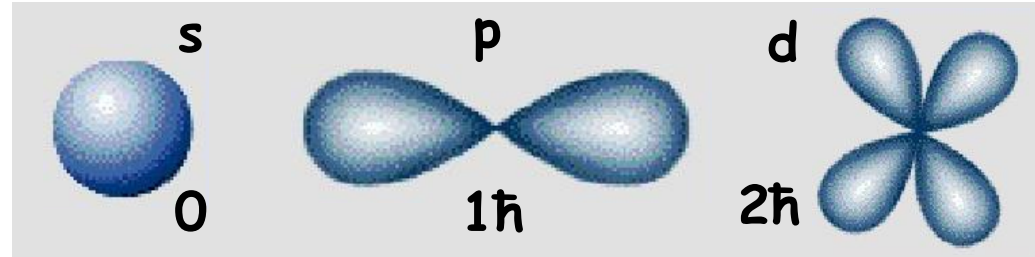
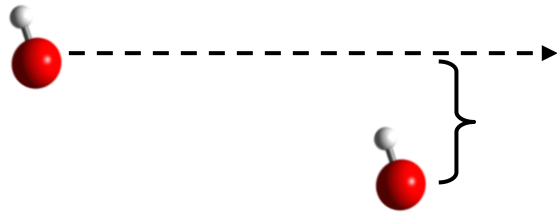


Cold collisions between identical Fermions

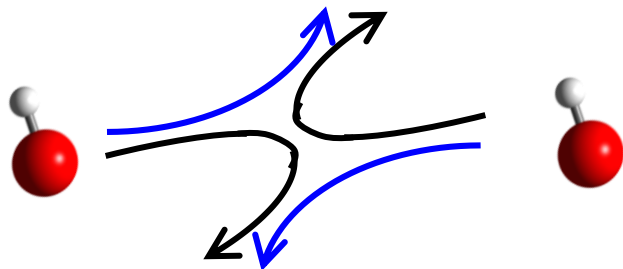
(1) Particles behave like waves



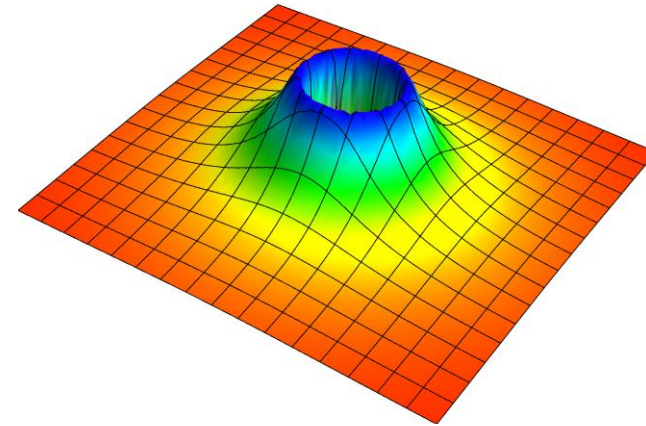
(2) Angular momentum is quantized



(3) Quantum statistics matter

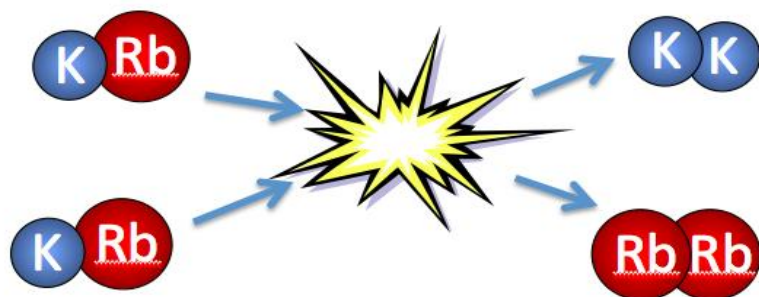


$$|\psi_0\rangle|\psi_1\rangle - |\psi_1\rangle|\psi_0\rangle$$



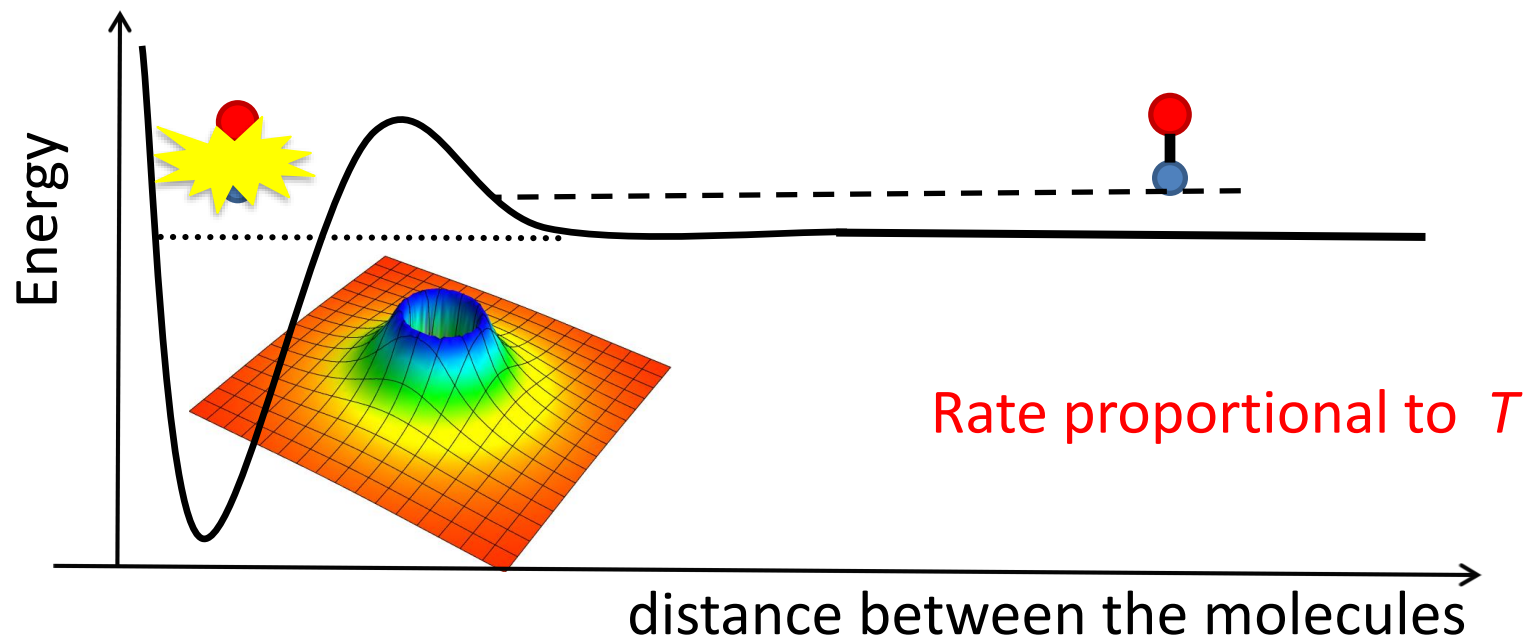
Fermions $\Rightarrow L = 1$, p -wave collisions

Ultracold quantum chemistry

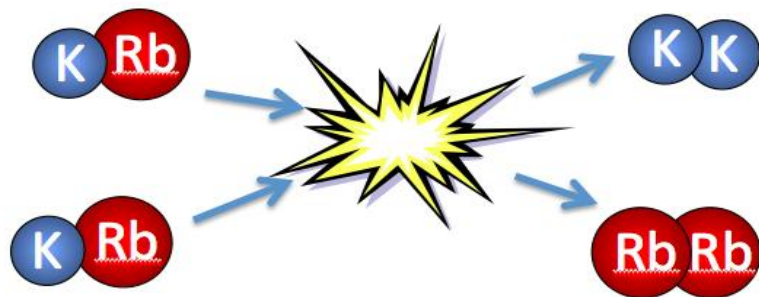


Ospelkaus *et al.*, Science **327**, 853 (2010).

At low T , the quantum statistics of fermionic molecules suppresses chemical reaction!

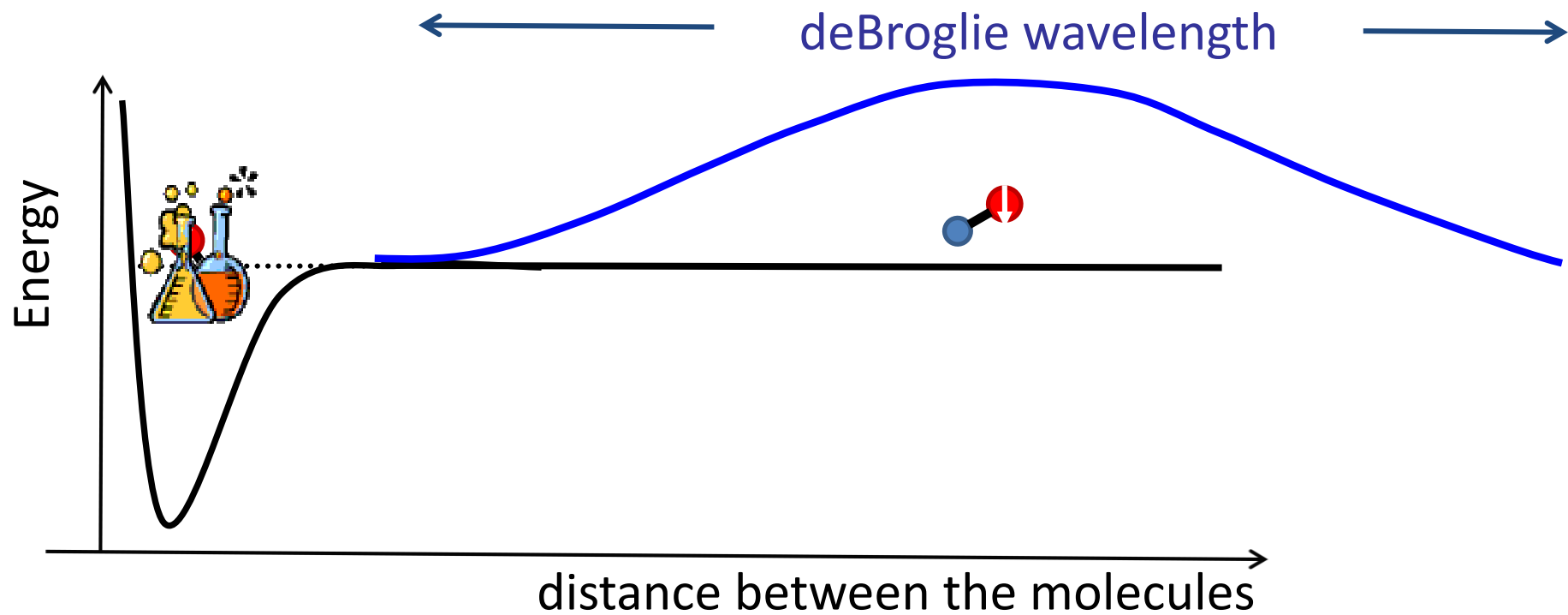


Ultracold quantum chemistry



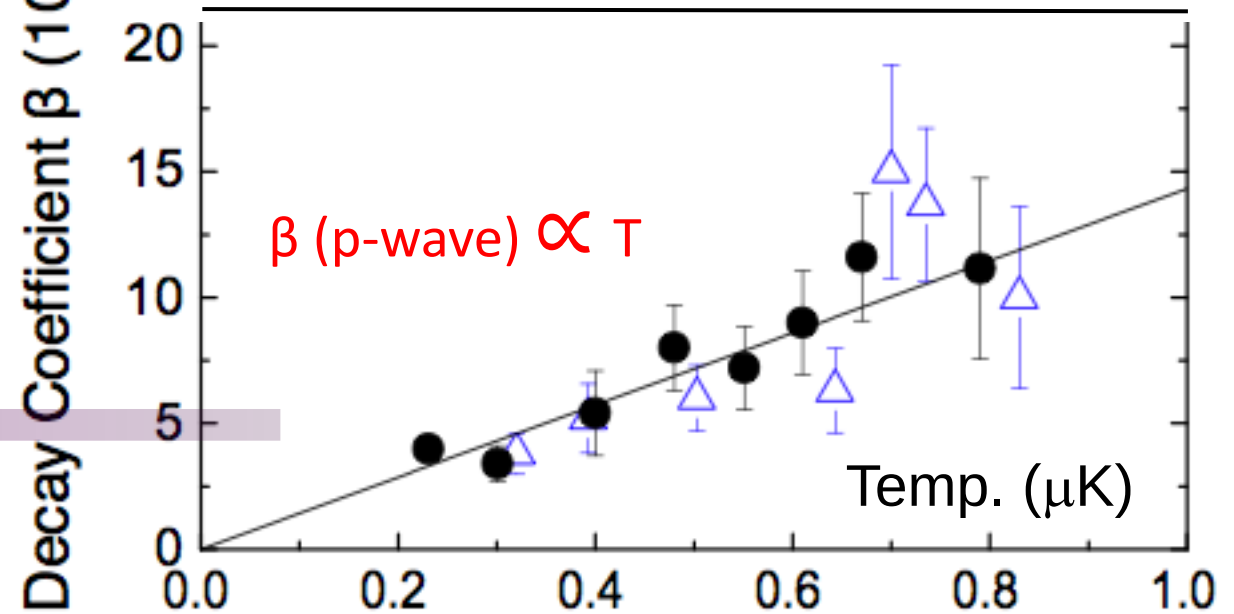
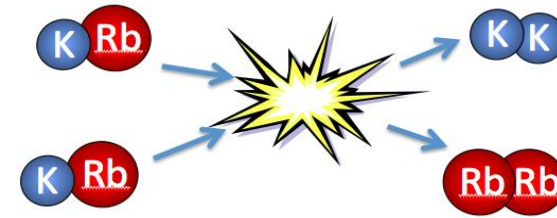
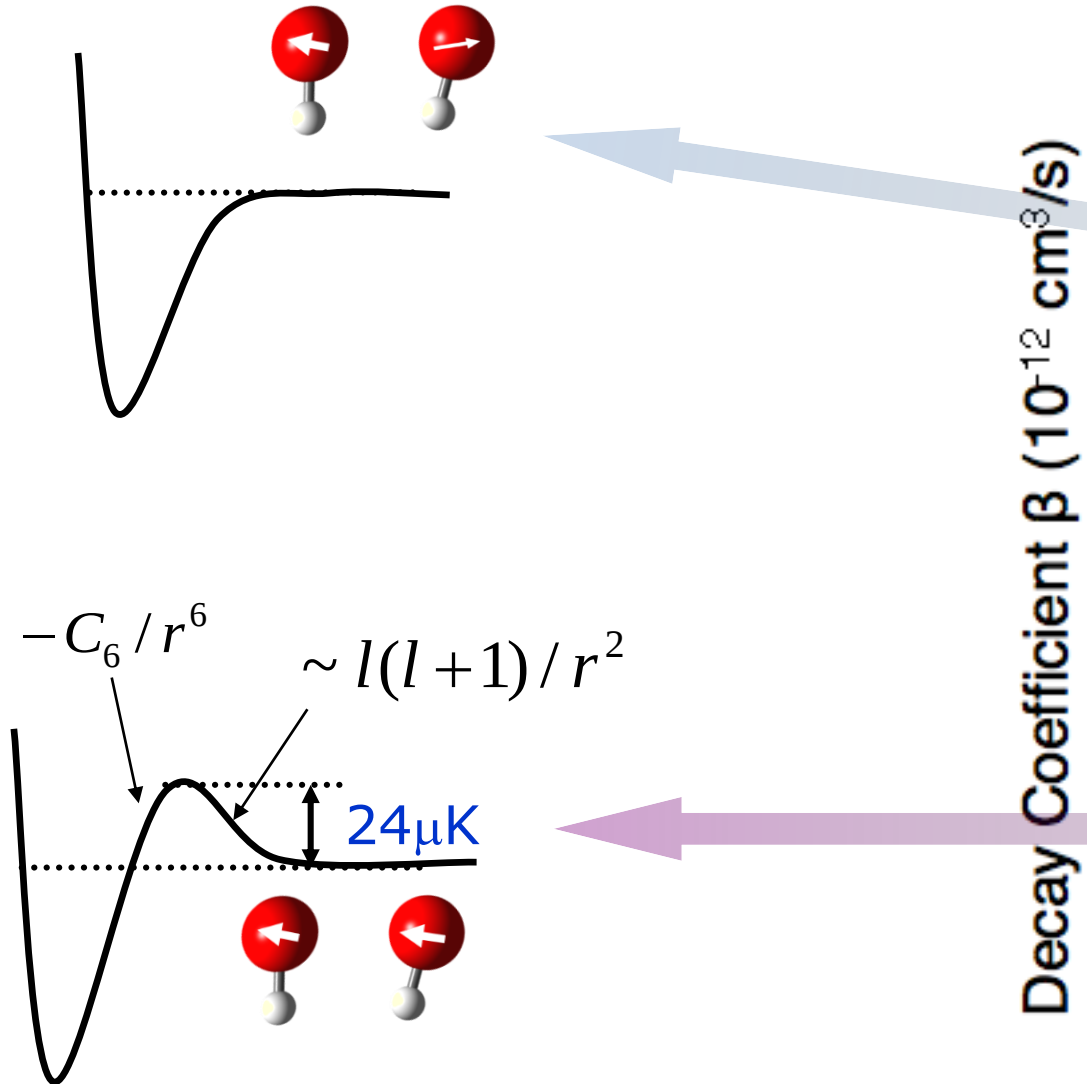
Ospelkaus *et al.*, Science **327**, 853 (2010).

Distinguishable molecules do not enjoy the suppression $\rightarrow$ rate is x 100 higher, independent of T



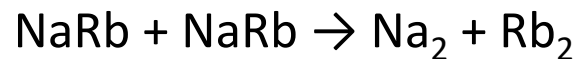
Bimolecular reactions: Wigner threshold law

Ospelkaus *et al.*, Science **327**, 853 (2010).

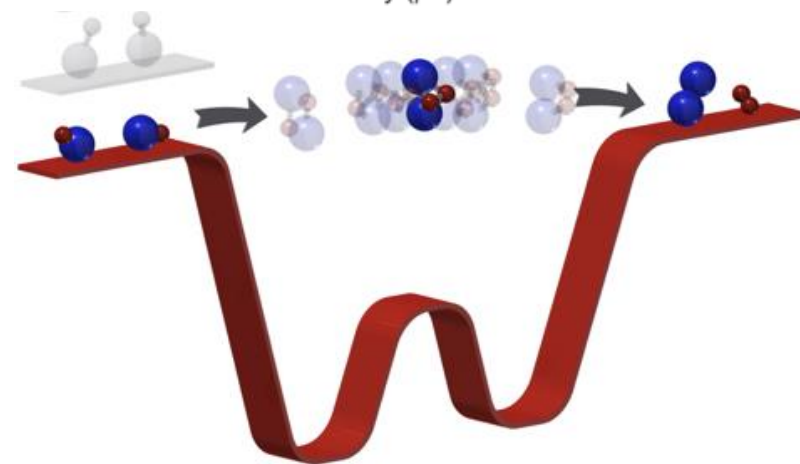
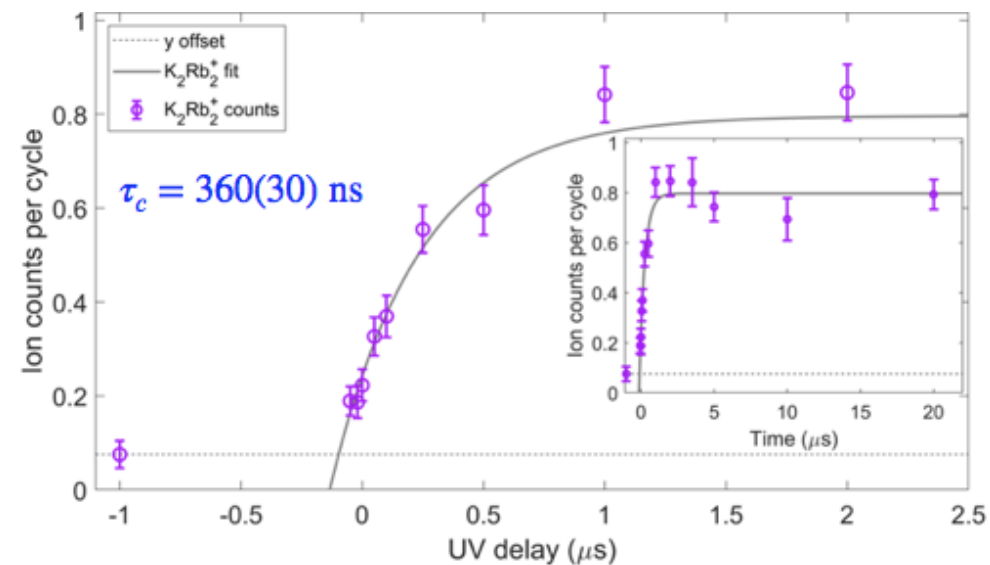
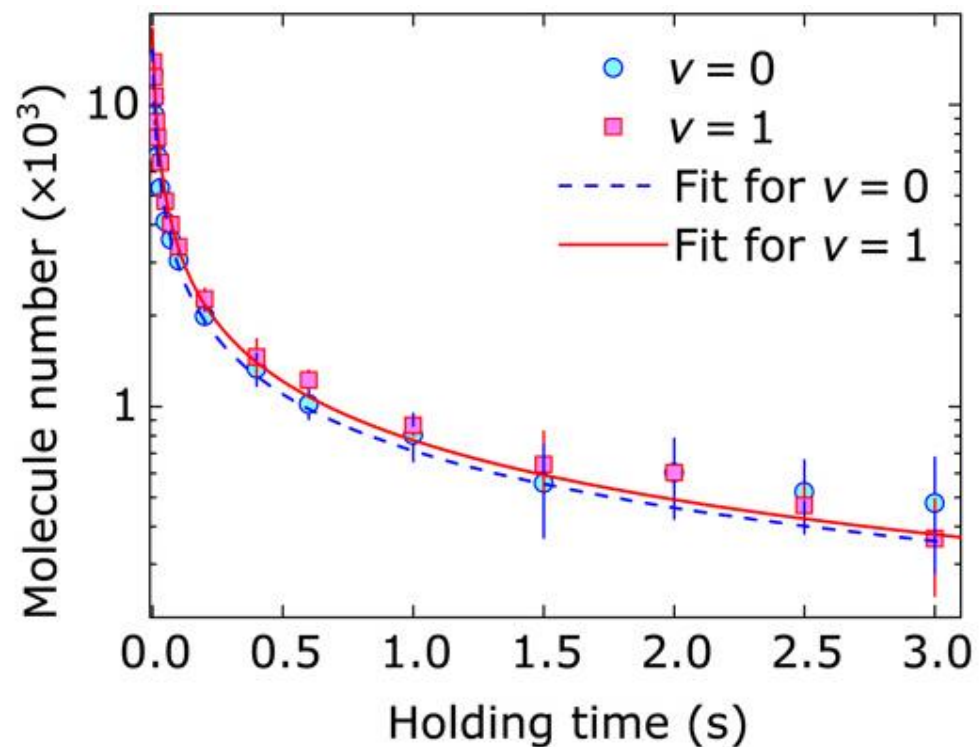


$$\beta = 1.2(3) \times 10^{-5} \text{ cm}^3/(\text{s K})$$

Molecular losses look universal



Dajun Wang *et al.*, *Sci. Adv.*, 4, eaaq0083(2018).



Direct detection of K_2Rb_2^* intermediate

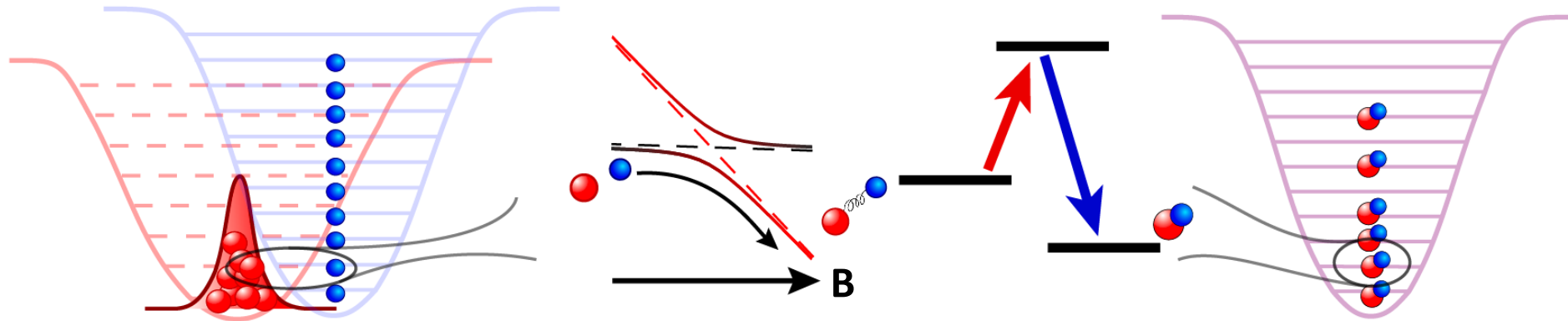
Kang-Kuen Ni *et al.*, *Science* 366, 1111 (2019); *Nature Physics* (2020).

A degenerate Fermi gas of molecules

Ni, Ospelkaus, de Miranda, Pe'er, Neyenhuis, Zirbel, Kotochigova, Julienne, Jin, & Ye, *Science* **322**, 231 (2008).

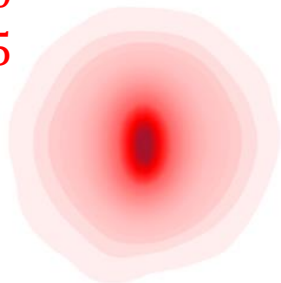
$$T/T_F \sim 1.4$$

Luigi De Marco *et al.*, *Science* **363**, 853 (2019).



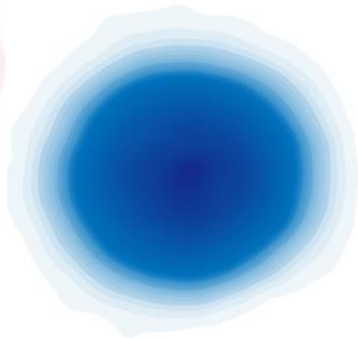
Innsbruck, Durham, MIT, Hong Kong, USTC, MPQ, Harvard, Singapore, ...

$$N = 7 \times 10^4$$
$$T/T_c = 0.5$$



⁸⁷Rb

⁴⁰K

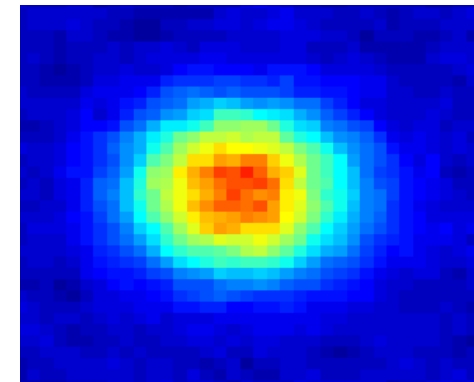


$$N = 5 \times 10^5$$
$$T/T_F = 0.1$$

Atom – Molecule
thermalization



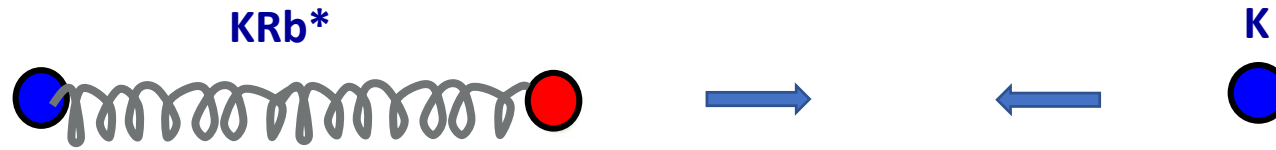
$$N = 3 \times 10^4, T = 50 \text{ nK}, T/T_F = 0.3$$



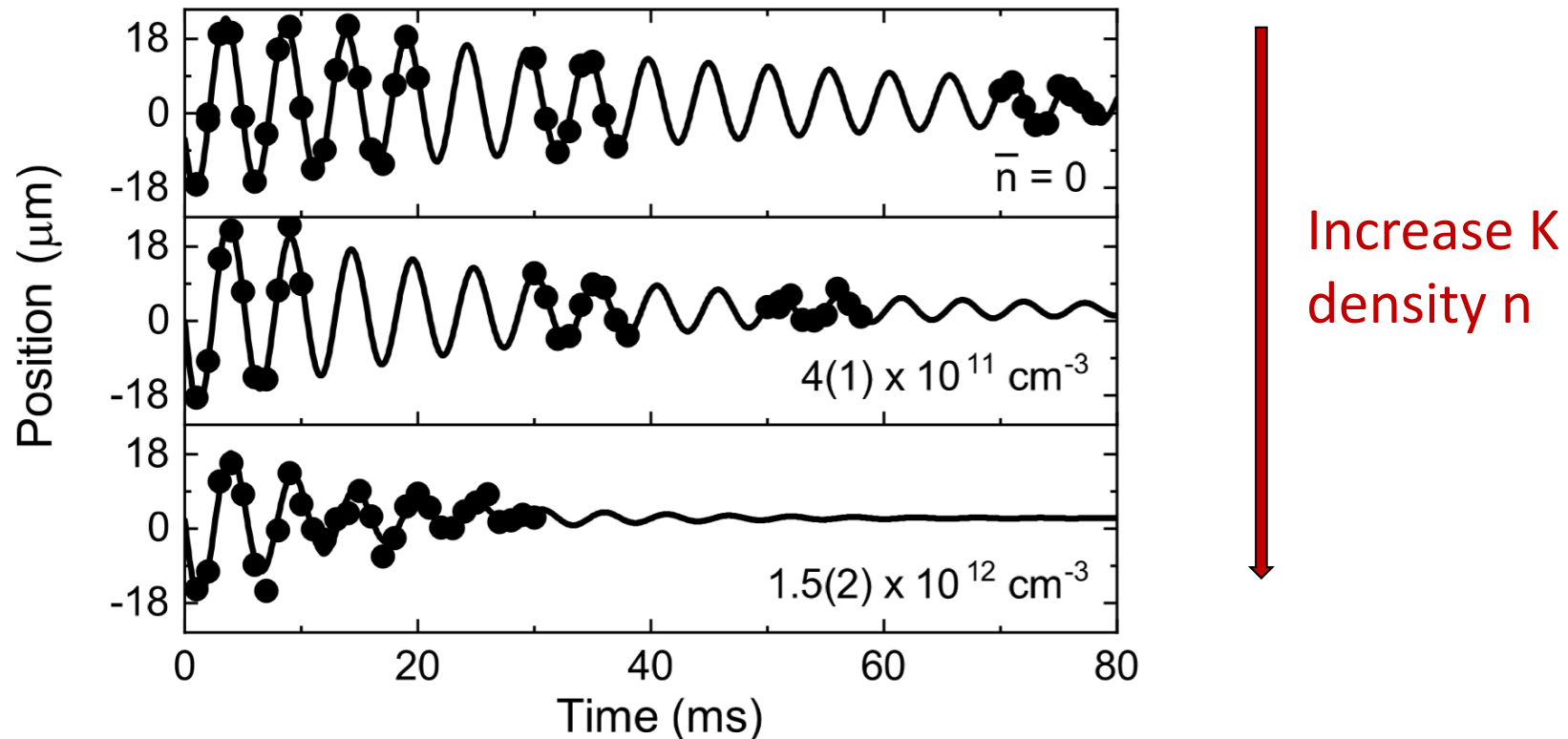
Atom - Molecule thermalization

W. Tobias *et al.*, Phys. Rev. Lett. **124**, 033401 (2020).

NaLi + Na:
Ketterle *et al.*,
Nature **580**, 197 (2020).

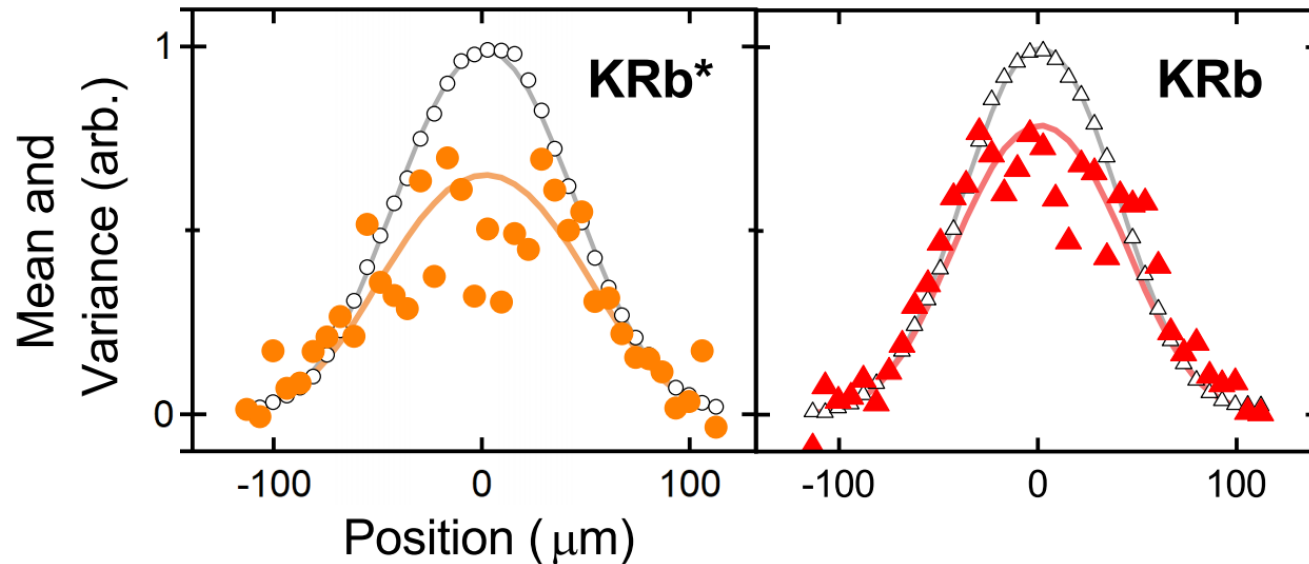
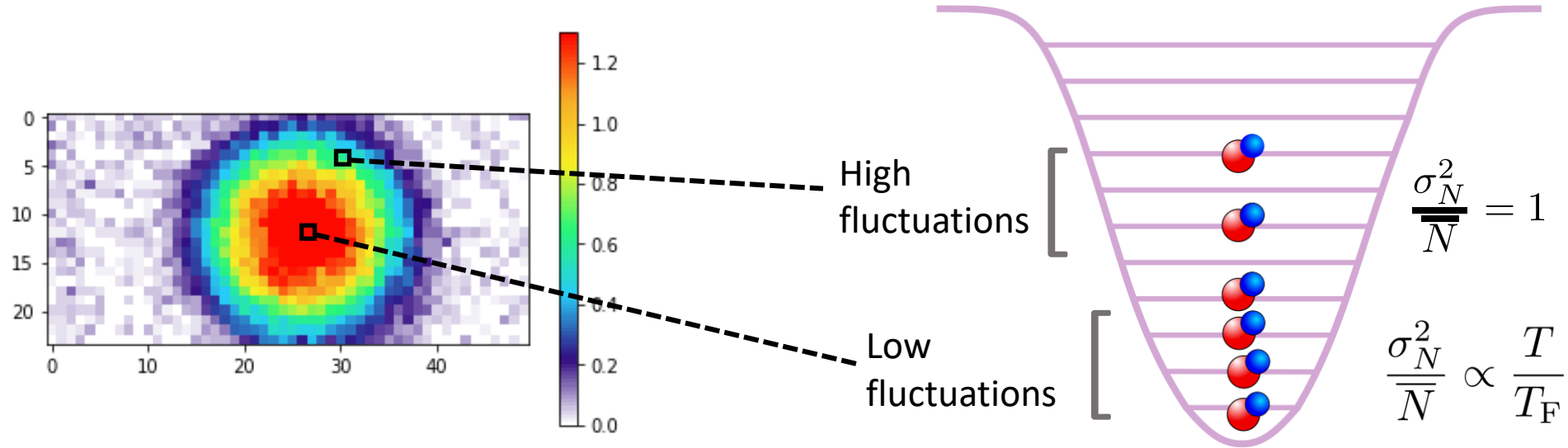


- Produce KRb^* , remove remaining Rb
- Excite center of mass oscillation of KRb^* but not K



Fermi suppression of density fluctuations

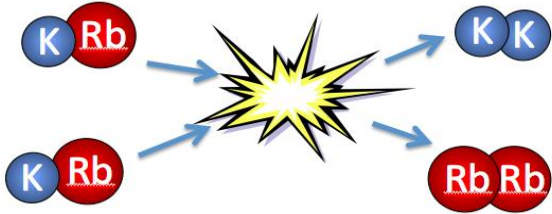
W. Tobias *et al.*, Phys. Rev. Lett. **124**, 033401 (2020).



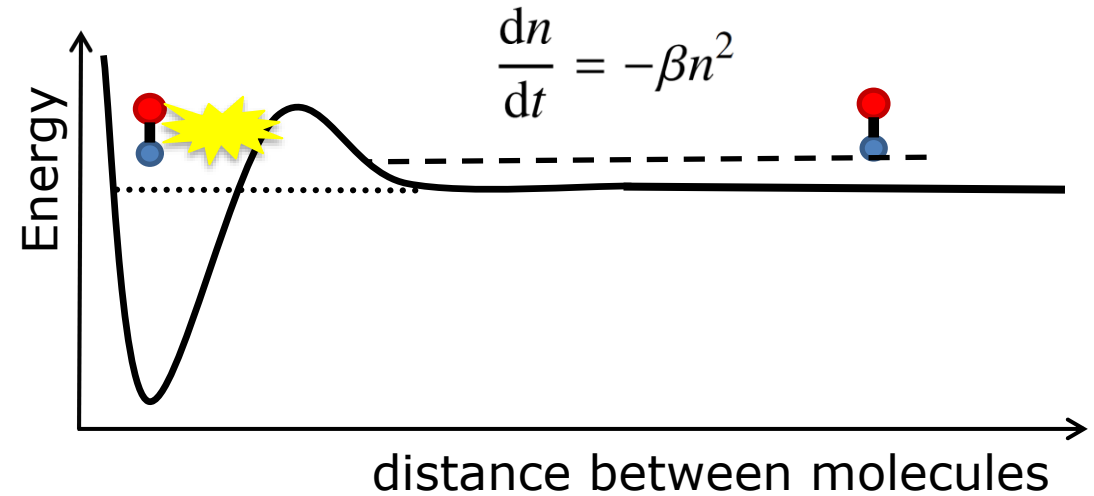
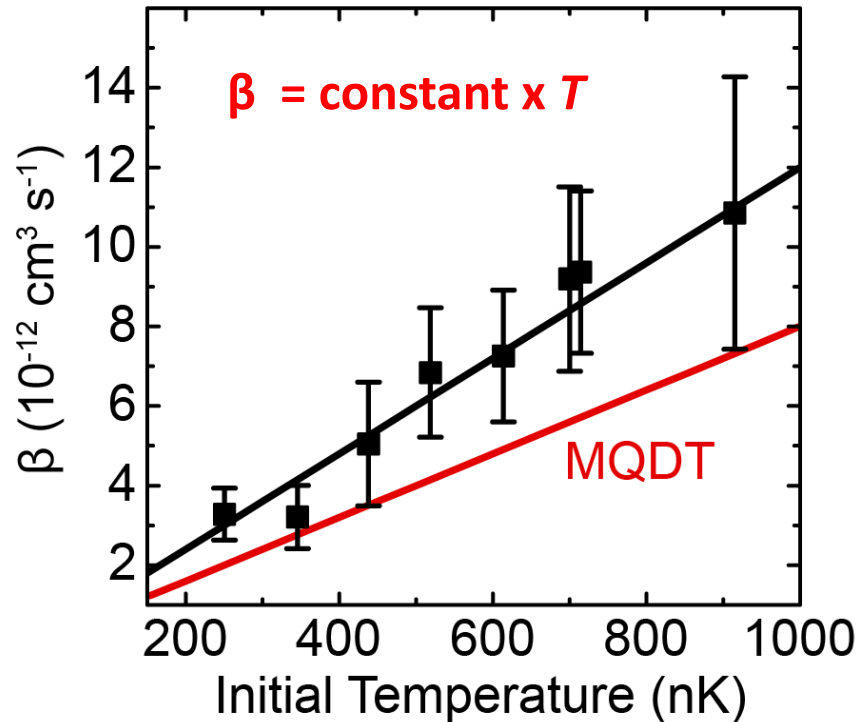
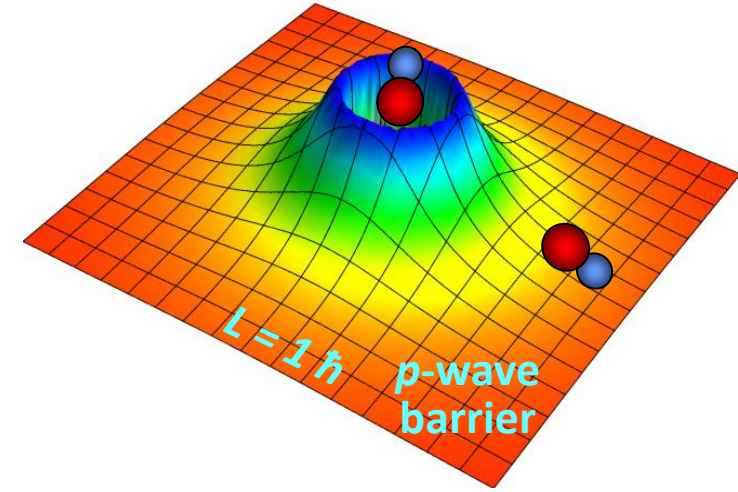
C. Sanner *et al.*, PRL (2010);
T. Muller *et al.*, PRL (2010).

Chemistry near absolute zero

Ospelkaus *et al.*, Science **327**, 853 (2010): $T/T_F \sim 1.4$

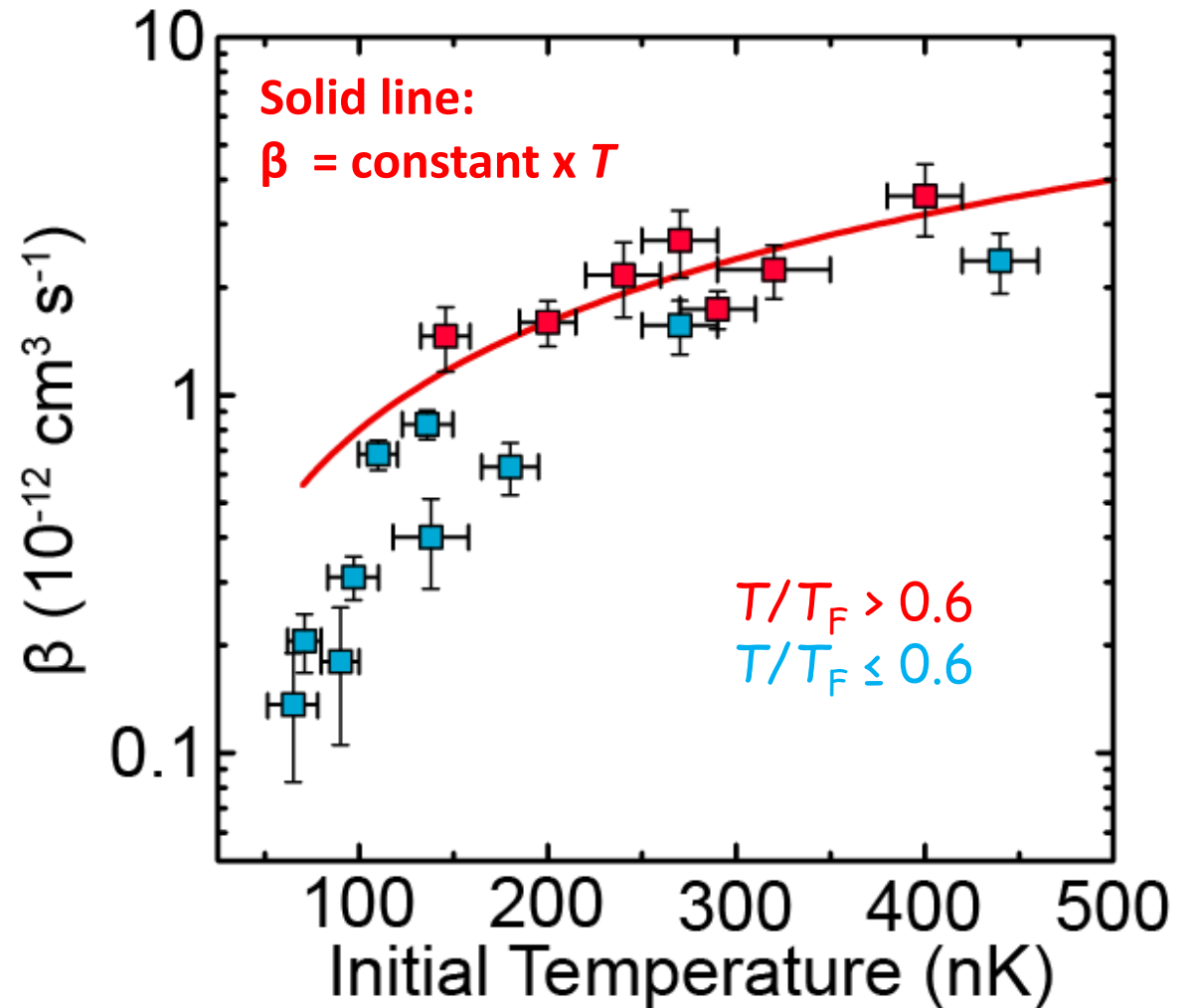


- Quantum statistics dictate reaction rate
- Single collision partial wave



Reactions in Degeneracy

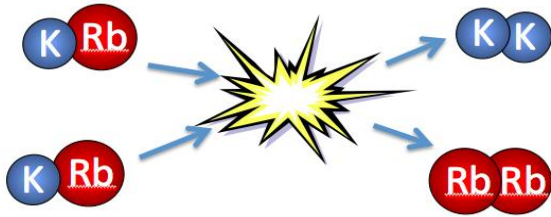
- At very low T , deviations from Bethe-Wigner threshold law
- For $T/T_F > 0.6$
 - $\beta/T = 0.84(6) \times 10^{-5} \text{ cm}^3 \text{ s}^{-1} \text{ K}^{-1}$
- For $T/T_F \leq 0.6$
 - sub-linear behavior



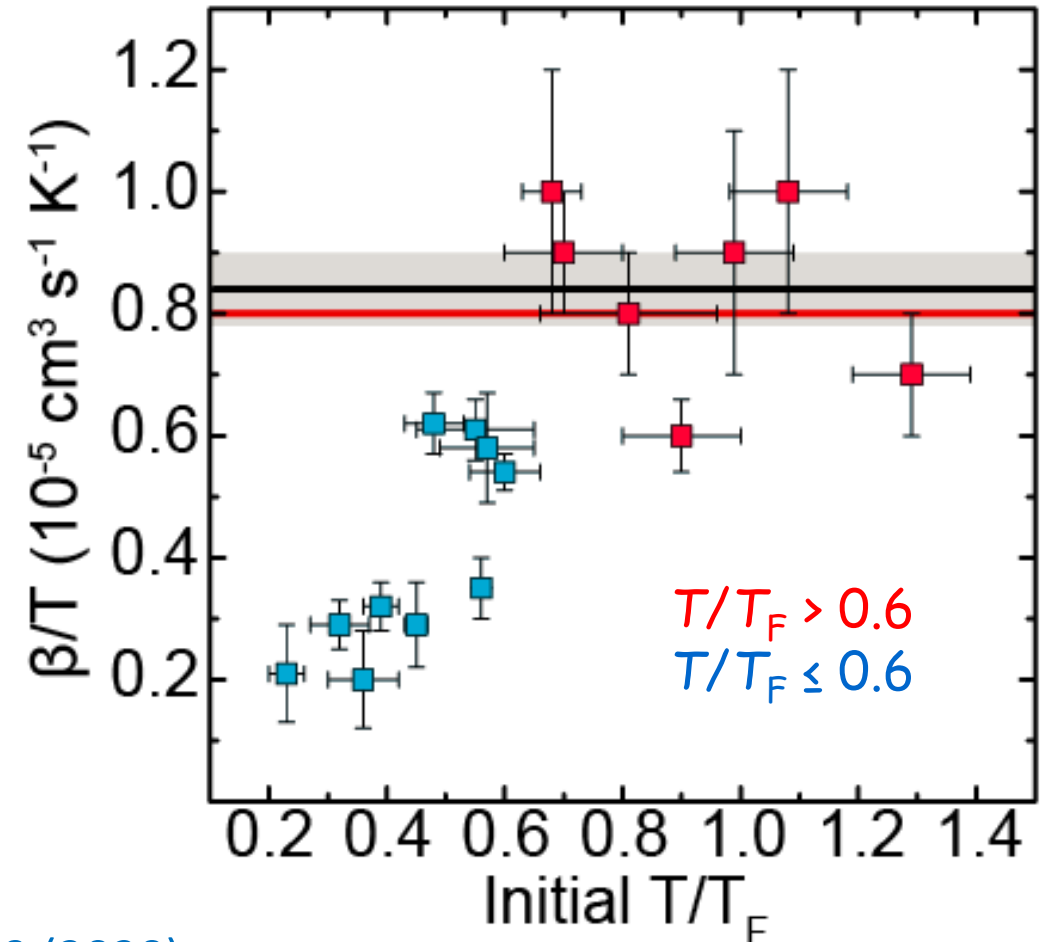
Chemistry in a degenerate Fermi gas

De Marco *et al.*, Science **363**, 853 (2019).

Rate coefficient $\beta / T = \text{constant}$ (thermal gas, p -wave)



- For $T/T_F > 0.6$
 - $\beta/T = 0.84(6) \times 10^{-5} \text{ cm}^3 \text{ s}^{-1} \text{ K}^{-1}$
- For $T/T_F \leq 0.6$
 - β/T decreases



Qi Zhou group: p -wave contact, Science Advances **6**, eabd4699 (2020).

Ana Maria Rey group: Zeno effect via intermediates, PRA **102**, 063322 (2020).

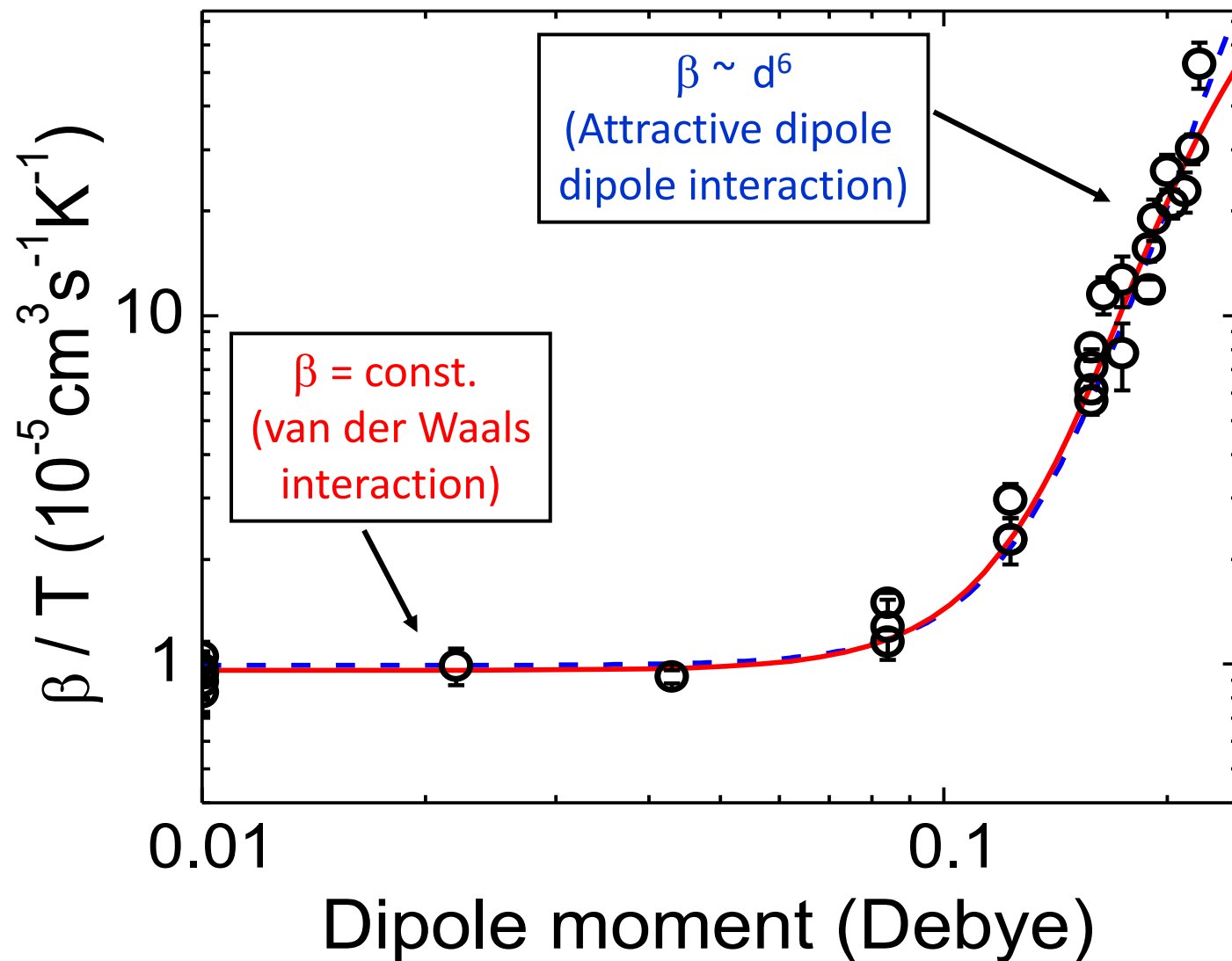
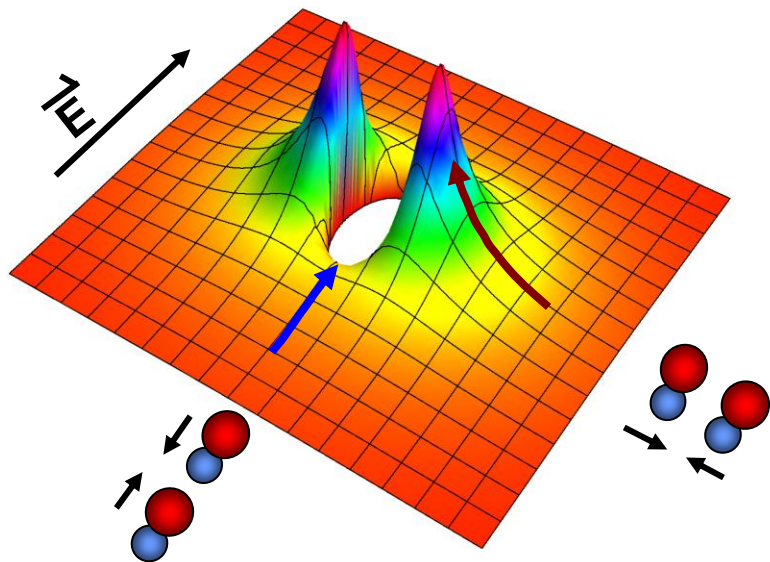
Inelastic collisions under E

Ni *et al.*, Nature **464**, 1324 (2010).

- Dipolar interaction enhances reaction
- Stereo chemistry – geometry matters

Long-range potential

$$V(R) = \frac{\hbar^2 L(L+1)}{2\mu R^2} - \frac{C_6}{R^6} - \frac{C_3}{R^3}$$



Dipolar physics in 2D

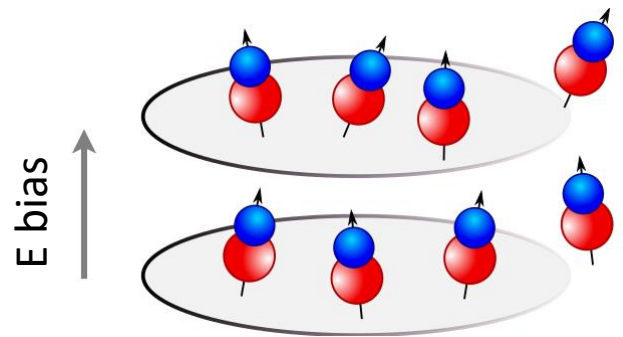
Büchler, Bohn, Bruun, Demler, Julienne, Lewenstein, Pupillo, Santos, Shlyapnikov, Baranov/Zoller, ...

Büchler, Demler, Lukin, Micheli, Prokof'ev, Pupillo, & Zoller, PRL **98**, 060404 (2007).

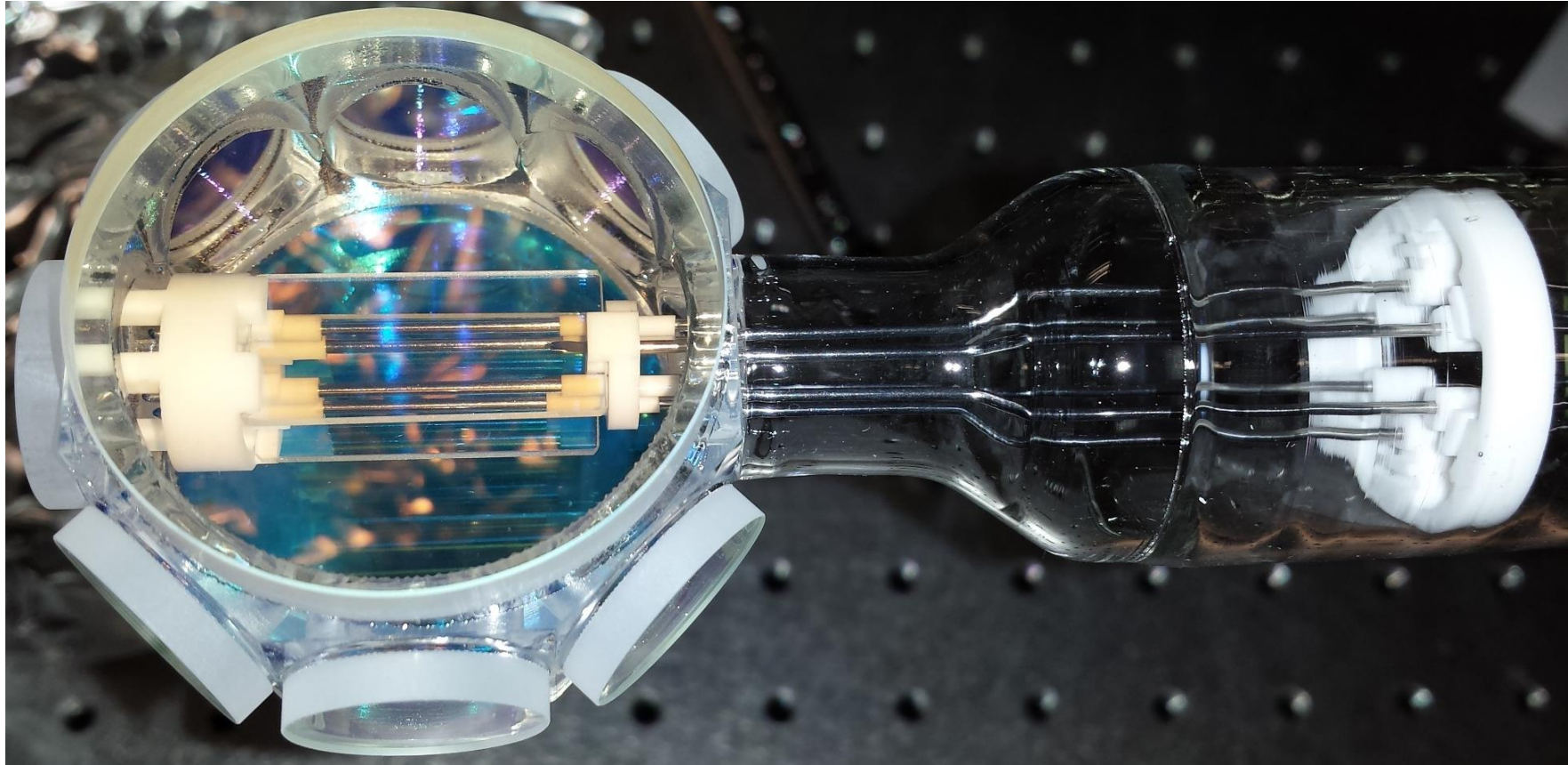
- Suppression of chemical reaction
- Crossover from 3D regime to 2D
- Elastic interaction $\gg$ inelastic loss
- Dipolar evaporative cooling
- Dipole-mediated collision resonance

latest

Bulk gas in 3D
Dipolar exchanges



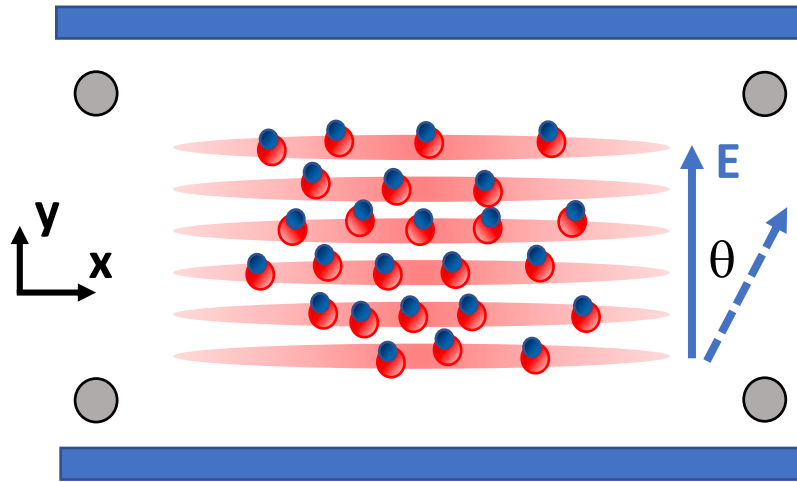
Control interactions in a molecular quantum gas



- All 6 electrodes are in vacuum
15 kV/cm, arbitrary orientation, reconfigurable gradients
- Use E to suppress loss & tune dipolar interaction

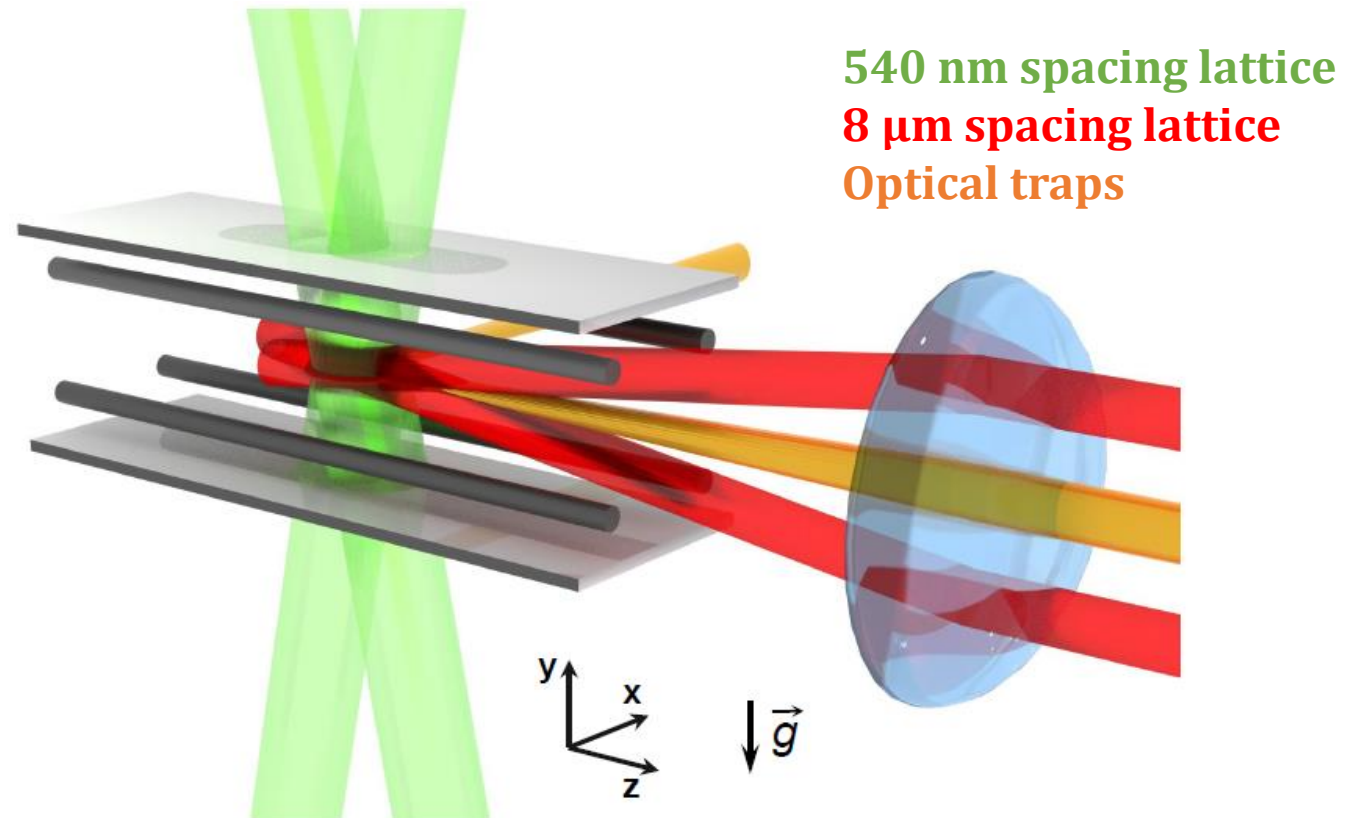
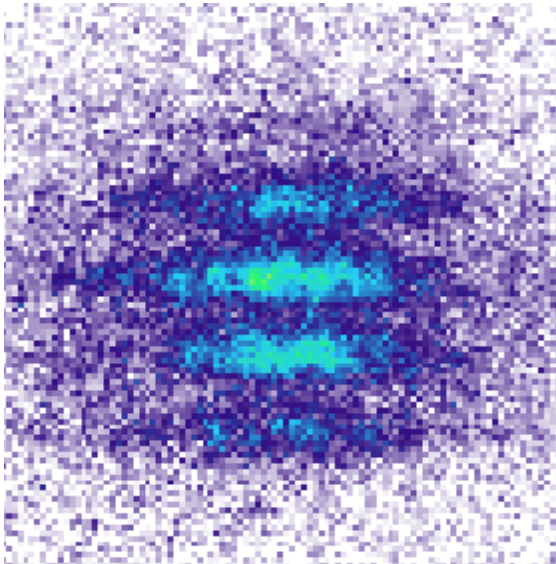
Polar molecules under precise E-field control

Valtolina *et al.*, Nature **588**, 239 (2020).



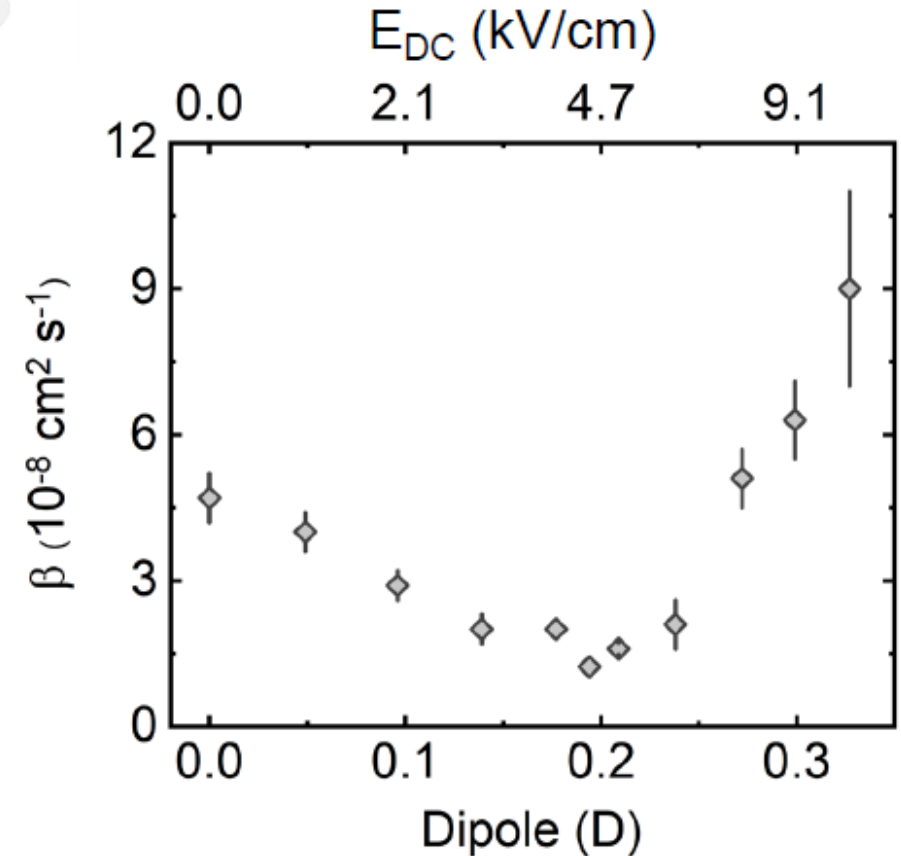
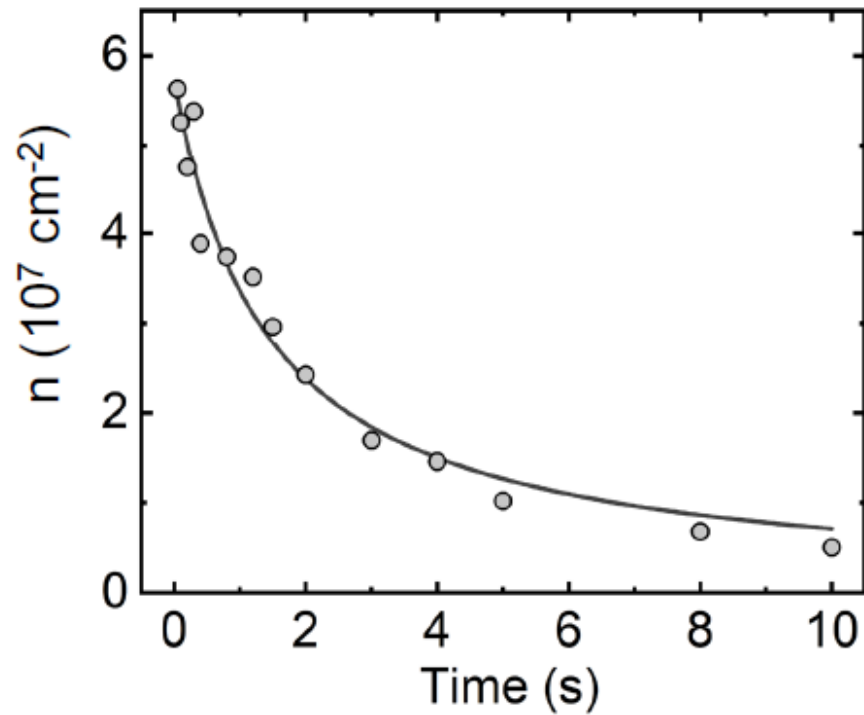
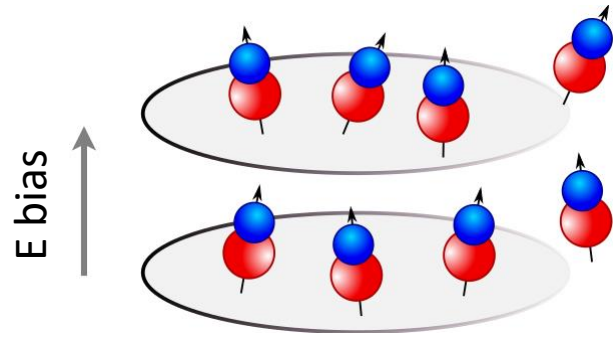
- E_{DC} : angle θ , 0 to 15 kV/cm (known to 10^{-4})
- Gradient (x, y): 0 to 8 kV/cm²; Curvature
- RF for rotational transition (~ 100 kHz Rabi)

4 Layers



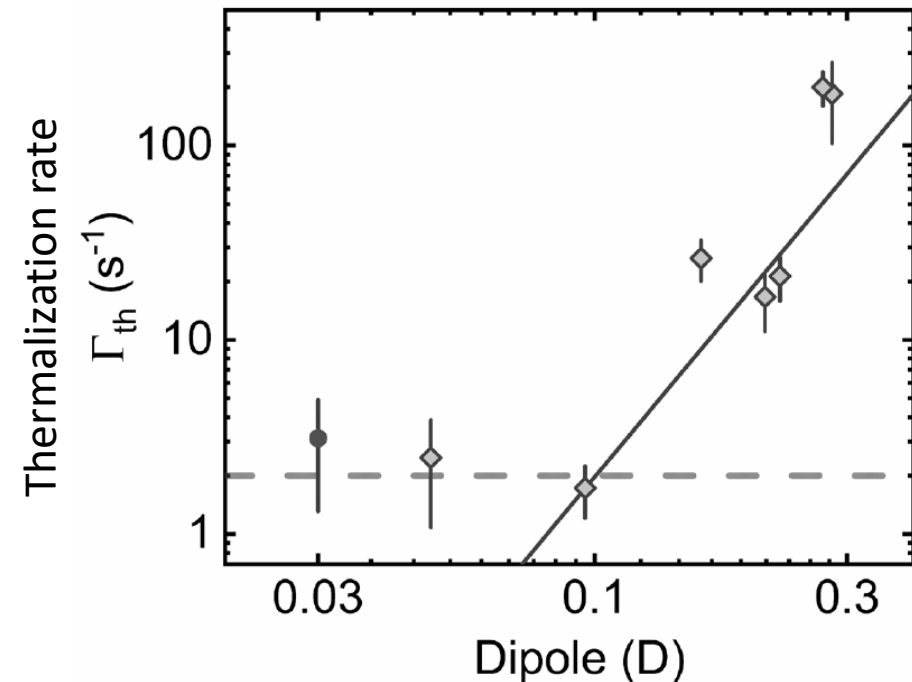
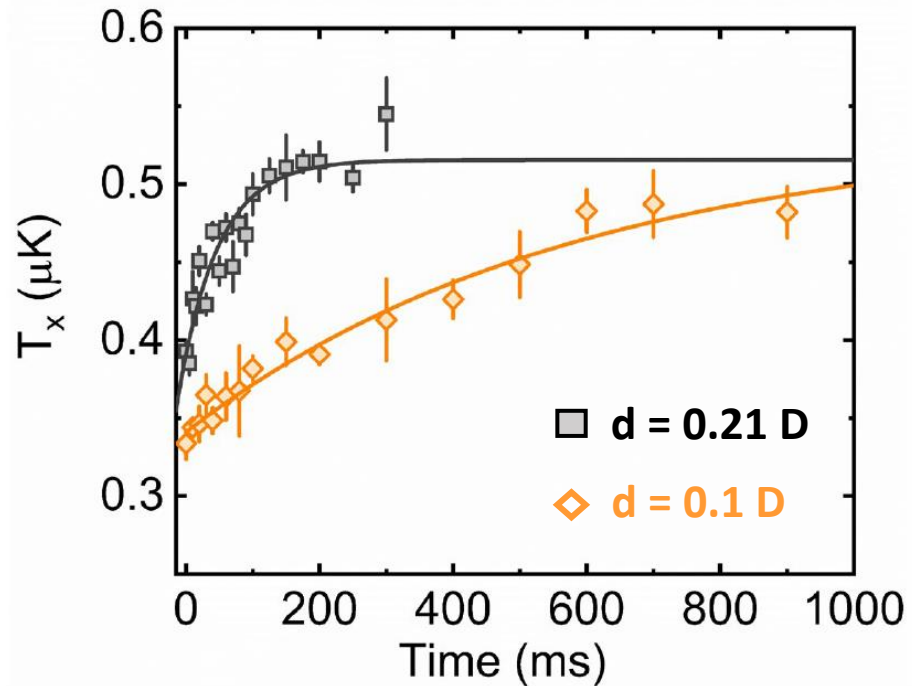
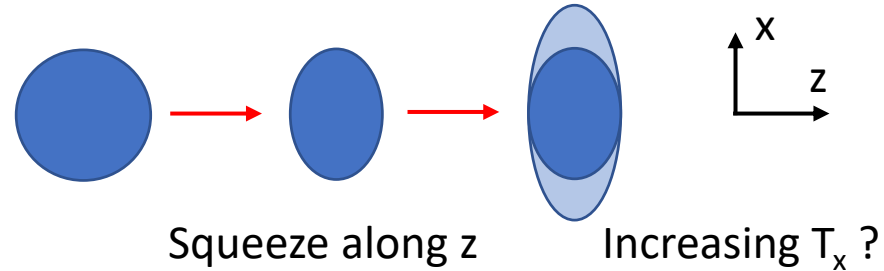
Suppression of inelastic loss in 2D

- For dipole moment of 0.2 D, elastic / inelastic ~ 200



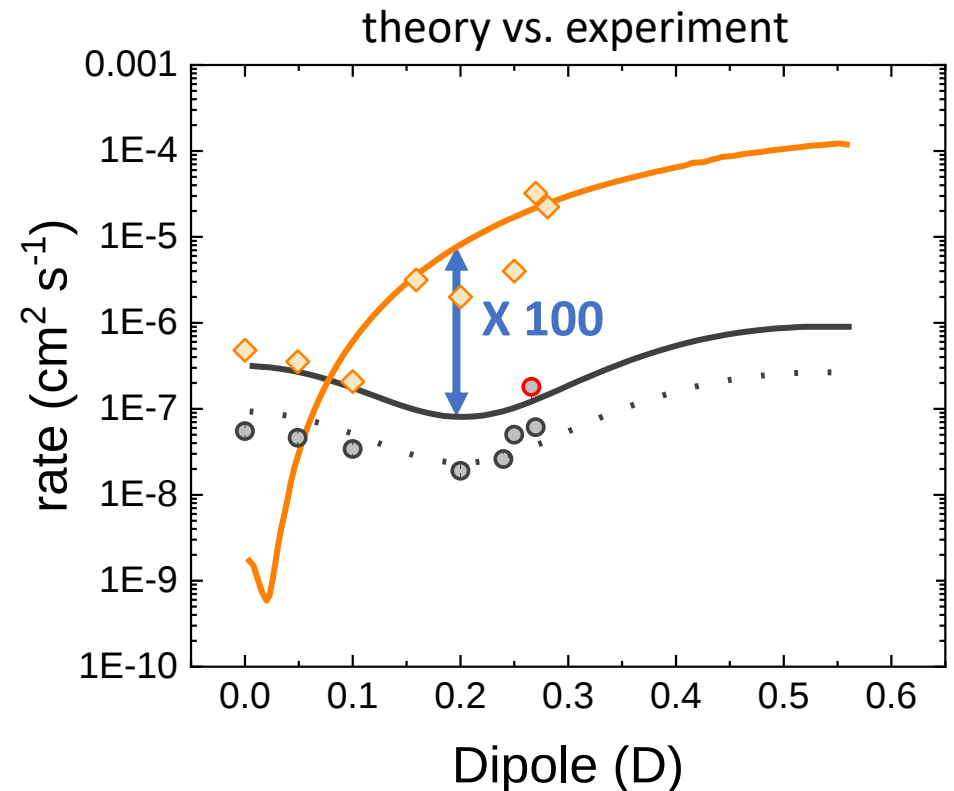
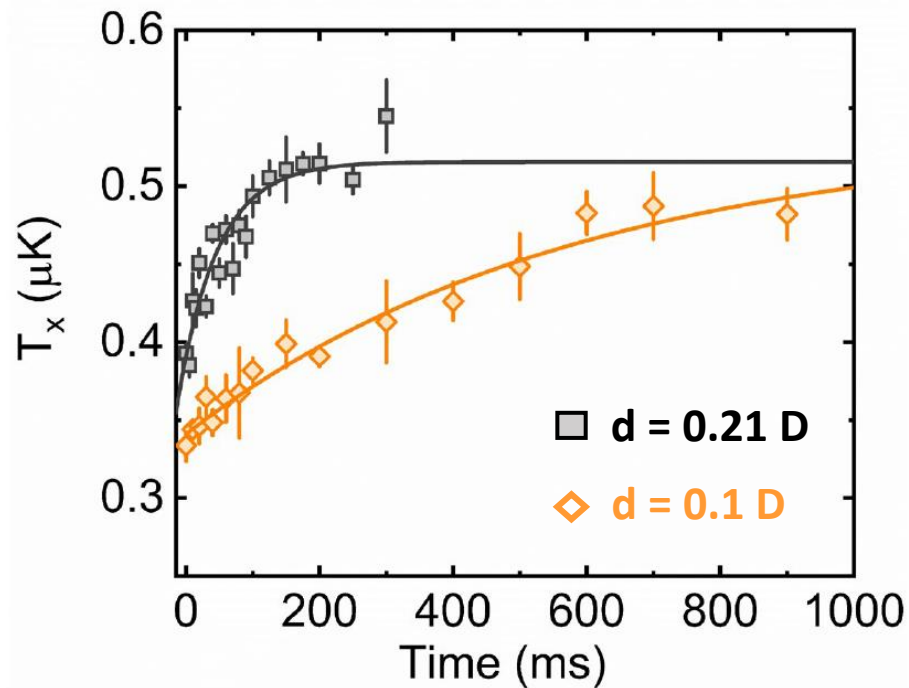
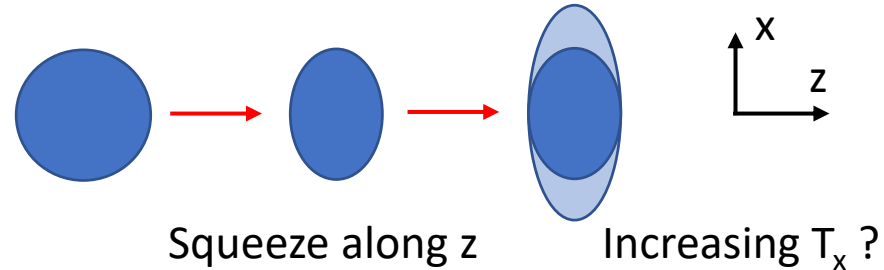
Dipolar thermalization

- Cross dimensional thermalization
- Determine dipolar collision cross-section



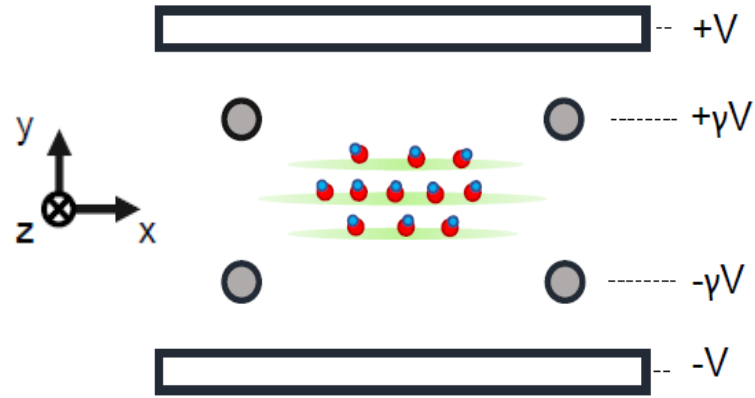
Dipolar thermalization

- Cross dimensional thermalization
- Determine dipolar collision cross-section

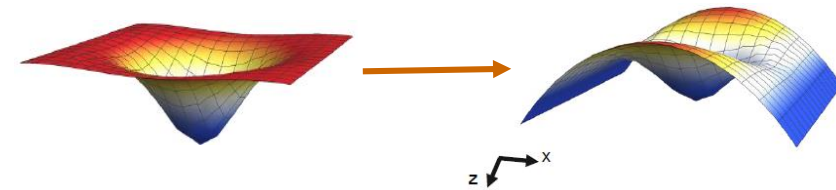


Dipole-assisted evaporation

Control trap potential with E & its gradient

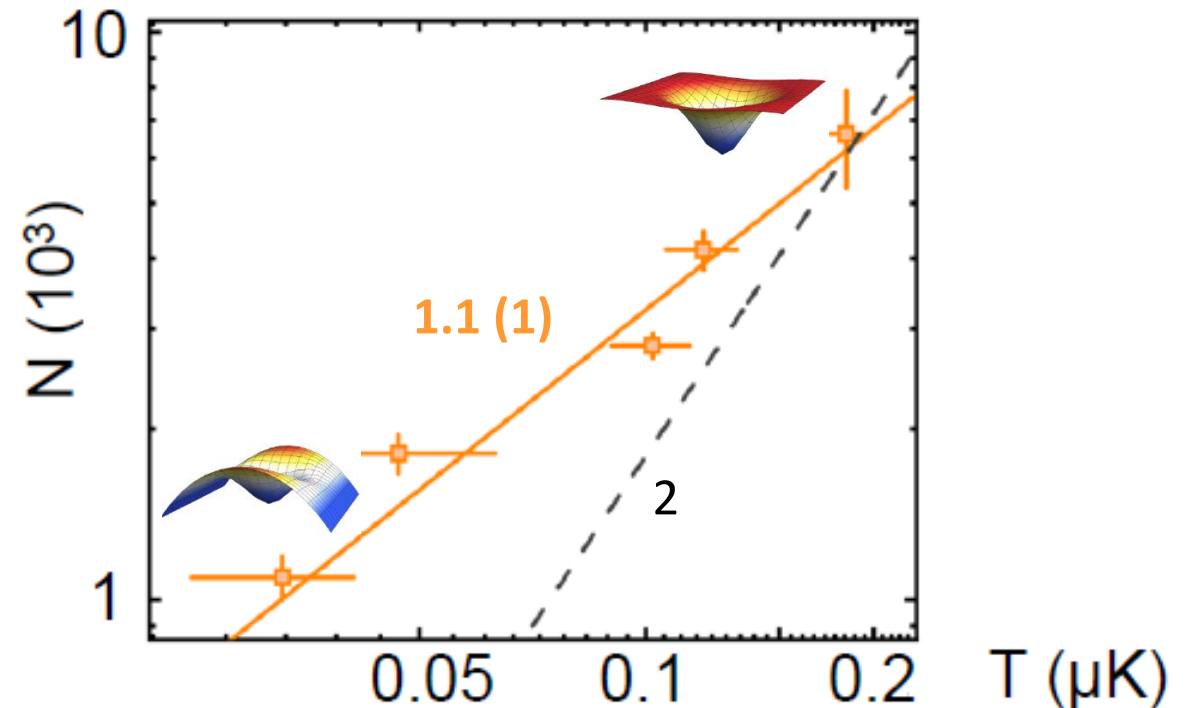


Increase anti-curvature/decrease trap depth



Criterion for good evaporation:

$$\frac{\partial \log N}{\partial \log T} < D = 2$$

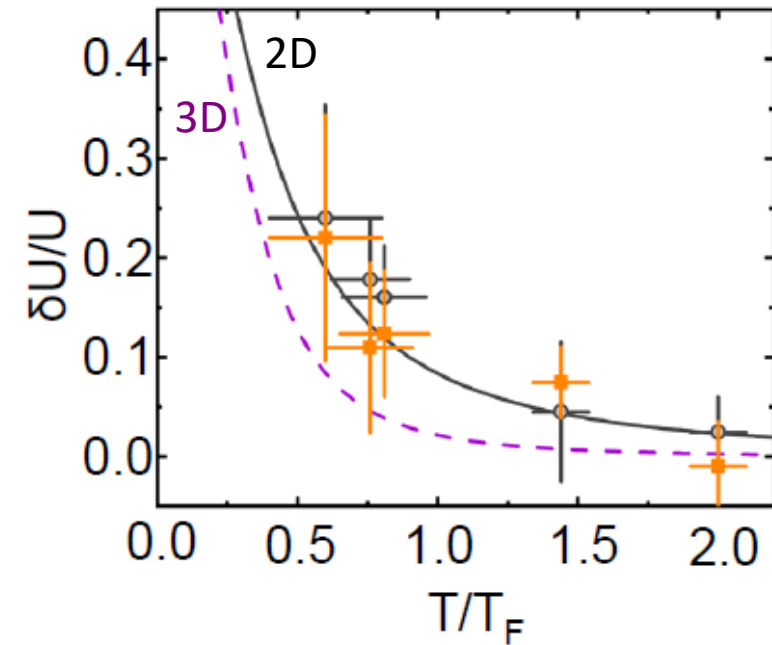
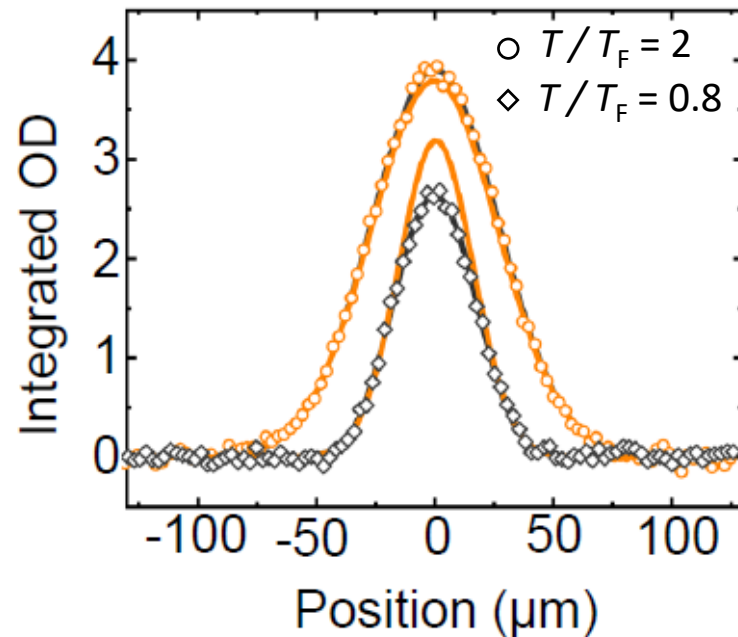
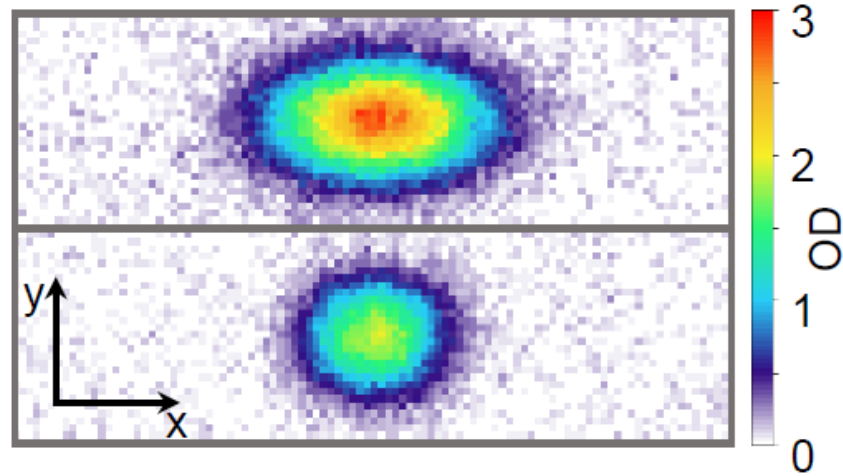


Dipole-assisted evaporation

Valtolina *et al.*, Nature **588**, 239 (2020).

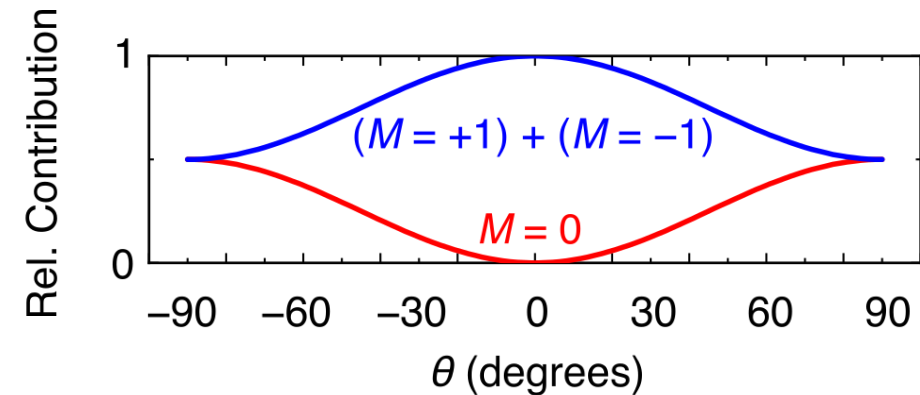
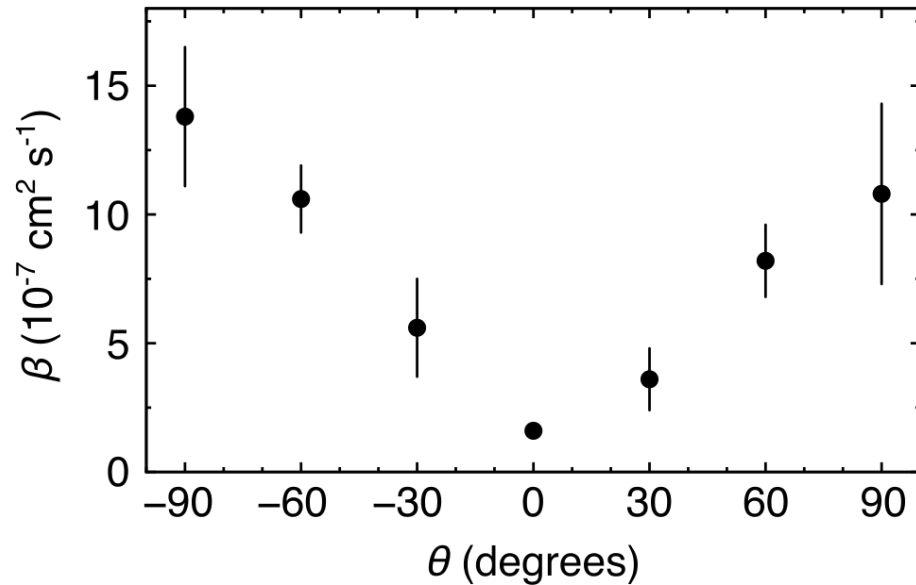
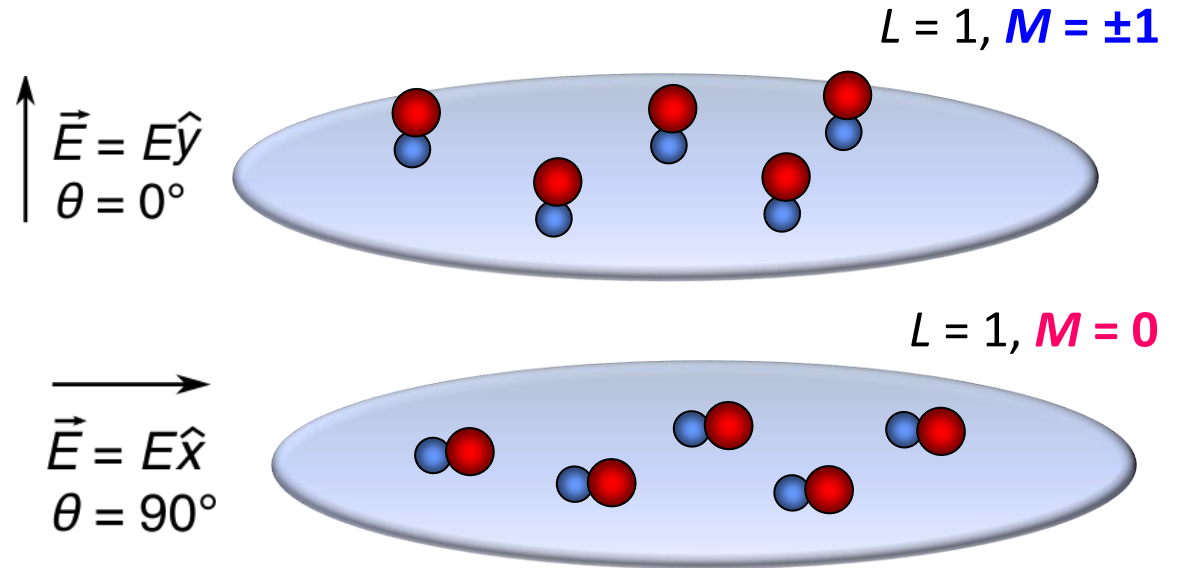
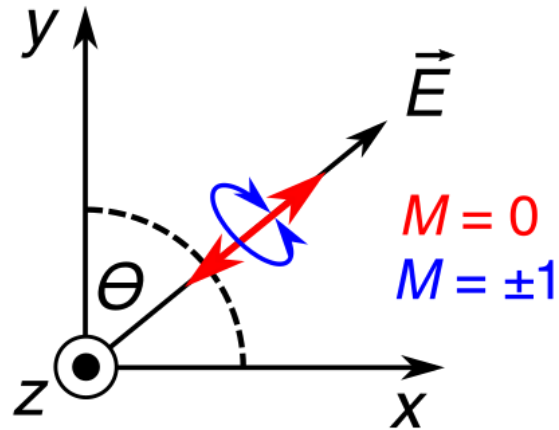
Evaporation image

- thermal
- degenerate

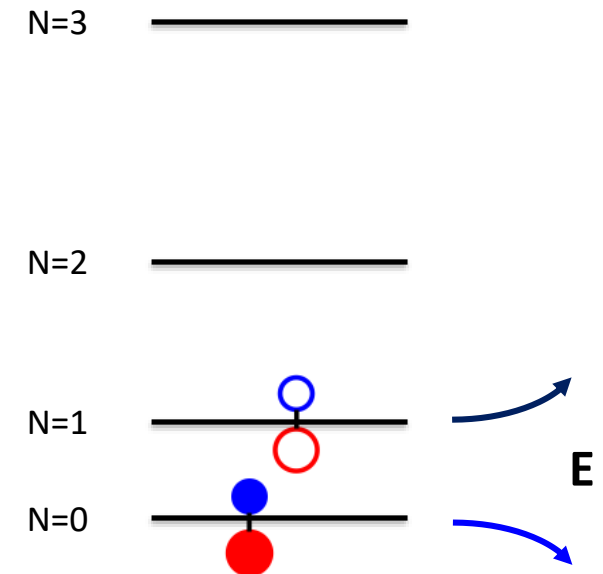
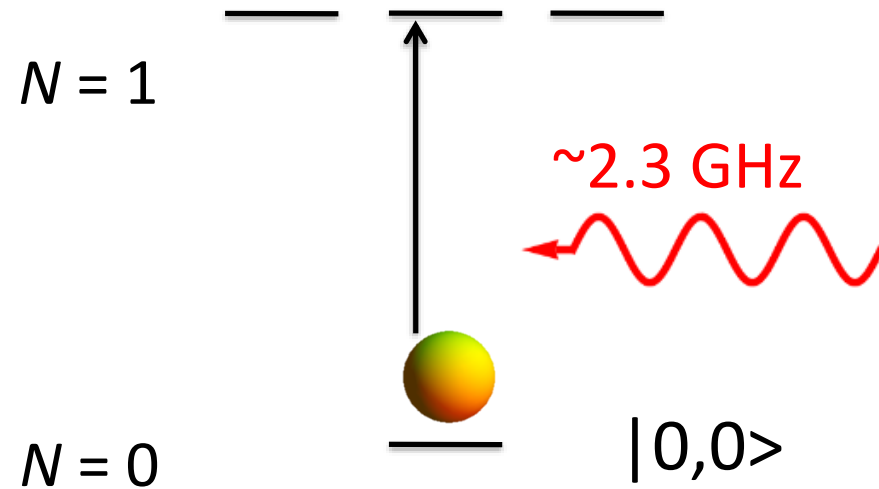


Control of reactions with E field orientation

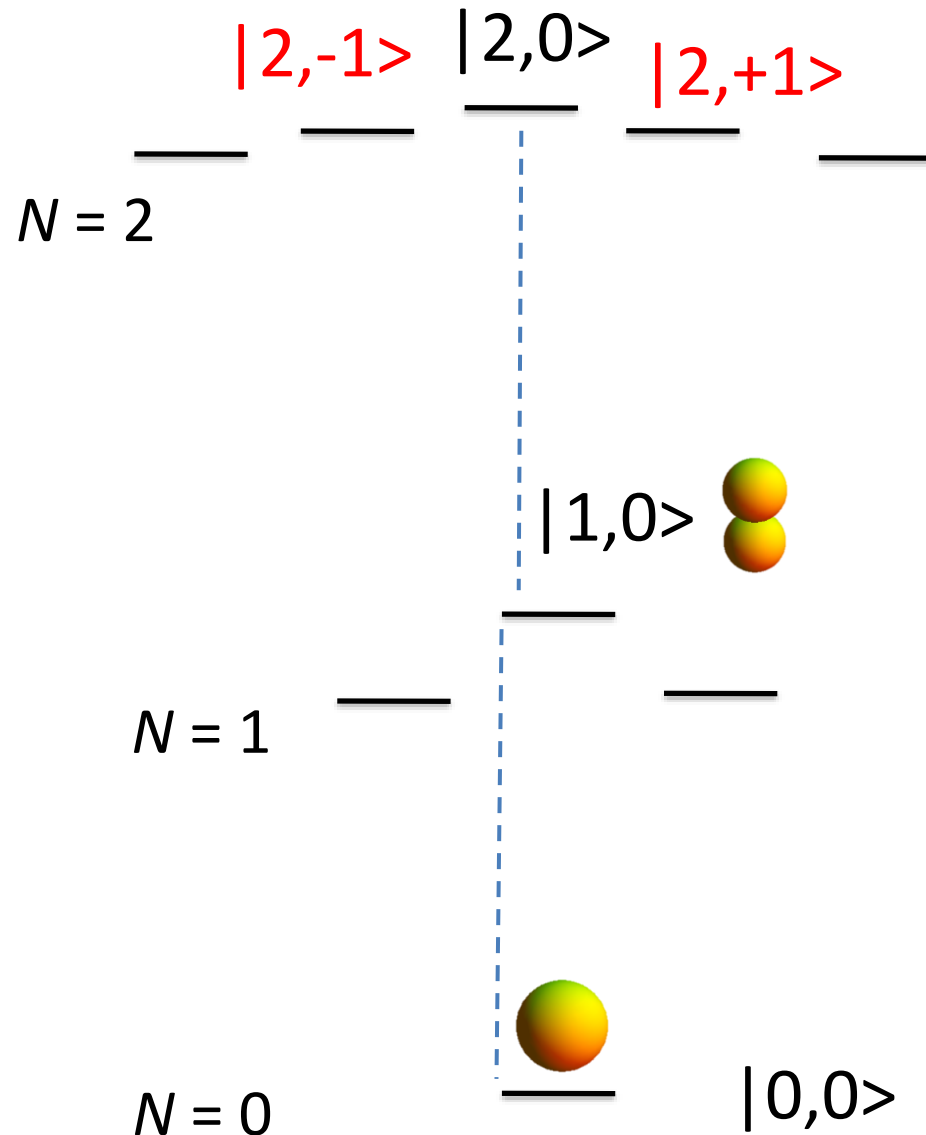
Matsuda *et al*, Science **370**, 1324 (2020).



Molecular energy tuned with $|E|$



Molecular energy tuned with $|E|$

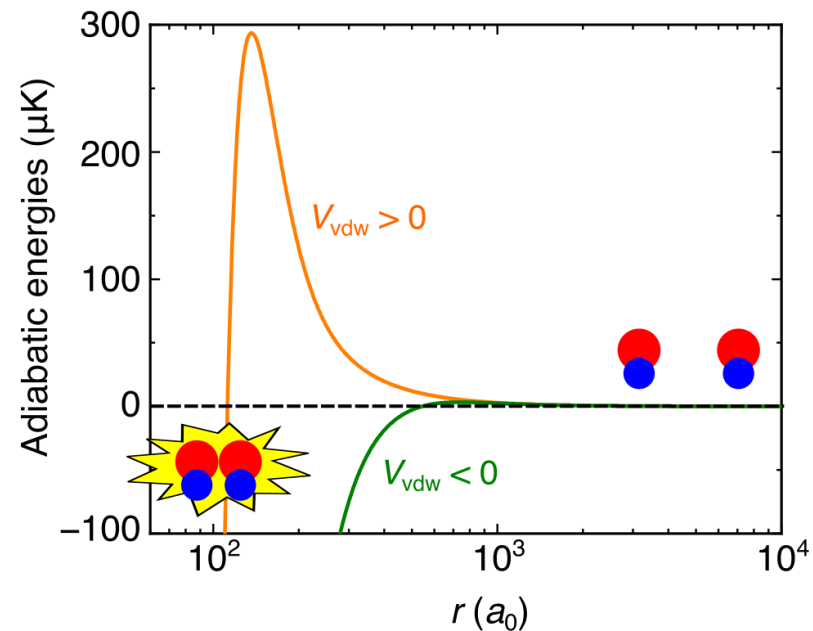
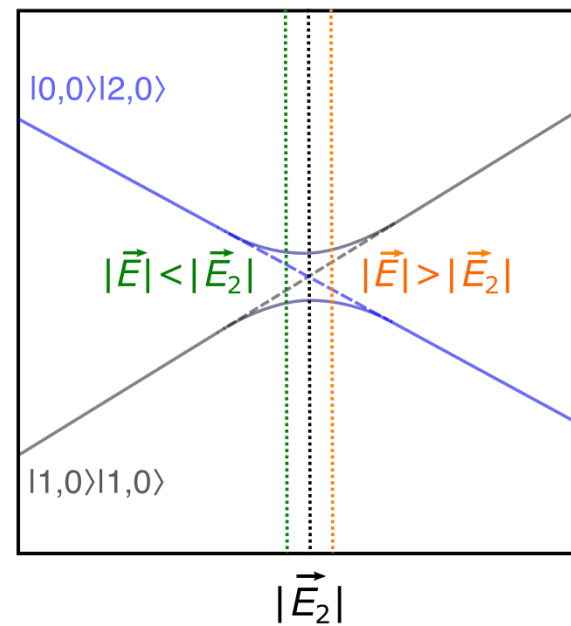
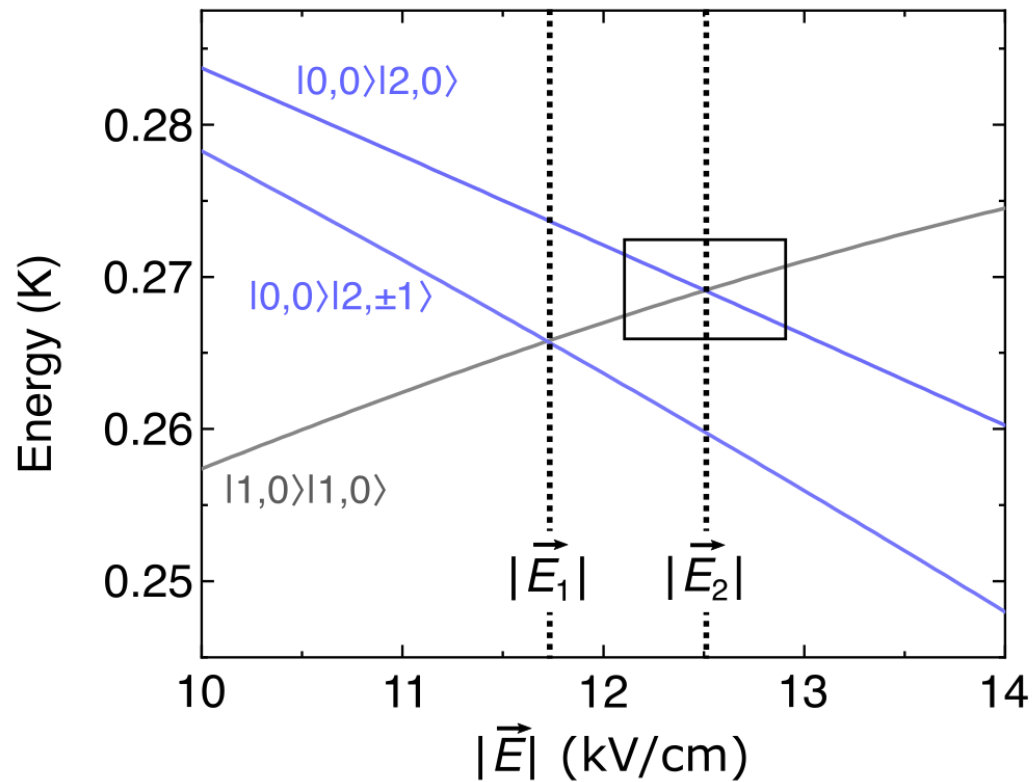


$$\begin{aligned} &|1,0\rangle + |1,0\rangle \\ &= |0,0\rangle + |2,0\rangle \end{aligned}$$

or,

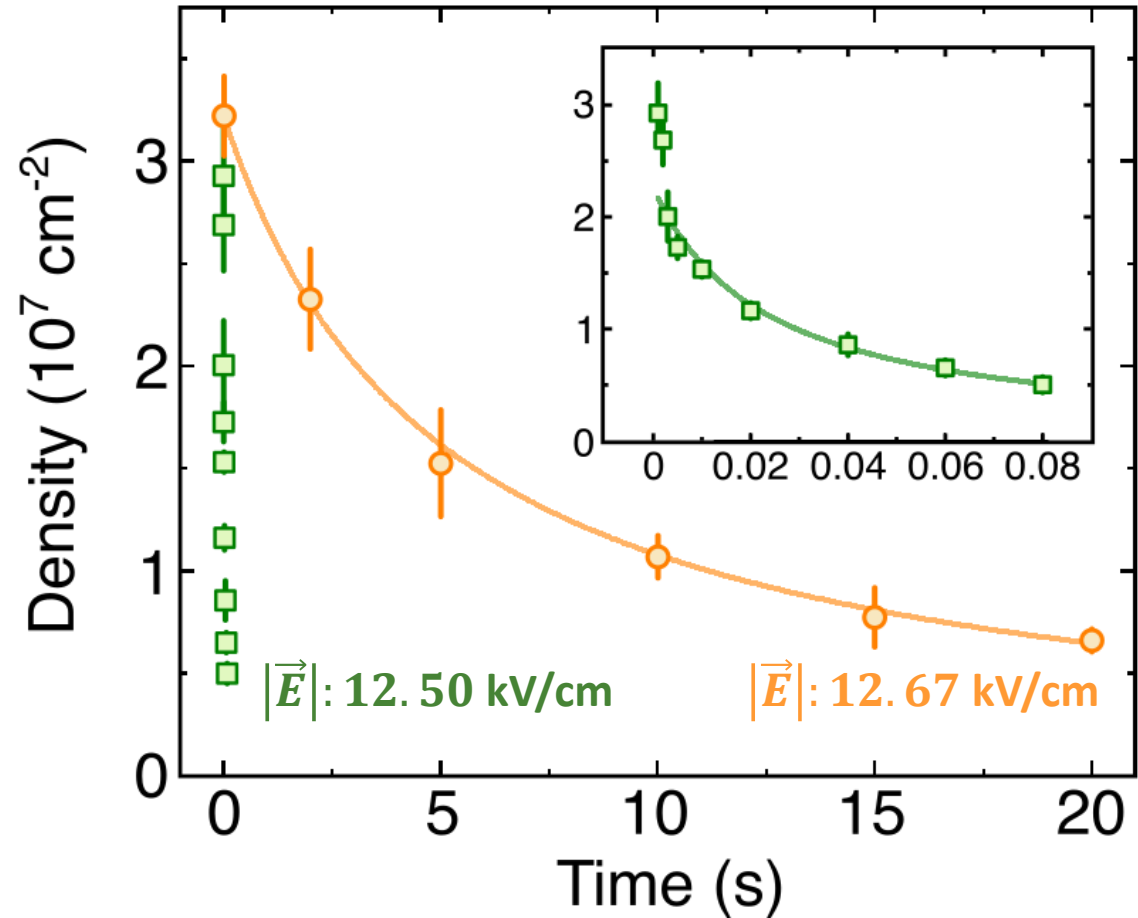
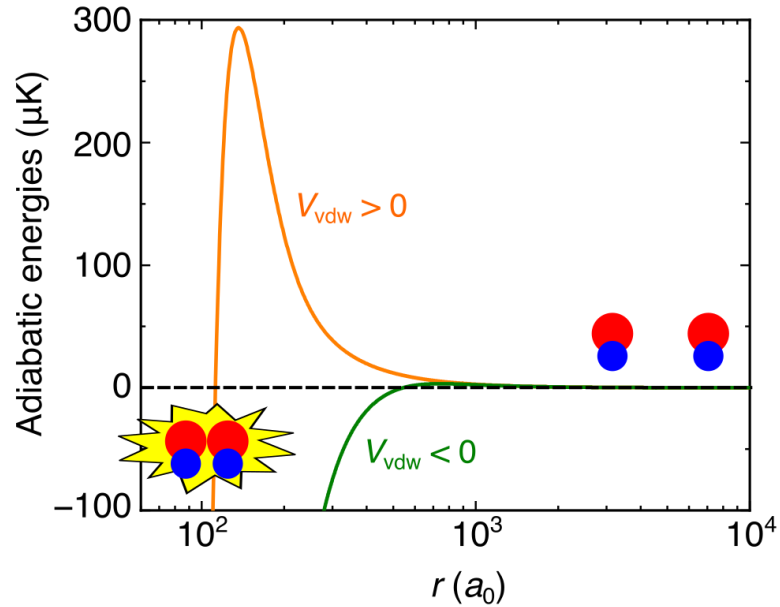
$$\begin{aligned} &|1,0\rangle + |1,0\rangle \\ &= |0,0\rangle + |2,\pm 1\rangle \end{aligned}$$

E field induced resonance & shielding



Resonant shielding & enhancement of reaction

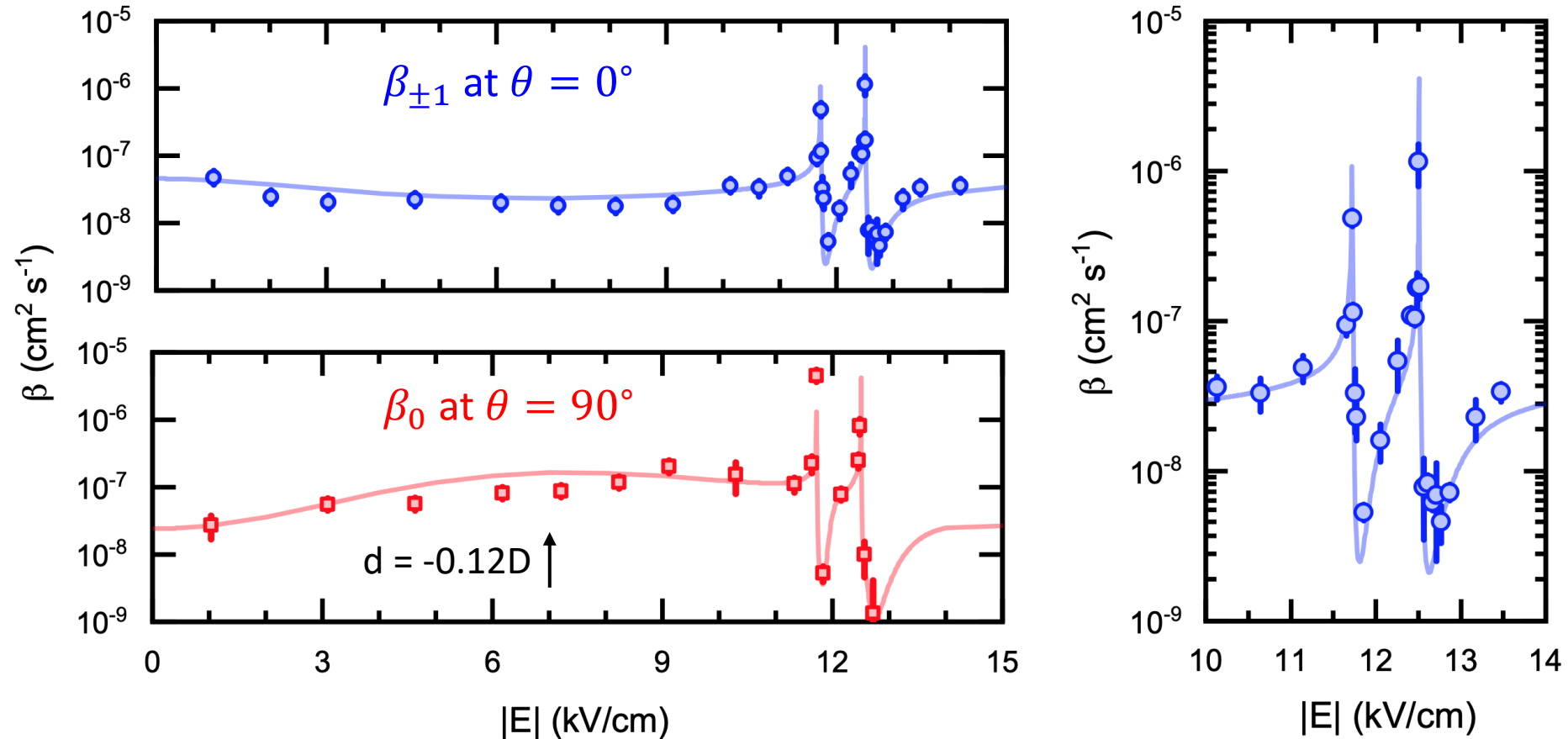
Matsuda *et al*, Science **370**, 1324 (2020).



Characterization of resonant shielding

Matsuda *et al*, Science (Dec. 10, 2020).

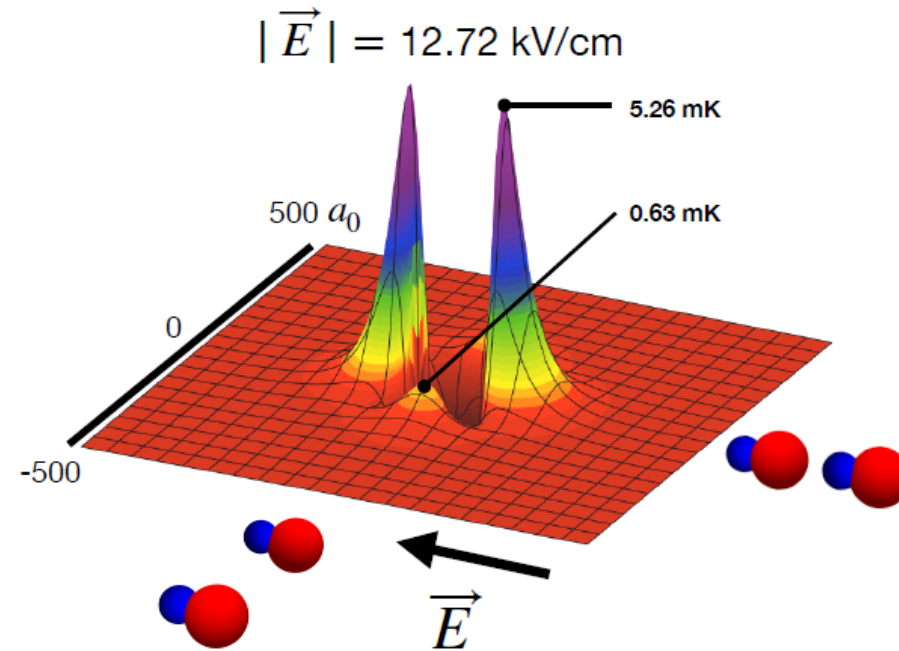
Solid lines: no free parameter scattering theory (Goulven Quéméner)



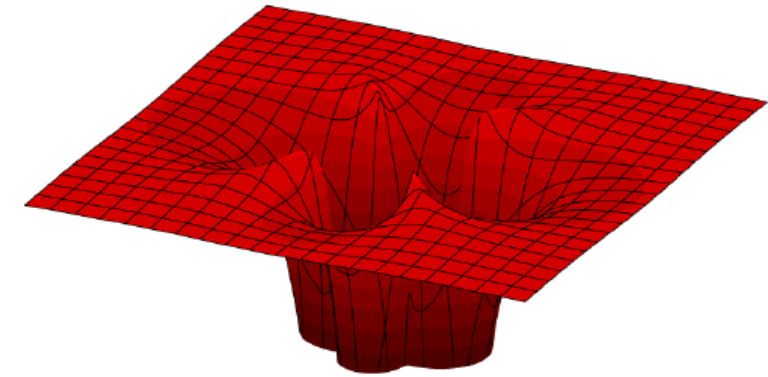
- Dipolar interaction controls collision resonances
- Shielding for both $M = 0$ & ± 1 channels

Resonant shielding works in 3D !

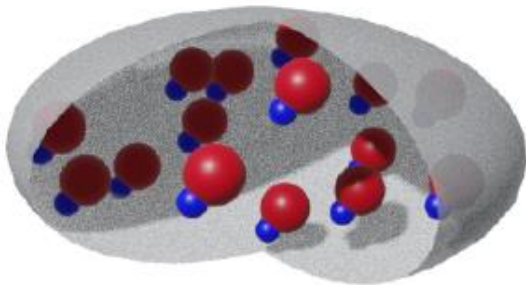
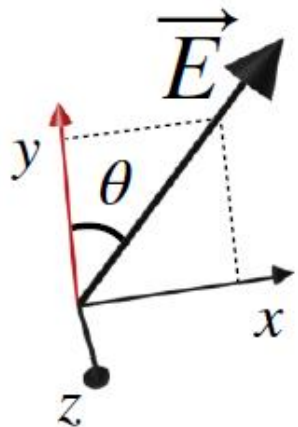
J. Li *et al*, arXiv:2103.06246 (Nature Phys. 2021).



$$|\vec{E}| = 12.50 \text{ kV/cm}$$

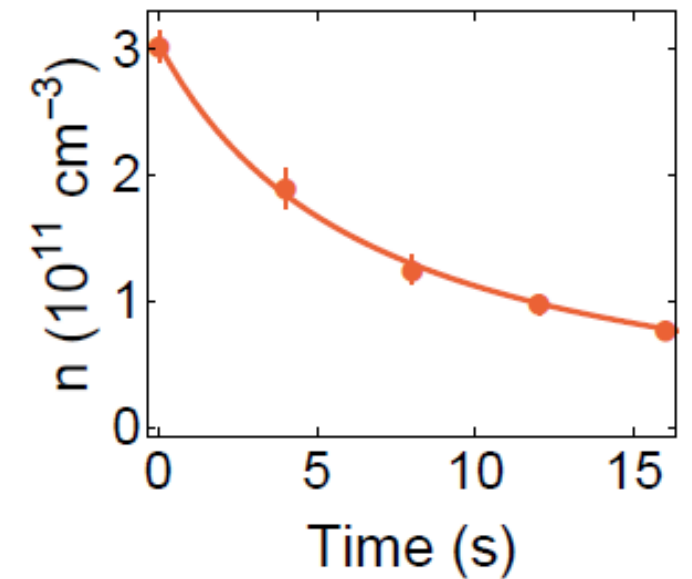
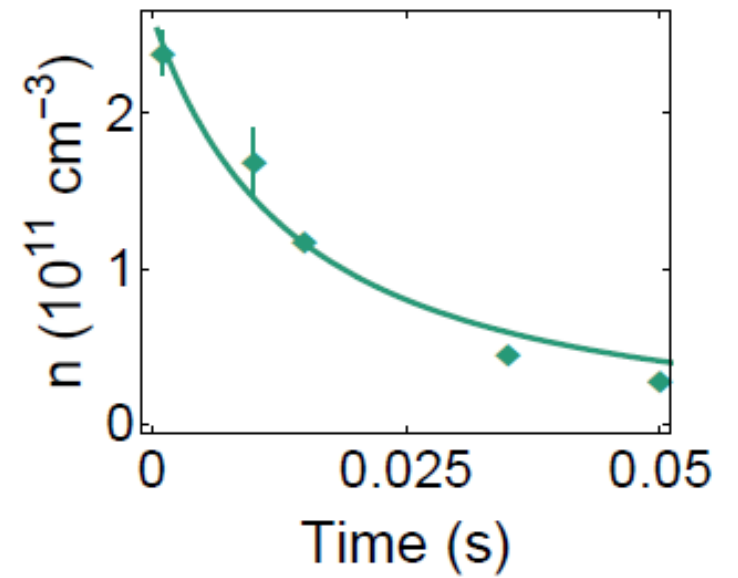
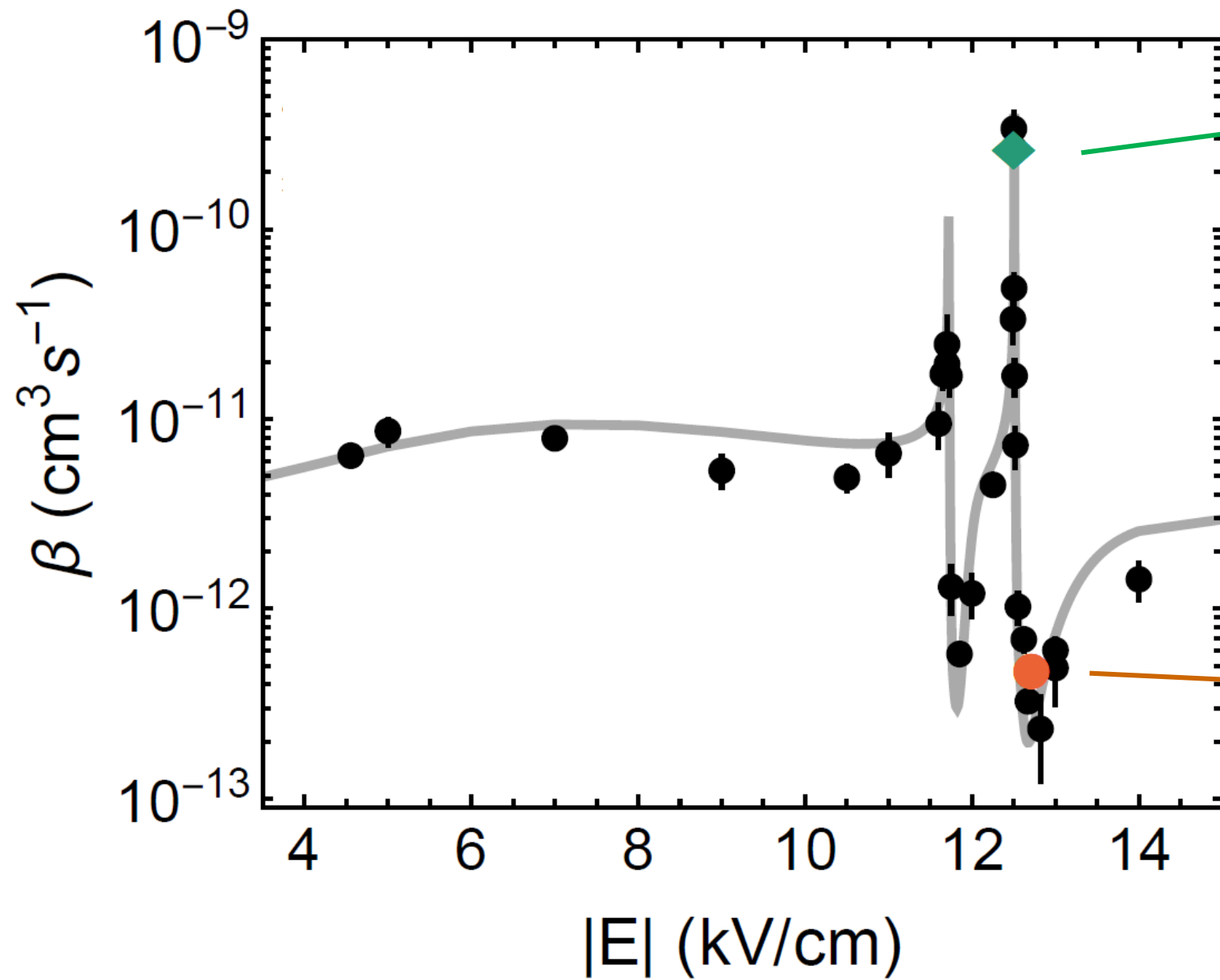


Collaboration: John Bohn, Goulven Quémener

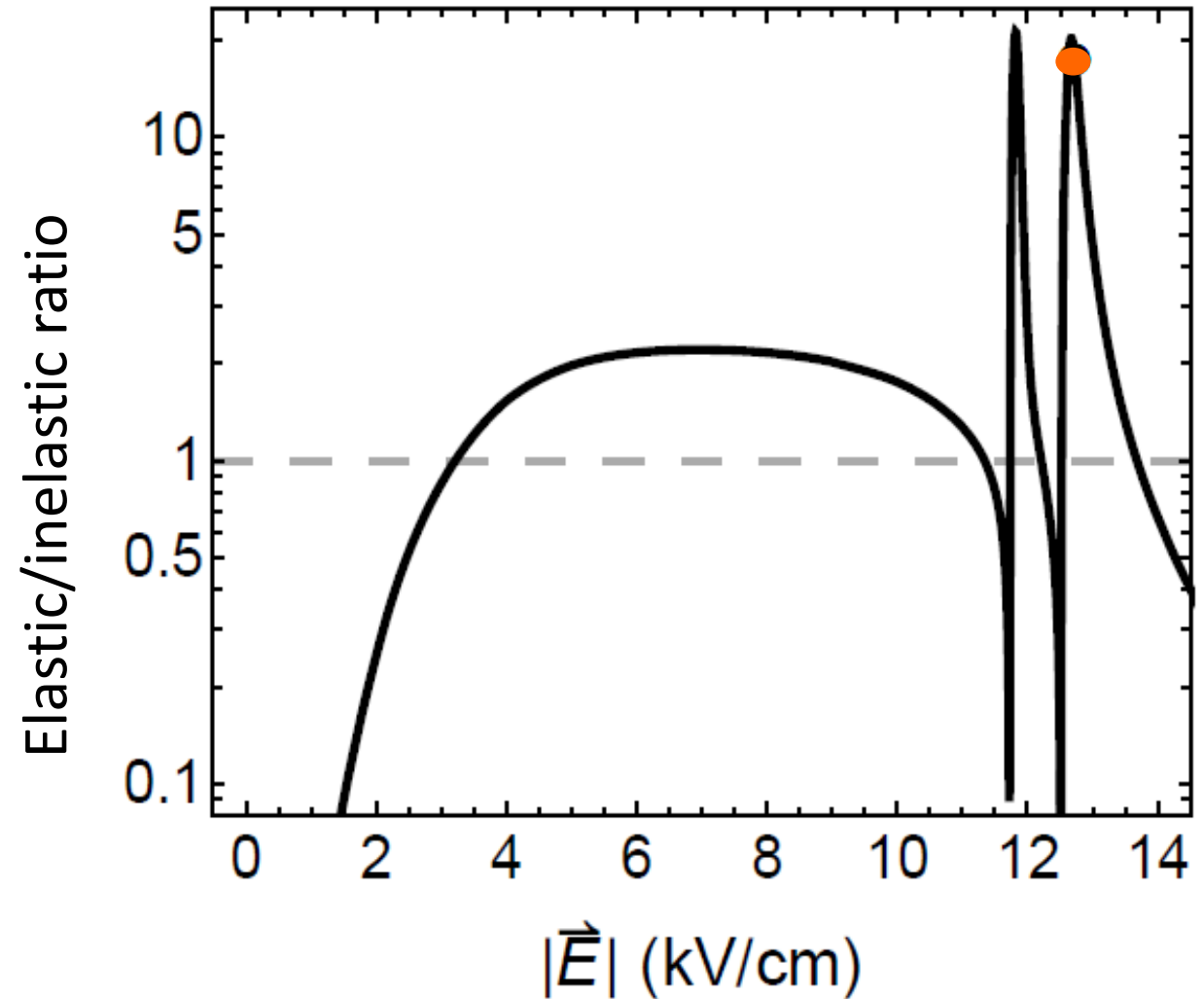
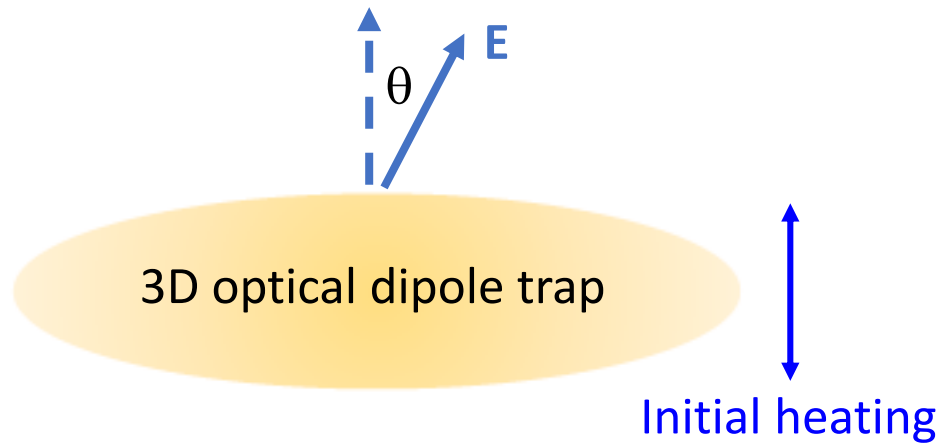


Trap frequencies: $(\omega_x, \omega_y, \omega_z) = 2\pi \times (40, 220, 40) \text{ Hz}$

Resonant shielding works in 3D !

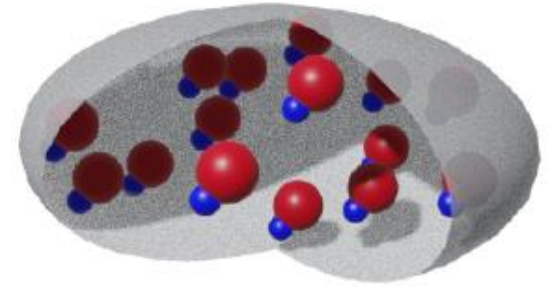
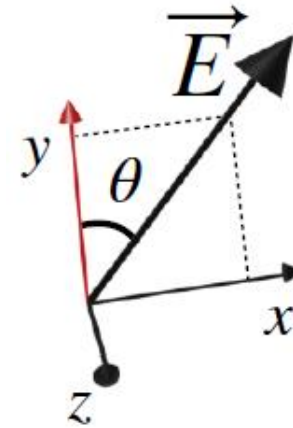


Dipolar thermalization in 3D, with reactive molecules

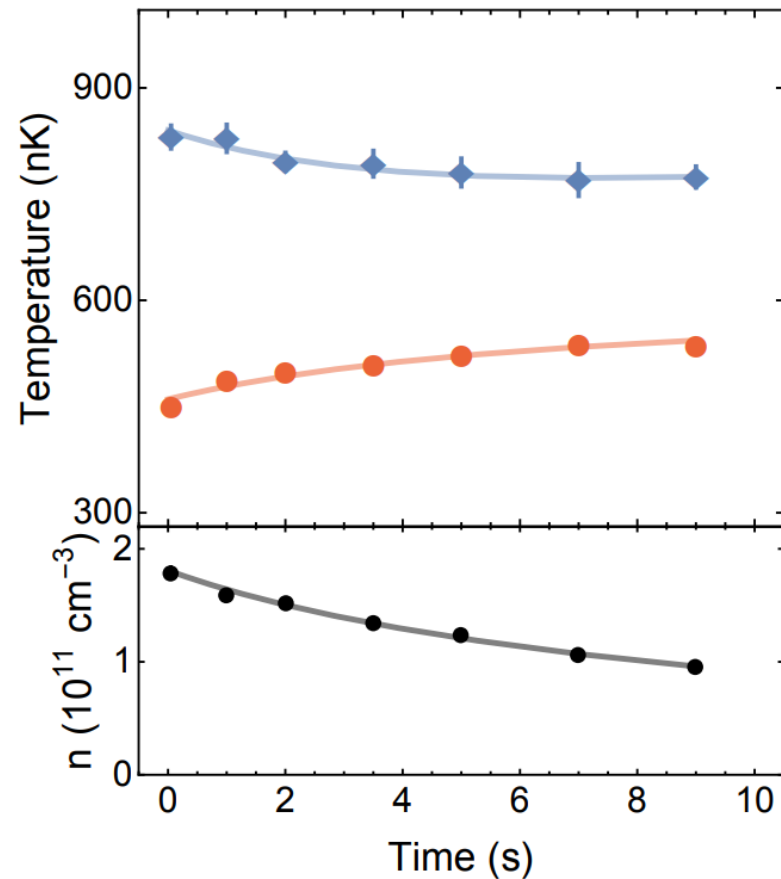


Dipolar thermalization in 3D

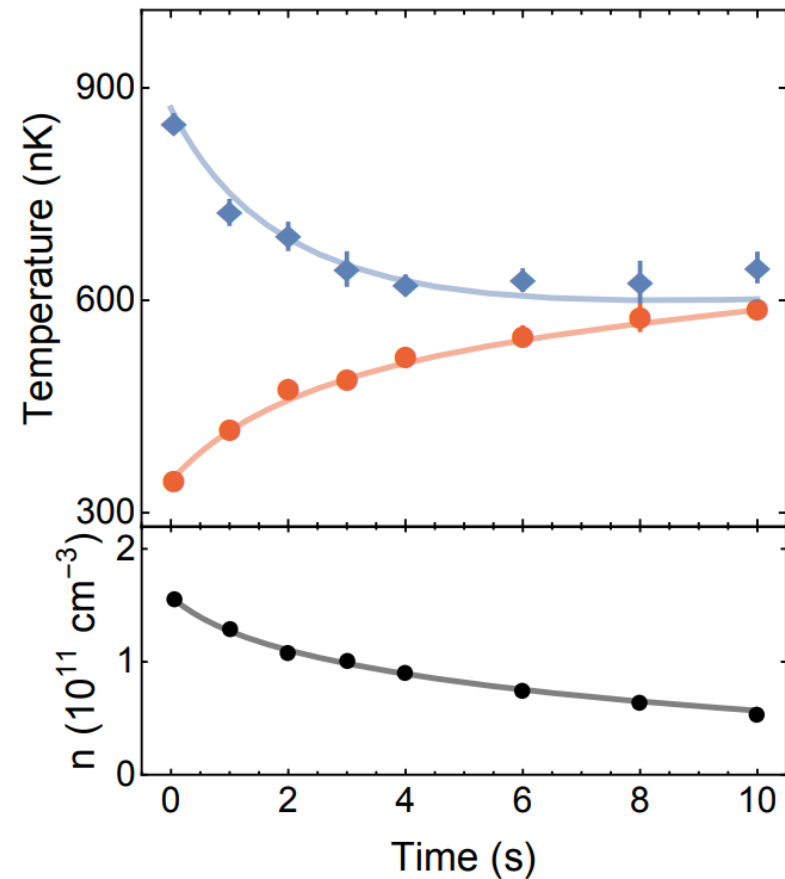
Anisotropic thermalization for magnetic atoms
(Ferlaino *et al.*, PRL 2014, Jin & Bohn PRA 2014)



$\theta = 90^\circ$

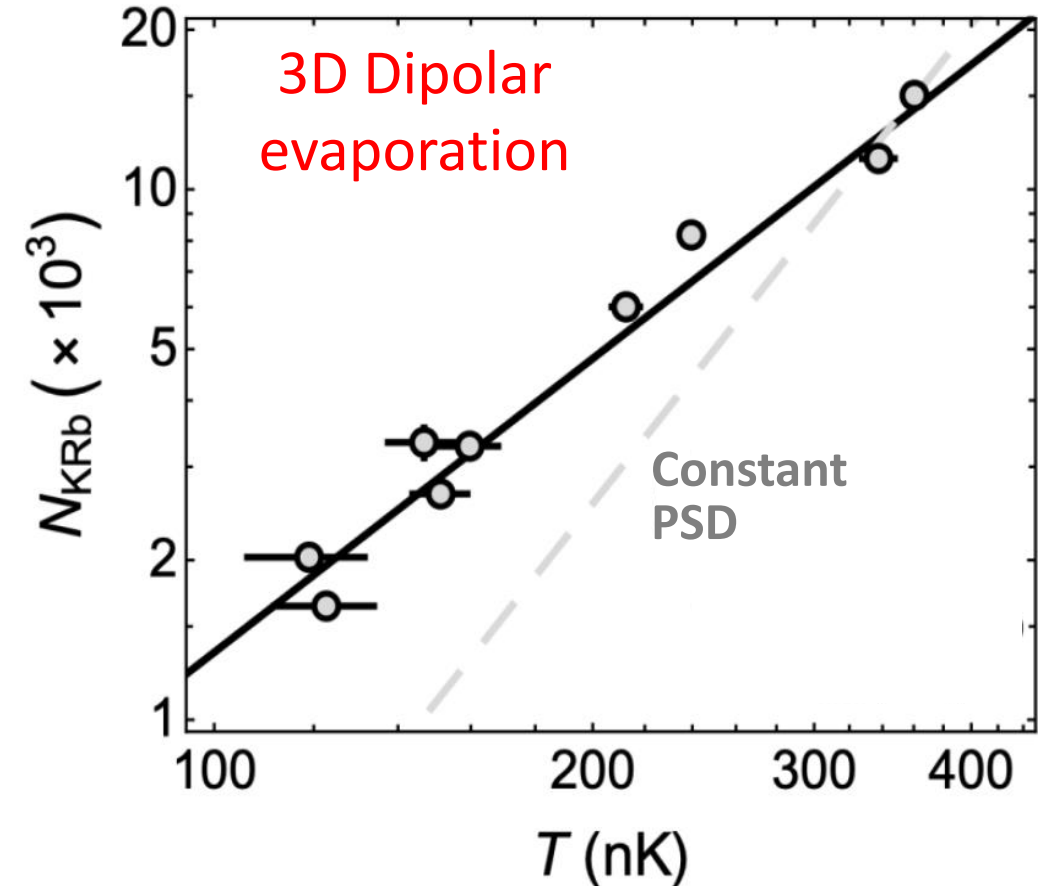
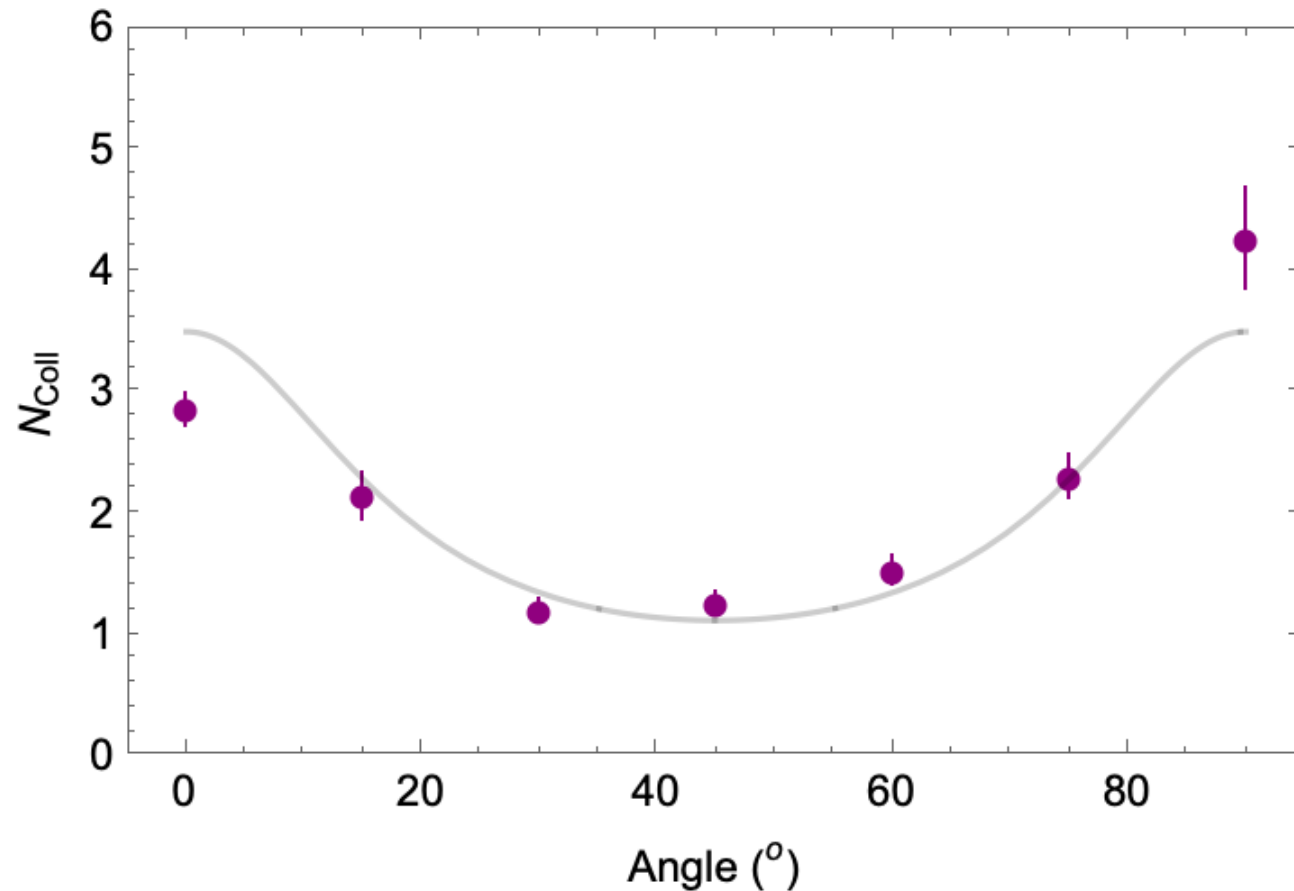
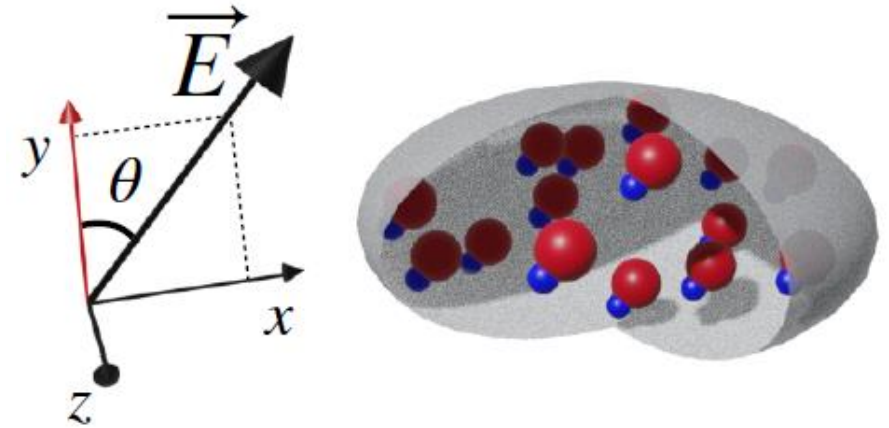


$\theta = 45^\circ$



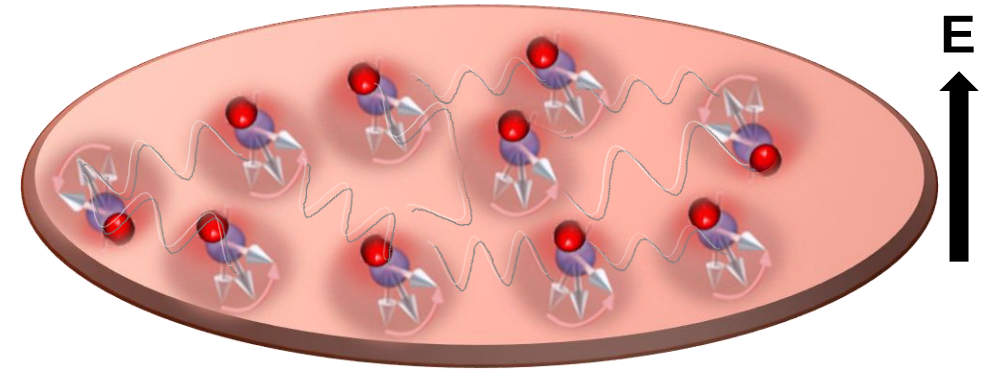
Dipolar thermalization in 3D

Anisotropic thermalization for magnetic atoms
(Ferlaino *et al.*, PRL 2014, Jin & Bohn PRA 2014)

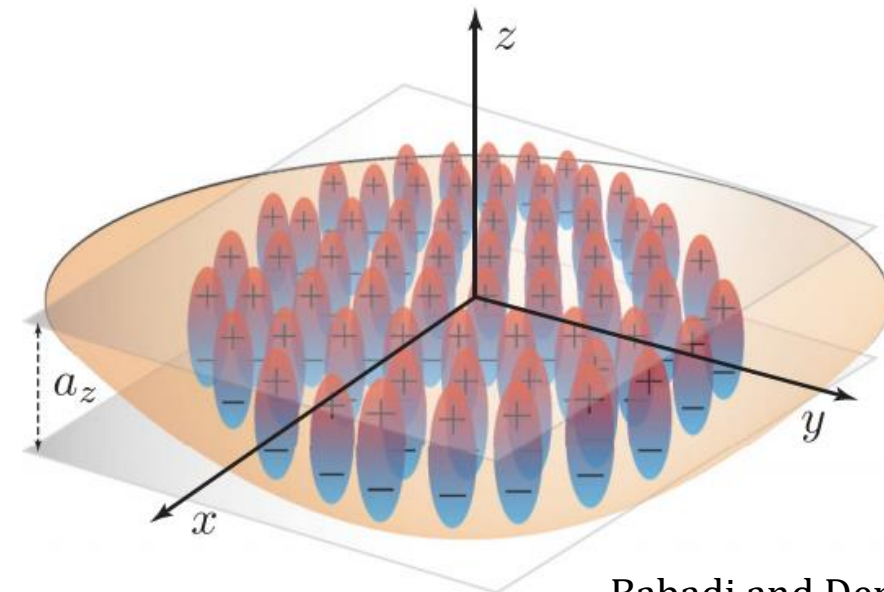


Many exciting explorations

Collective spins in 2D plane (spin squeezing)
Bilitewski *et al.*, Phys. Rev. Lett. in press (2021).



Collective hydrodynamic modes of dipolar fermions



Babadi and Demler, PRA (2012)

Bohn, Rey, Ye,
Science **357**, 1002 (2017).

Mobile molecules

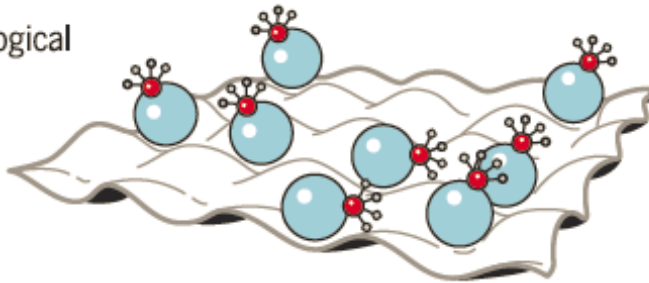
Topological superfluids
t-J models
Dipolar chains and clusters



Efficient cooling
Control of chemistry

Pinned multi-level molecules

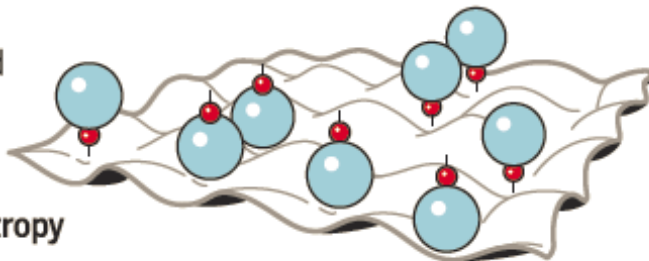
Spin-orbit coupling
Symmetry protected topological
phases
Fractional Chern insulators



Control of microwaves
Local dressing

Pinned two-level molecules

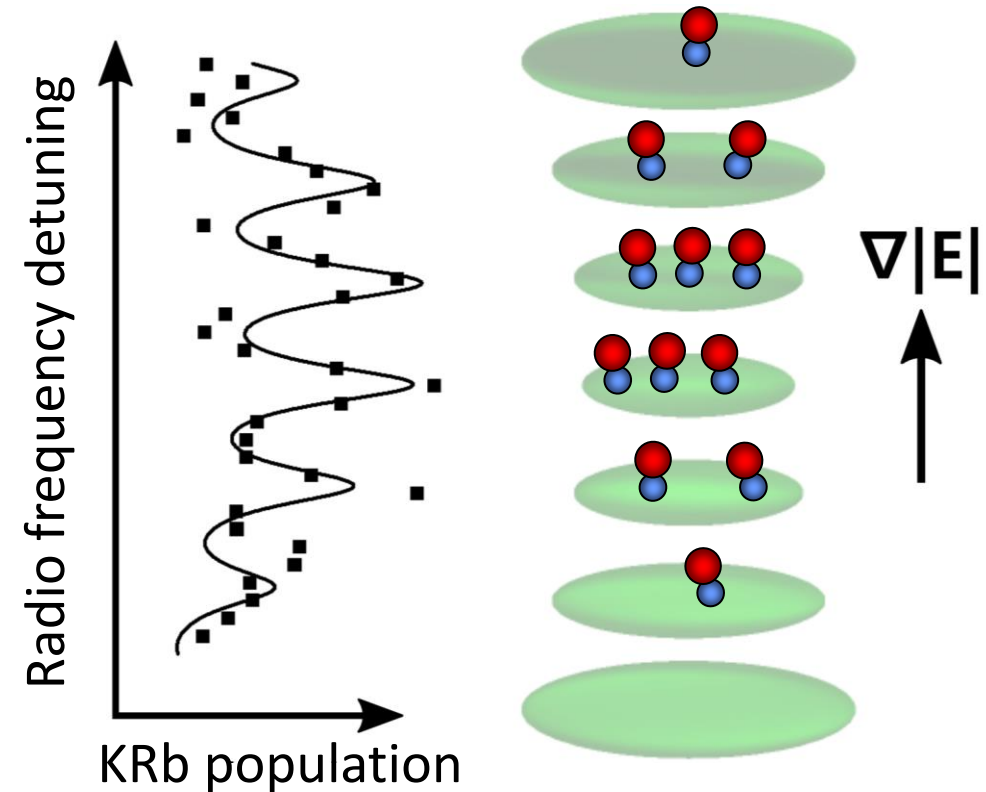
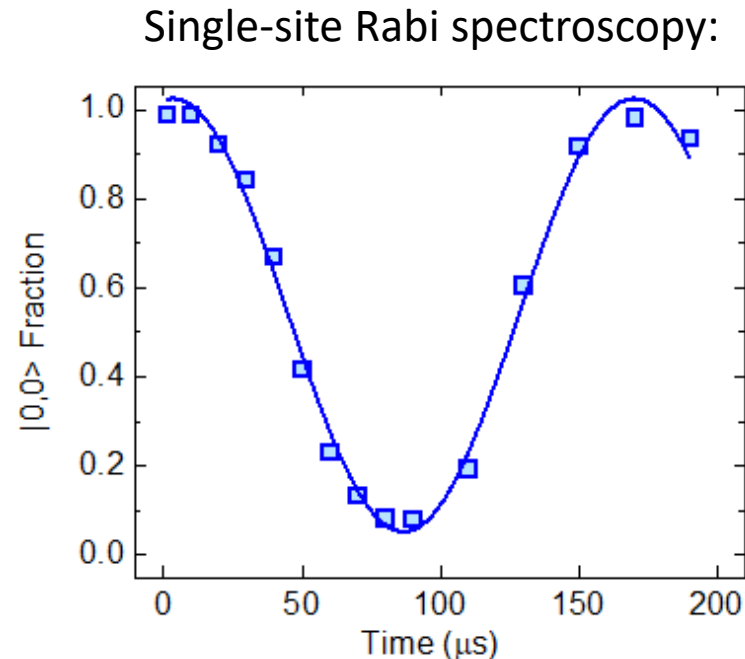
XXZ spin model
Spin liquids
Many-body localization and
transport



Control of E-fields
Higher fillings and low entropy
Addressability

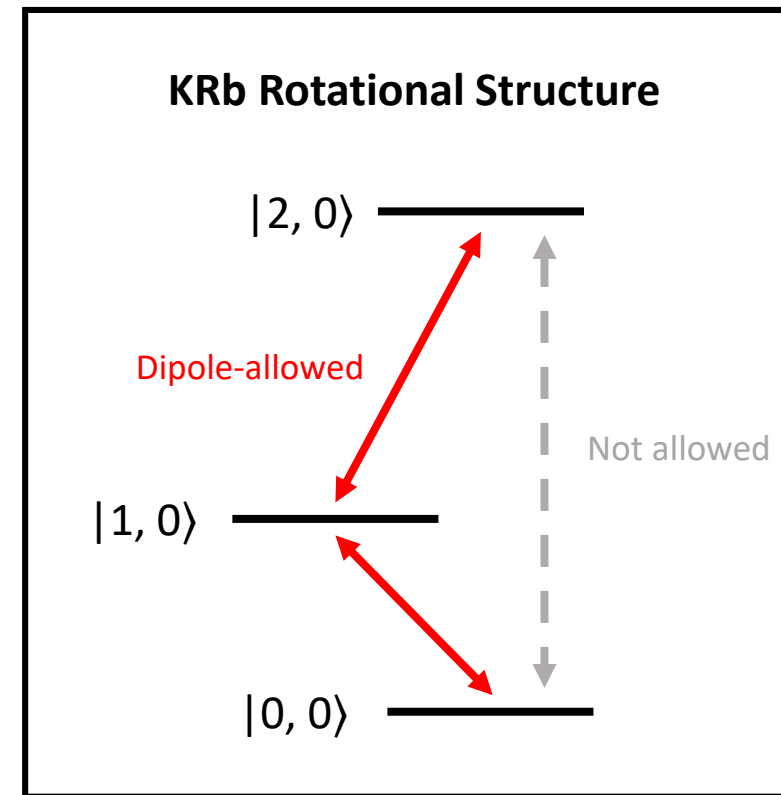
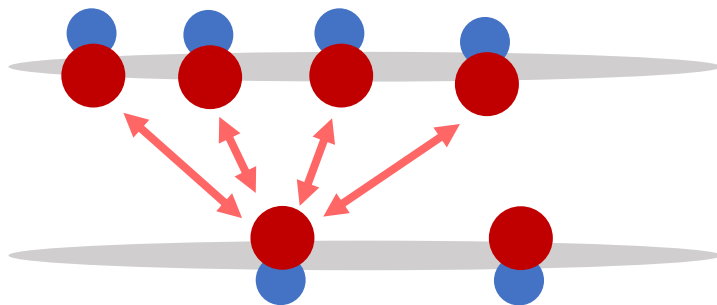
Selecting a single layer of molecules

- Molecules confined in 1D optical lattice (540 nm spacing)
- Stabilize lattice phase relative to E ; Apply ∇E along lattice
- Single-site address of the rotational transition



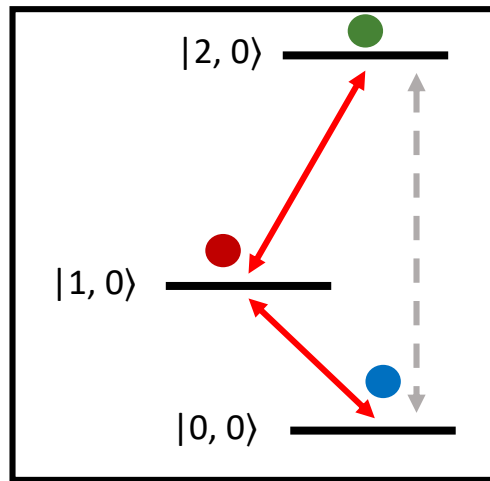
Interlayer spin exchange

- Preparing 2D layers in selected rotational states $|N, m_N\rangle$
- Spin exchange between layers allowed for $\Delta N = 1$
- Many-body effects may modify the spin exchange rate



Interlayer spin exchange

- Preparing single layer with different “spin environments” (rotational states of neighboring layers)
- Measuring loss rate of molecules from single layer
- Three conditions
 1. No neighboring layers (slow loss)
 2. Neighbors in $\Delta N = 1$ rotational state (fast loss)
 3. Neighbors in $\Delta N = 2$ rotational state (slow loss)



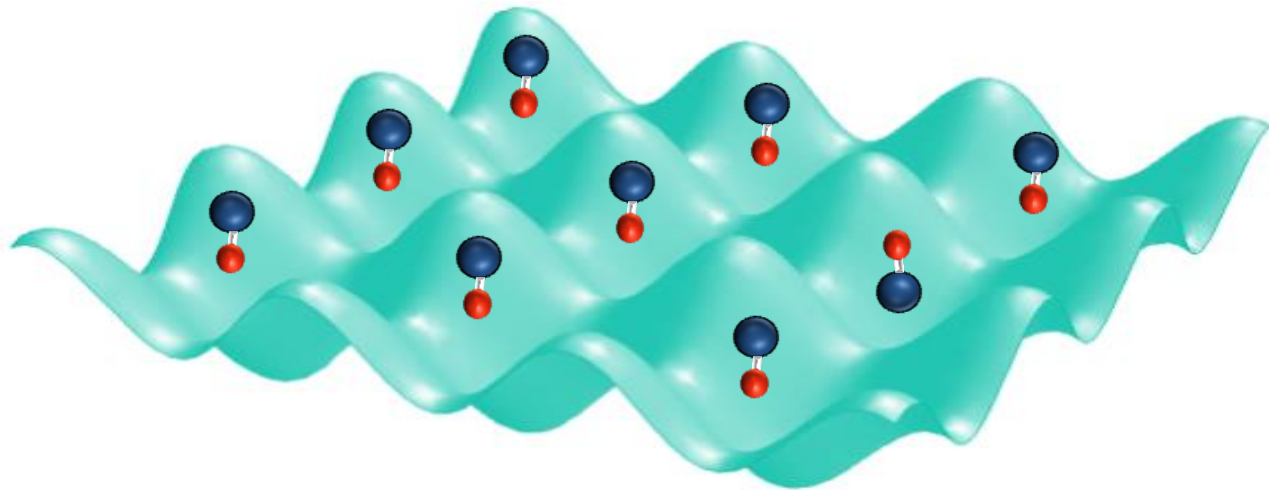
$N = 0, 1, 2$



Molecules as dipolar spins

Gorshkov *et al.*, Phys. Rev. Lett. **107**, 115301 (2011).

Molecules are physically pinned down,
but spins are exchanged & mobile



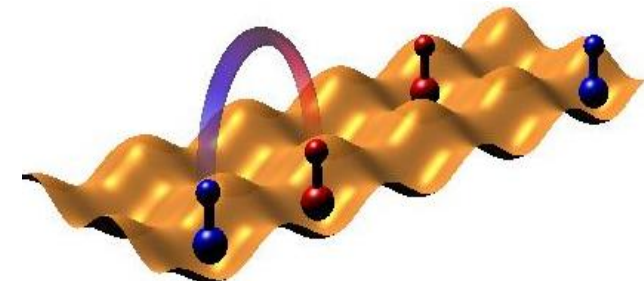
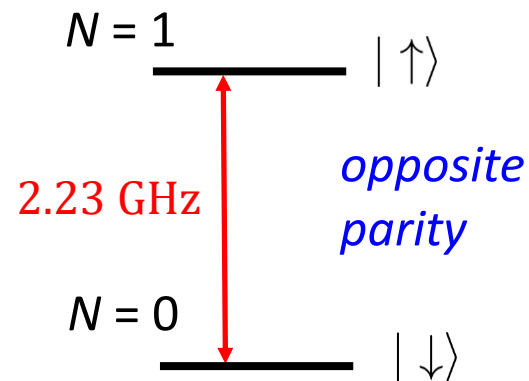
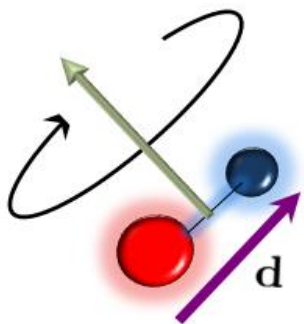
$$H = \sum_{i>j} V_{dd}(\mathbf{r}_i - \mathbf{r}_j) \left[J_z S_i^z S_j^z + \frac{J_{\perp}}{2} (S_i^+ S_j^- + S_i^- S_j^+) \right]$$



$$\frac{1 - 3 \cos^2 \theta_{ij}}{|\mathbf{r}_i - \mathbf{r}_j|^3}$$

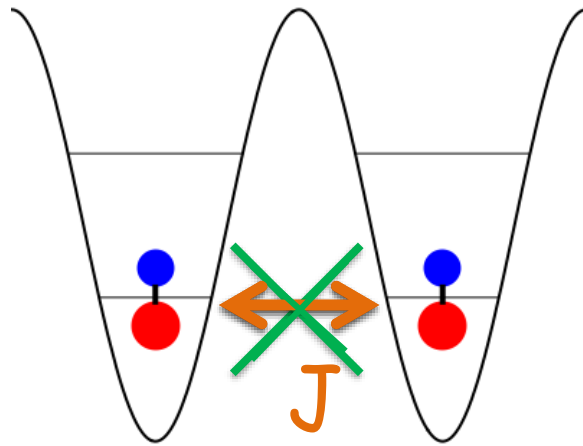
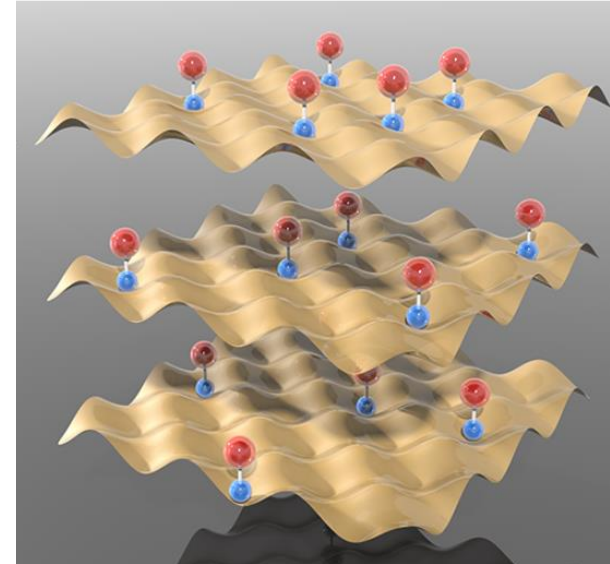
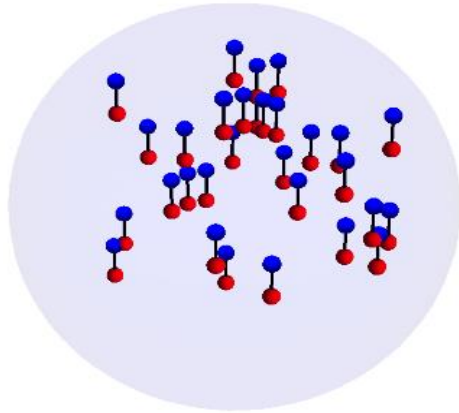
Ising $J_z \sim (d_{\uparrow} - d_{\downarrow})^2$

Spin exchange $J_{\perp} \sim d_{\uparrow\downarrow}^2 \sim 100 \text{ Hz}$

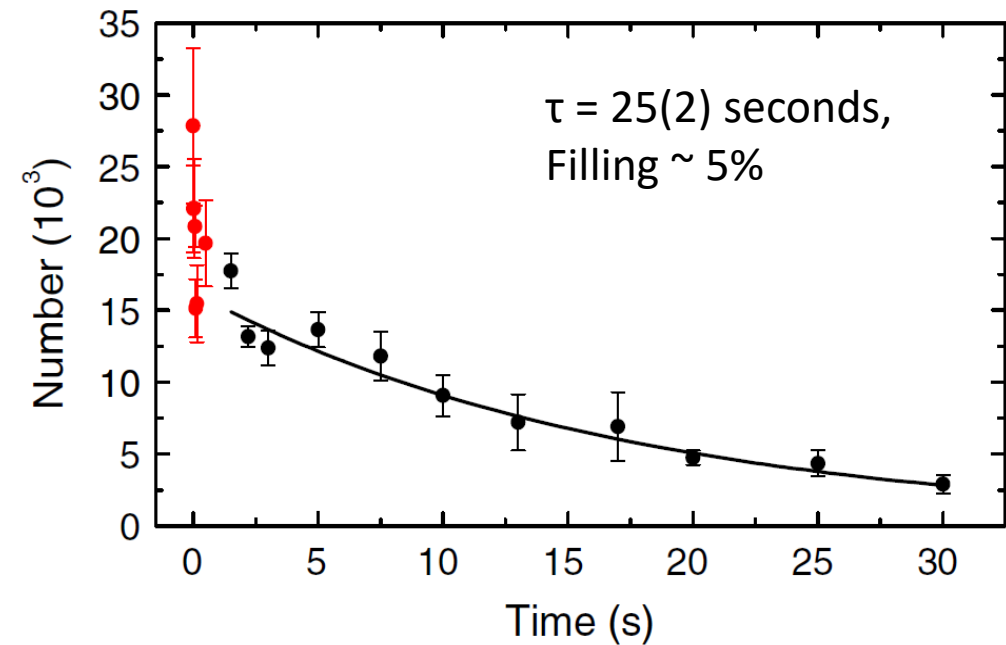


Putting dipoles in a 3D lattice

Chotia *et al.*, PRL **108**, 080405 (2012); Zhu *et al.*, PRL **112**, 070404 (2014).



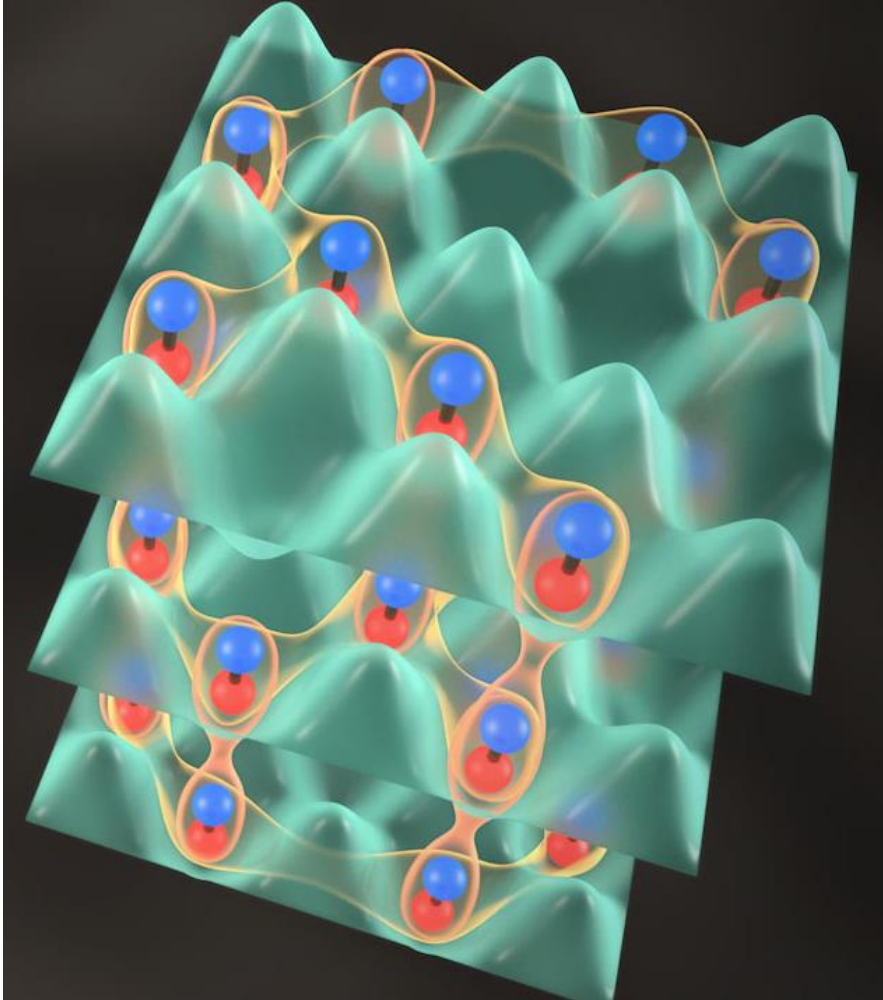
Pauli exclusion
Interaction blockade



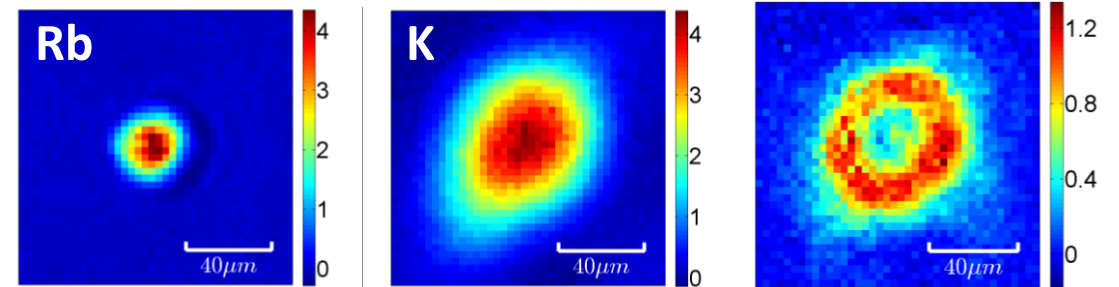
Synthesis of molecular matter

Moses *et al.*, Science **350**, 659 (2015).

KRb: 1.5×10^3 , $\sim 25\%$ filling



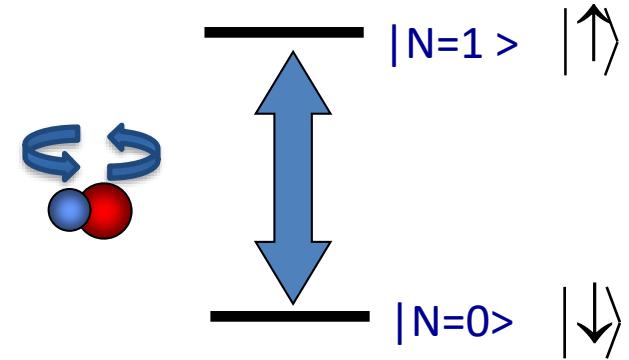
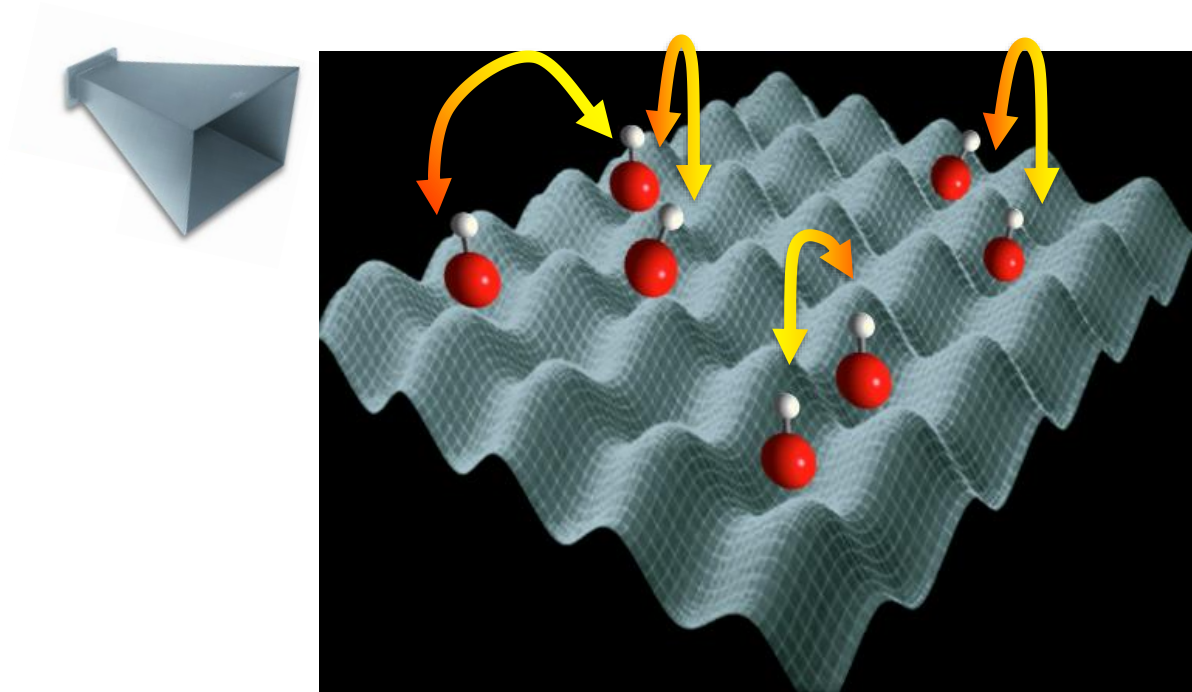
Dual Mott (Rb) / band (K) insulator



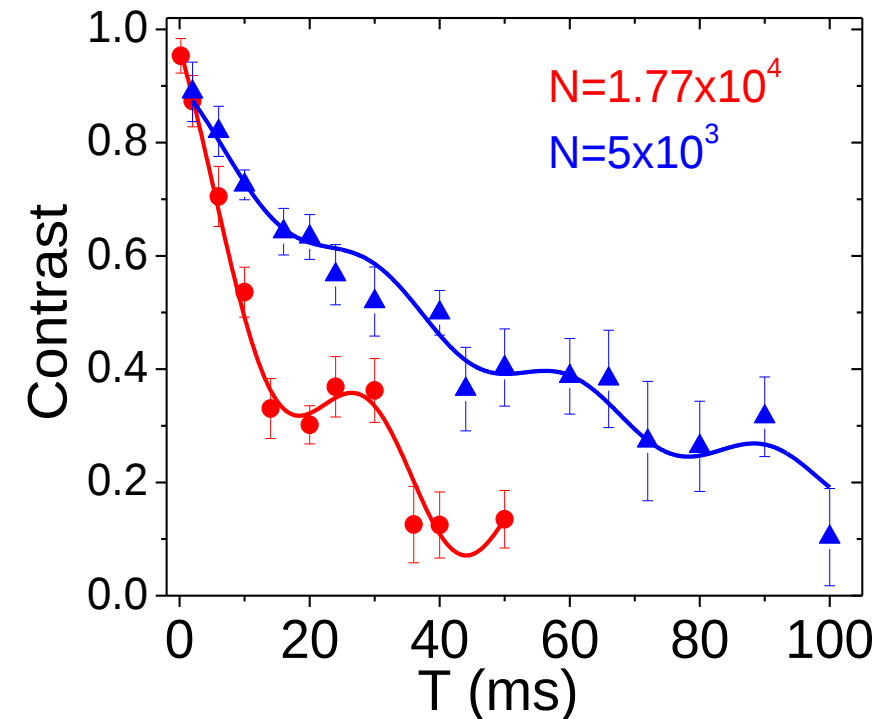
Sites with one atom of each species

A Dipolar Spin Lattice

Yan *et al.*, Nature **501**, 521 (2013); Hazzard *et al.*, Phys. Rev. Lett. **113**, 195302 (2014).

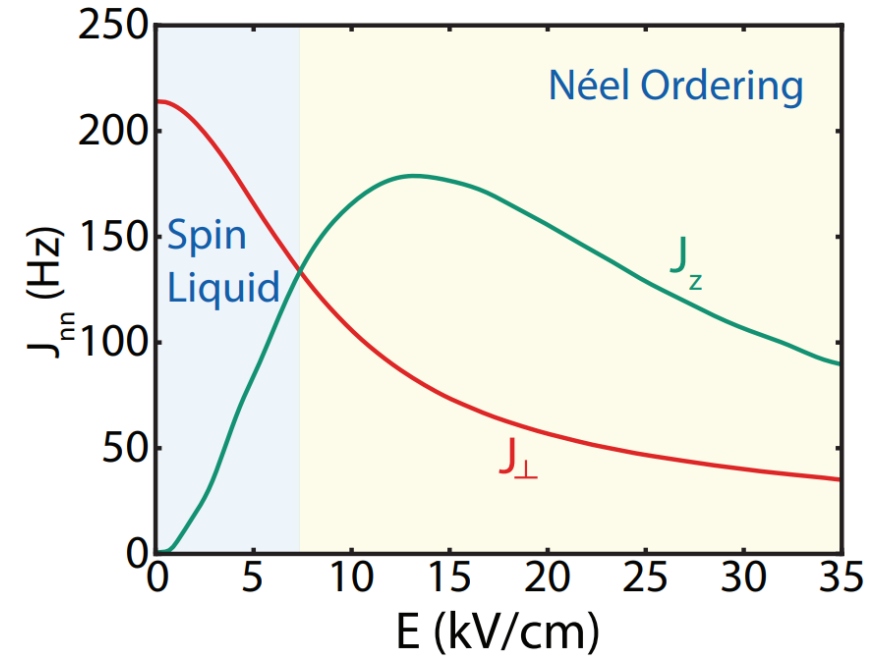
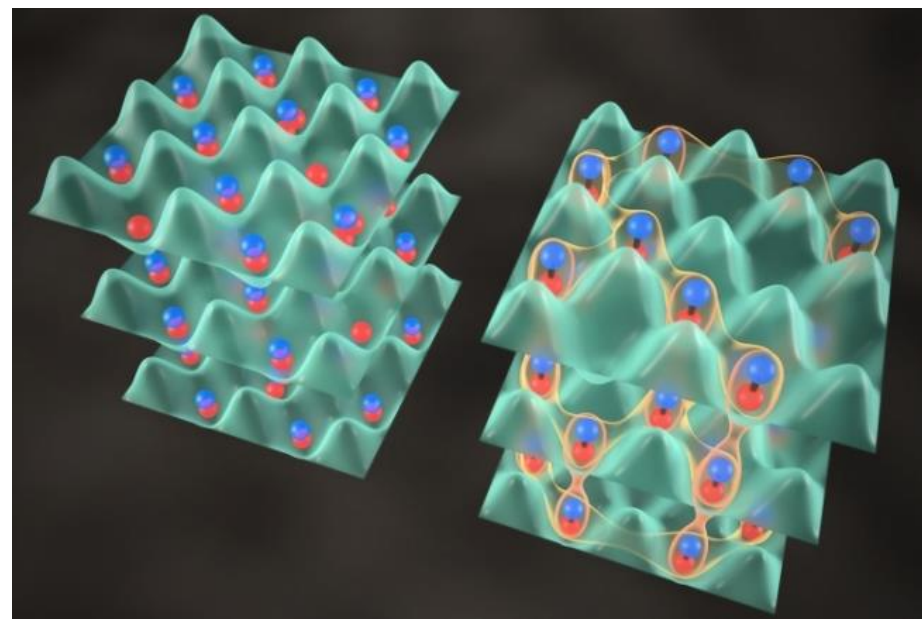


- Start with $N=0$. $|\downarrow\rangle$
- Drive a coherent spin superposition. $\frac{1}{\sqrt{2}}(|\uparrow\rangle + |\downarrow\rangle)$
- Probe spin coherence at T . (Ramsey spectroscopy)



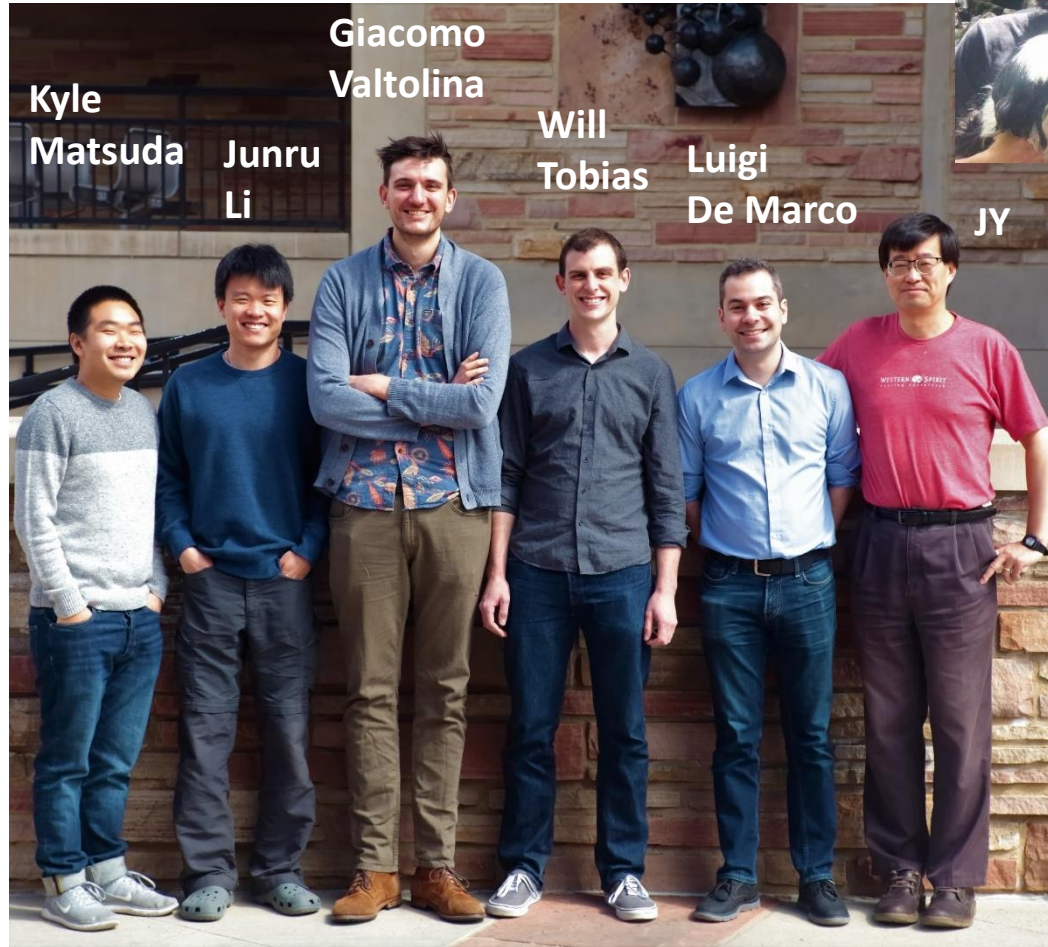
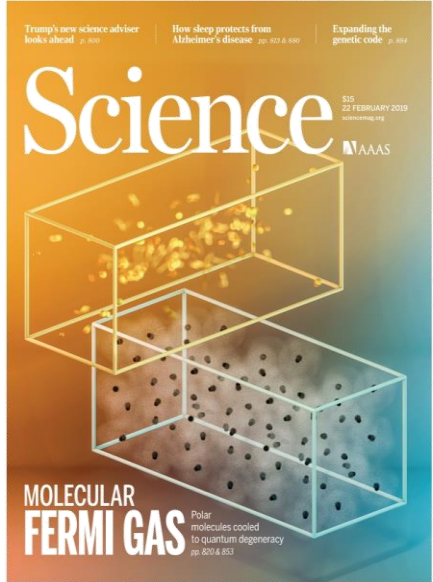
A Dipolar Spin Lattice

$$H = \frac{1}{2} \sum_{i \neq j} V_{\text{dd}}(i, j) \left[J_z S_i^z S_j^z + \frac{J_{\perp}}{2} (S_i^+ S_j^- + \text{H.c.}) \right]$$

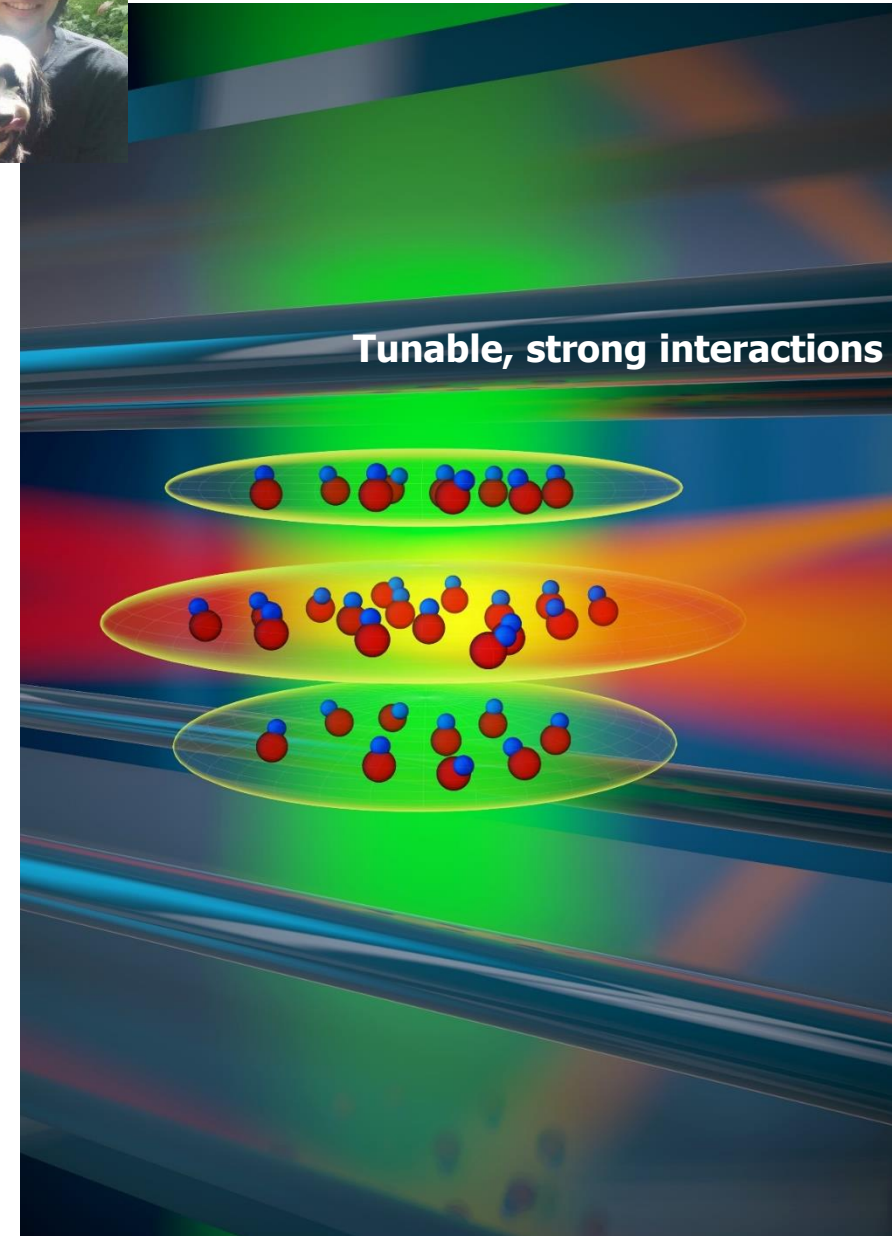


- Exploring phase transition ($J_{\perp}/J_z$)
- Transport and localization
- Exotic lattice geometries (long-range interactions + frustration)
- Spin-orbit coupling
- Pair production using shielding resonance ($|1,0\rangle|1,0\rangle \rightarrow |0,0\rangle|2,0\rangle$)
- Microwave dressing & Floquet dynamics

Future plans



Calder
Miller



Theory Collaborations

John Bohn, Goulven Quéméner (Dipolar collisions)
Ana Maria Rey (Spin squeezing, lattice spin model)
Eugene Demler (Dipole-mediated hydrodynamics)
Svetlana Kotochigova (Coherence)
Norm Yao, Baranov/Peter Zoller (Many-body, exotic quantum phenomena)