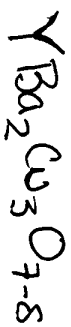
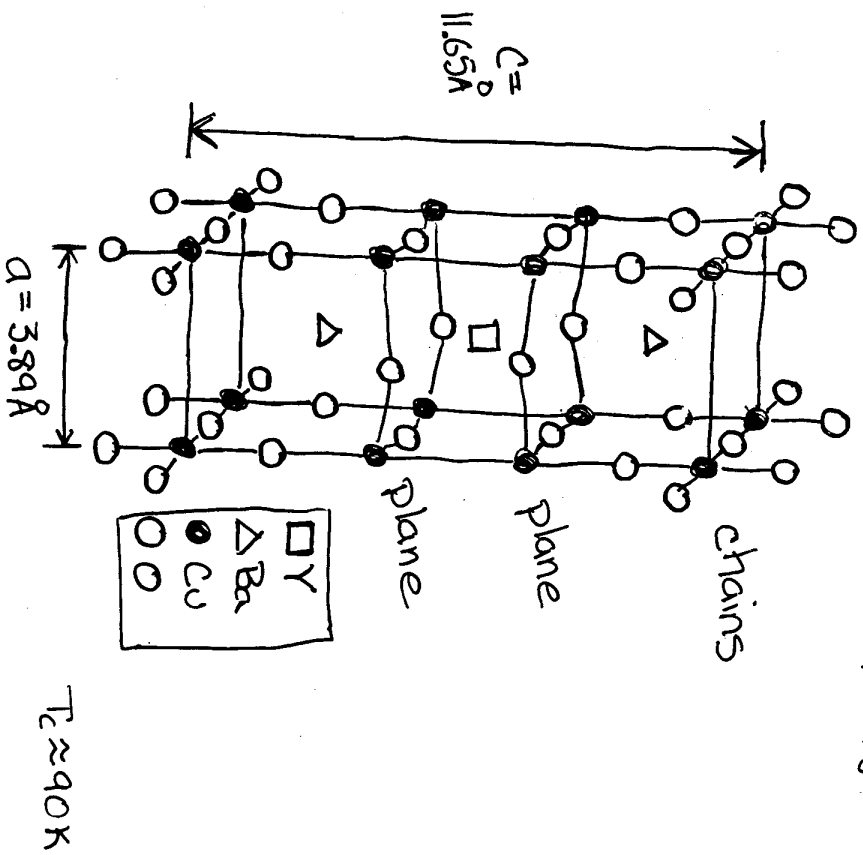


②



drawn for $\delta=0$
(fully oxygenated)



Moler
Lecture 2

①

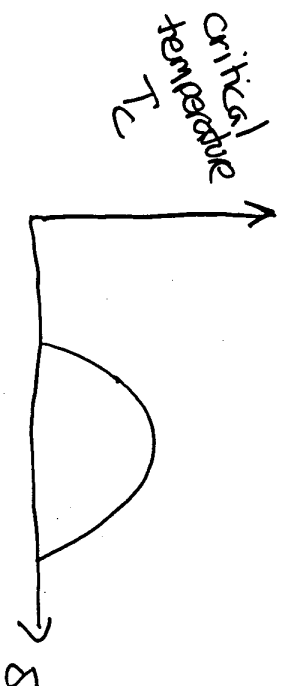
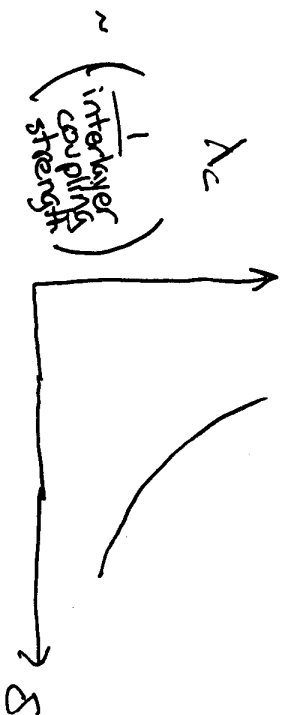
Interlayer Tunneling in Cuprate Superconductors

KAM July 5 2000

1. There is interlayer tunneling, and the Lawrence-Doniach model provides a pretty good phenomenological description.
2. The Inter-layer Tunneling (ILT) model proposed as a mechanism for high- T_c has testable experimental consequences.

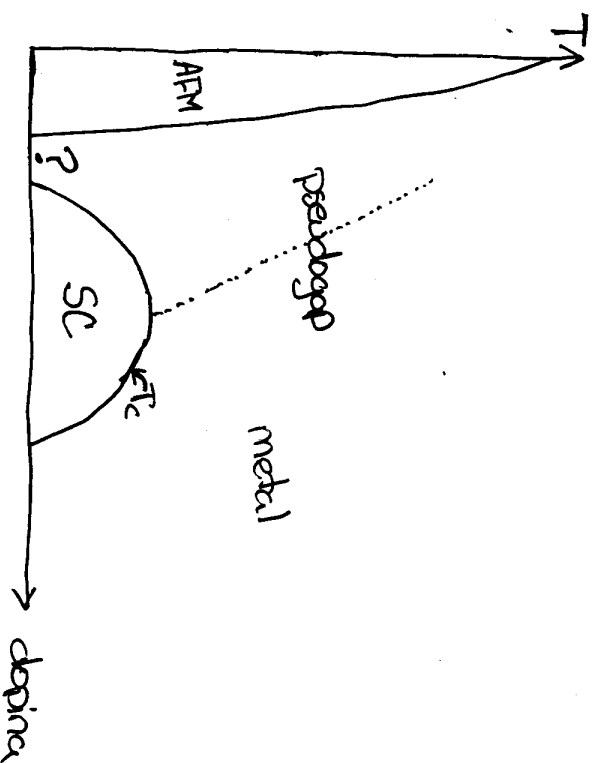
⑦

CARRIER DOPING ALSO HAS A RADICAL BUT DIFFERENT EFFECT ON THE INTERLAYER COUPLING:



③

CARRIER DOPING HAS A RADICAL EFFECT ON THE PHYSICS



⑥

Popular School of Thought:

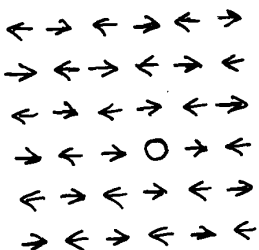
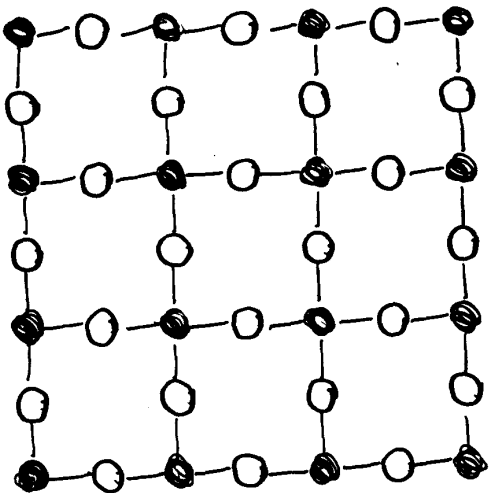
Superconductivity occurs because of an in-plane mechanism

but we don't need to know what it is to describe these materials quite well phenomenologically

⑤

Copper Oxide Planes

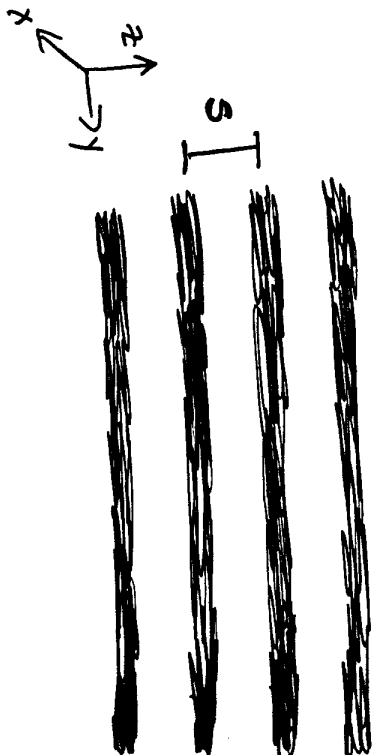
● Copper
○ Oxygen



t-J model
antiferromagnetism (J)
plus hopping (t)

⑧

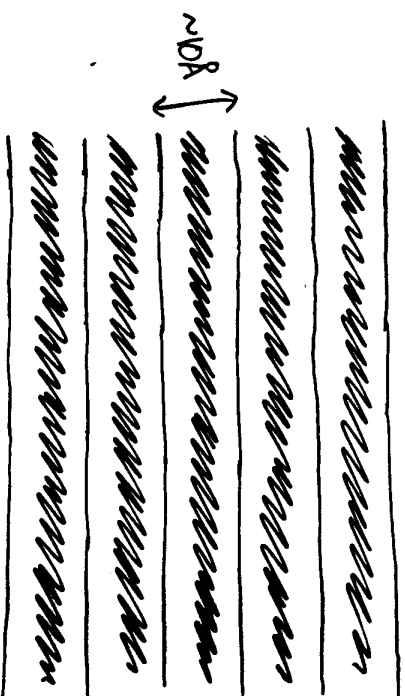
Lawrence-Doniach Model 1971



④ $\psi_n(x, y)$ in plane
 $J_c \sin(\phi_n - \phi_{n-1})$
 Josephson coupling
 between planes

⑦

One way to look at cuprate superconductors:



copper oxide plane
 (superconducts)

stuff

- charge reservoir
- doesn't superconduct

Lawrence-Vonica equation:

$$\begin{aligned} & \propto \psi_n + \beta |\psi_n|^2 \psi_n - \frac{\hbar^2}{2m_b} \left(\vec{\nabla} - i \frac{2e}{\hbar c} \vec{A} \right)^2 \psi_n & \vec{\nabla} = \hat{x} \frac{\partial}{\partial x} + \hat{y} \frac{\partial}{\partial y} \\ & - \frac{\hbar^2}{2m_c s^2} |\psi_{n+1} e^{-2ieA_z s / \hbar c} - 2\psi_n + \psi_{n-1} e^{2ieA_z s / \hbar c}|^2 = 0 & \vec{A} = A_x \hat{x} + A_z \hat{z} \end{aligned}$$

for smoothly varying ψ , this reduces to
Anisotropic Ginzburg-Landau:

$$\propto \psi + \beta |\psi|^2 \psi - \frac{\hbar^2}{2} \left(\vec{\nabla} - i \frac{2e}{\hbar c} \vec{A} \right) \cdot \frac{1}{m} \cdot \left(\vec{\nabla} - i \frac{2e}{\hbar c} \vec{A} \right) \psi = 0$$

$$\begin{aligned} \vec{\nabla} &= \hat{x} \frac{\partial}{\partial x} + \hat{y} \frac{\partial}{\partial y} + \hat{z} \frac{\partial}{\partial z} \\ \vec{A} &= A_x \hat{x} + A_y \hat{y} + A_z \hat{z} \end{aligned}$$

$\frac{1}{m}$ reciprocal mass tensor
weak interlayer coupling $\Rightarrow m_c \gg m_b$

Ginzburg-Landau free energy in the absence of terms

$$\textcircled{6} \quad F = \int d^3x \left[\kappa |\psi|^2 + \frac{1}{2} \beta |\psi|^4 + \frac{1}{2m^*} \left| \frac{\hbar}{i} \vec{\nabla} \psi \right|^2 \right] dx dy dz$$

Lawrence-Vonica free energy:

$$\begin{aligned} F = \int d^3x & \left[\kappa |\psi_n|^2 + \frac{1}{2} \beta |\psi_n|^4 + \frac{\hbar^2}{2m_b} \left(\left| \frac{\partial \psi_n}{\partial x} \right|^2 + \left| \frac{\partial \psi_n}{\partial y} \right|^2 \right) \right. \\ & \left. + \frac{\hbar^2}{2m_c s^2} |\psi_n - \psi_{n-1}|^2 \right] dx dy \end{aligned}$$

aside: setting $\psi_n = |\psi_n| e^{-i\phi_n}$ and $\psi_{n-1} = |\psi_{n-1}| e^{-i\phi_{n-1}}$,
the last term becomes

$$\frac{\hbar^2}{m_c s^2} |\psi_n|^2 [1 - \cos(\phi_n - \phi_{n-1})]$$

which looks like a Josephson coupling energy
(you can think of either J_c or m_c as being
the intrinsic parameter)

②

Phenomenology of high- T_c in LD model: 1

anisotropic
coherence
length

$$\xi_i^2(T) = \frac{\hbar^2}{2m_i |v_i(T)|}$$

thermodynamic
critical
field

$$H_c(T) = \frac{\Phi_0}{2\sqrt{2}\pi \xi_i(T) \lambda_i(T)}$$

cannot depend on i

penetration
depth

$$\lambda_{ab} \sim 0.1 - 0.2 \mu m$$

$$\lambda_c \sim 1 \mu \rightarrow \text{larger than sample}$$

anisotropy
parameter

$$\gamma = \left(\frac{m_c}{m_{ab}} \right)^{1/2} = \frac{\lambda_c}{\lambda_{ab}} = \frac{\xi_{ab}}{\xi_c}$$

$$\sim 7 \text{ YBCO}$$

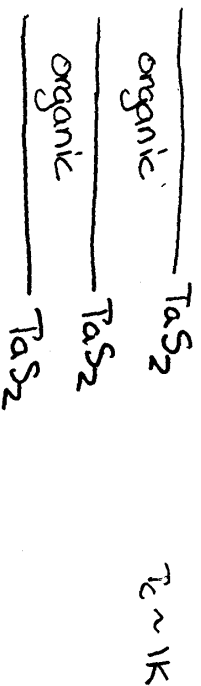
$$> 100 \text{ BiSCCO}$$

$$\text{both } T_c \approx 90K$$

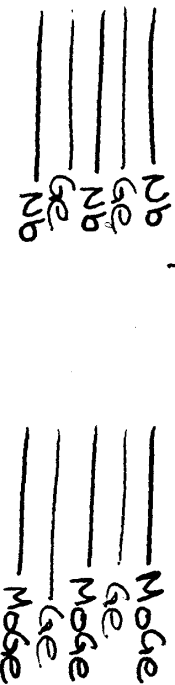
③

Lawrence - Doniach model applied to:

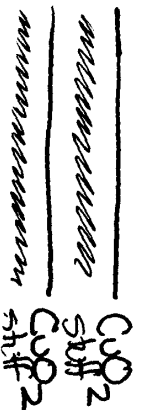
• Transition-metal dichalcogenides



• Artificial multilayers

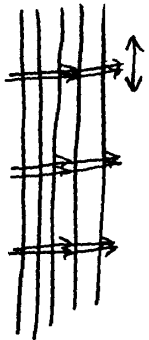


• Cuprate superconductors



(7)

LD phenomenology in high- T_c : 2
"pancake vortices" and 3D-2D behavior



flux tubes or
vortices
parallel to c-axis

vortex core size: ξ_{ab}

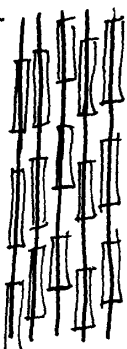
magnetic flux size: λ_{ab}

vortex spacing: $\sqrt{\Phi_0/3}$



thermal, quantum, and pinning effects

extreme 2D limit:

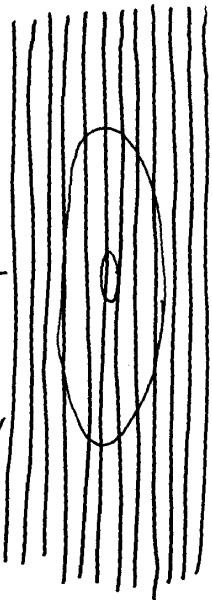


decoupled "pancake" vortices

(13)

LD phenomenology in high- T_c : 3
"interlayer Josephson vortex"

$\xi_c \uparrow \lambda_{ab} \downarrow$



vortices parallel
to a-axis

λ_c
 ξ_{ab}

Josephson core:
vortex core "fits between"
layers

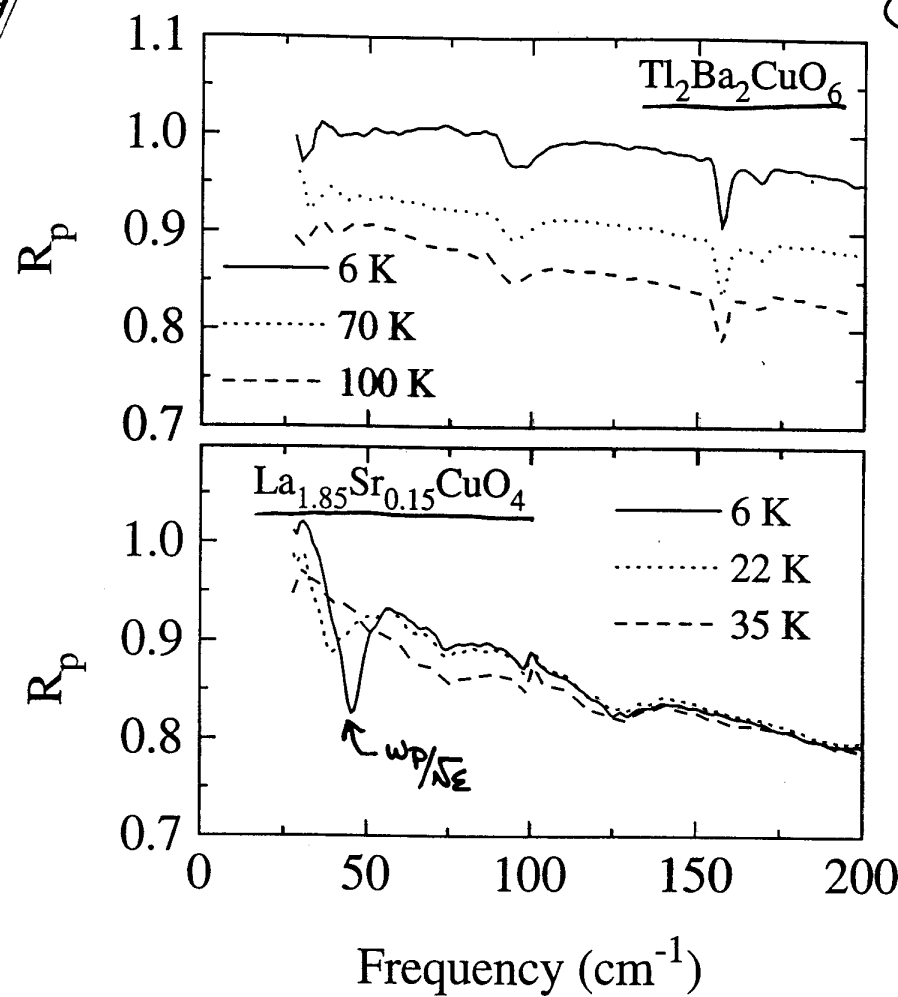
vortex in isotropic GL:

$$B(x,y) = \frac{\Phi_0}{2\pi\lambda^2} K_0 \left(\sqrt{\left(\frac{y}{\lambda}\right)^2 + \left(\frac{z}{\lambda_c}\right)^2} \right)$$

vortex in LD:

$$B(x,y) = \frac{\Phi_0}{2\pi\lambda\lambda_c} K_0 \left(\sqrt{\left(\frac{y}{\lambda_c}\right)^2 + \left(\frac{x}{\lambda_c}\right)^2 + \left(\frac{z}{\lambda_c}\right)^2} \right)$$

16



$$\lambda_c = \frac{c}{2\pi f_p}$$

Schützmann et al
TL-2201 lower limit
 $\frac{1}{(2\pi)100\text{cm}^{-1}} = 16\mu\text{m} < \lambda_c$

15

LD phenomenology in high- T_c : 4

Josephson plasma resonance

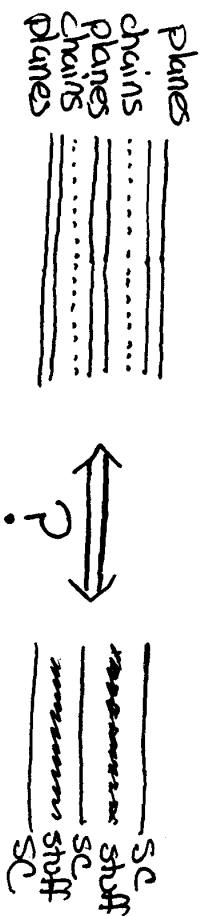
$$\omega_p = \frac{1}{2\pi\sqrt{\epsilon}} \frac{1}{\lambda_c}$$

dielectric constant of interlayer medium

characteristic frequencies: far-infrared to microwave

18

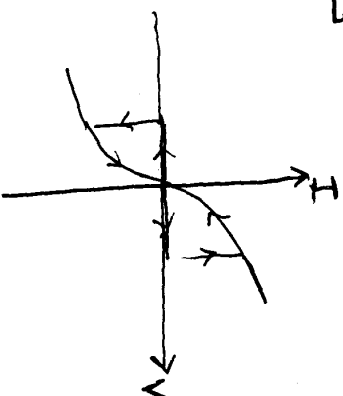
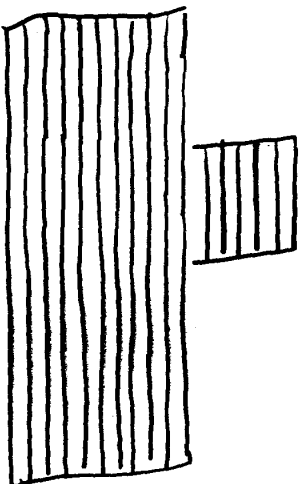
Qualitative fly in the ointment:



17

LD phenomenology: 5

direct observation of Josephson Junction behavior in BSCCO mesas



19

Naive model for c-axis tunneling:

Ambegaokar-Baratoff

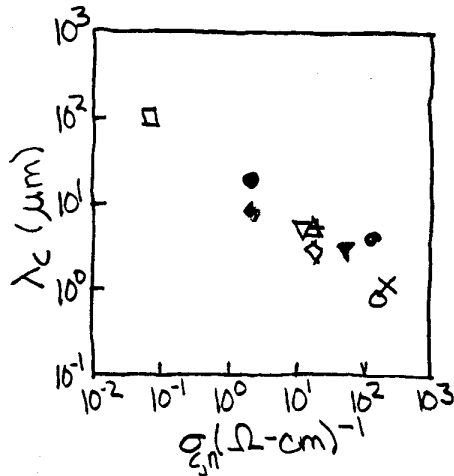
(diffusive transfer of s-wave pairs)

$$J_0 = \frac{\pi \Delta_0}{2e \rho_{c,n}} \quad \lambda_c = \sqrt{\frac{c \Phi_0}{8\pi^2 s J_0}}$$

- problems:
- what's $\rho_{c,n}$ ($T=4K, H \approx 0$)?
 - effective mass (Das Sarma)
 - d-wave

$$\lambda_c \approx 6 \mu \text{ (Tl-2201)}$$

$$\lambda_c \approx 8 \mu \text{ (Hg-1201)}$$



adapted from
Basov et al

20

Quantitative fit in the environment:

LD gives a good description if λ_{ab} and λ_c are free parameters but are they related to microscopic parameters in the way you'd expect for a stack of coupled Josephson junctions?

(22)

Interlayer Tunneling (ILT) Model



tunneling inhibited in normal state
 $\therefore$ c-axis kinetic energy saved
 in superconducting state

caution 1: ILT model $\neq$ interlayer tunneling

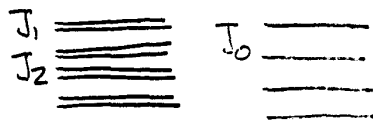
caution 2: ILT model $\neq$ Anderson-Chakravarty model

- non-observation of ω_p in Tl-2201 $\Rightarrow \lambda_c \geq 15\mu$
 (Groningen) $\omega_p = \frac{c}{2\pi\lambda_c}$

- quantitative pre-requisite (Leggett) known geometrical factor
 $\lambda_{ILT} = \frac{A}{(E_c)^{1/2}}$
 $\lambda_c = \frac{\lambda_{ILT}}{2\eta^{1/2}}$
 $\nwarrow$ condensation energy

$\eta \approx$ fraction of condensation energy which could come from c-axis K.E. savings

- best tested on single-layer high- T_c material



Tl-2201	$\lambda_{ILT} \sim 1\mu$
Hg-1201	$\lambda_{ILT} \sim 1\mu$
LSCO	$\lambda_{ILT} \sim 3\mu$

(21)

"Conventional" estimates for λ_c in Tl-2201

specular transmission
 (parallel momentum conserved)

$$\lambda_c \approx 1\mu$$

diffusive transmission
 (parallel momentum not conserved)

$$\lambda_c \approx 1-6\mu$$

diffusive + d-wave
 (or other anisotropic gaps)

$$\lambda_c > 1-6\mu$$

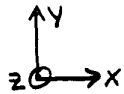
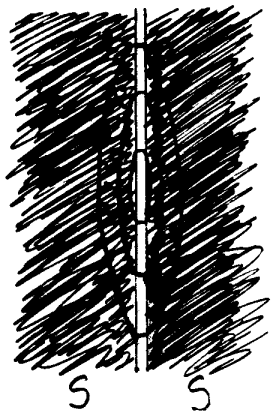
Fertig & Das Sarma
 (microscopic tight binding)

$$\lambda_c \approx 15-450\mu$$

Interlayer tunneling model $\lambda_c = 0.8-2\mu$

Images of Interlayer Josephson Vortices

Josephson vortex

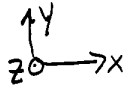
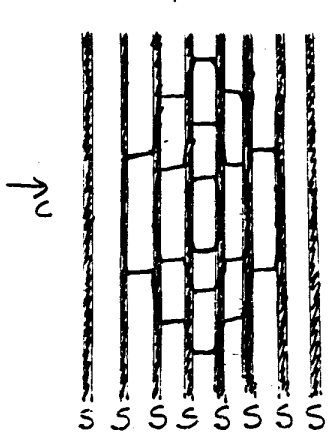


$$b_z(x, y) = \frac{\Phi_0}{2\pi\lambda_L\lambda_J} \operatorname{sech}(y/\lambda_J) e^{-|x|/\lambda_L}$$

$$\lambda_L \sim 0.2 \mu\text{m}$$

$$\lambda_J \sim \text{microns}$$

Interlayer Josephson vortex



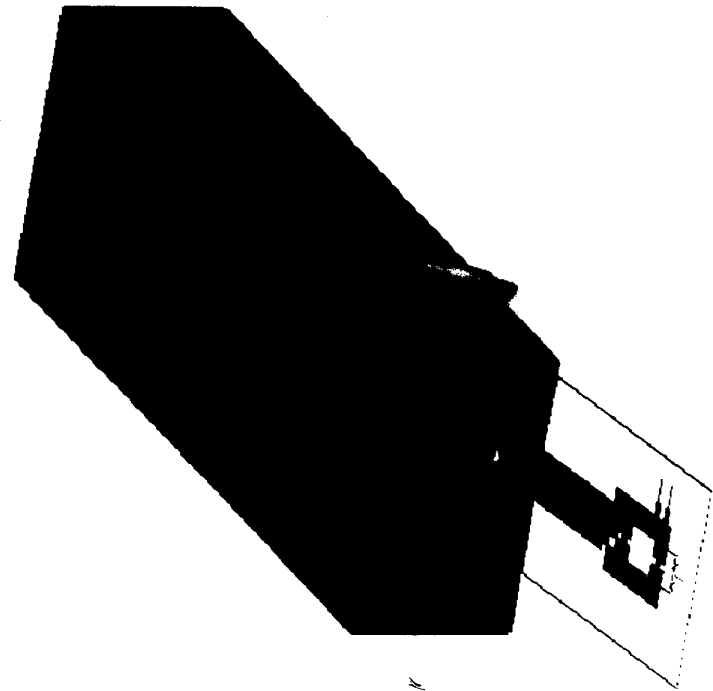
$$b_z(x, y) = \frac{\Phi_0}{2\pi\lambda_a\lambda_c} K_0 \left(\sqrt{\left(\frac{s}{2\lambda_a}\right)^2 + \left(\frac{x}{\lambda_a}\right)^2 + \left(\frac{y}{\lambda_c}\right)^2} \right)$$

$$s \sim 10 \text{ \AA}$$

$$\lambda_a \sim 0.2 \mu$$

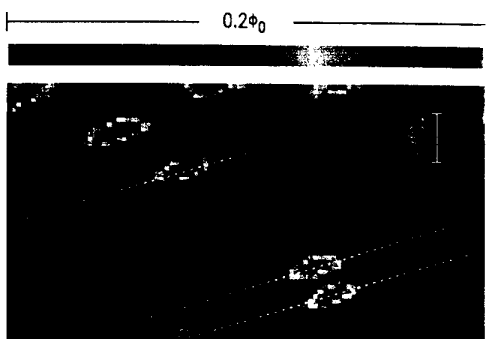
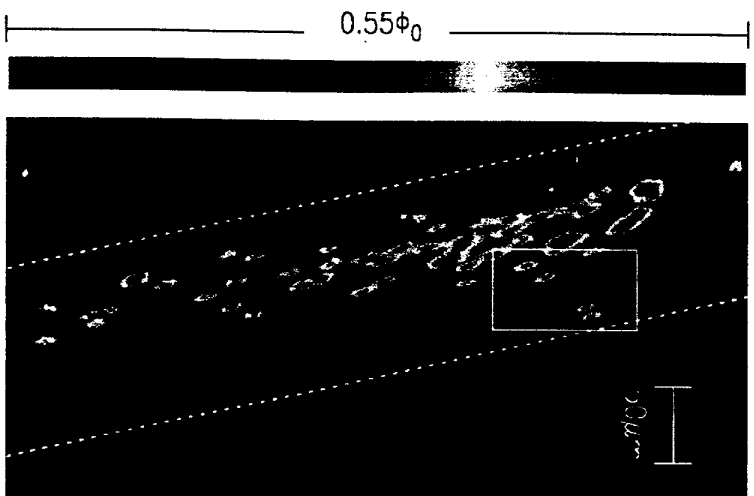
$$\lambda_c \sim \text{microns}$$

Scanning SQUID microscopy of Josephson vortices

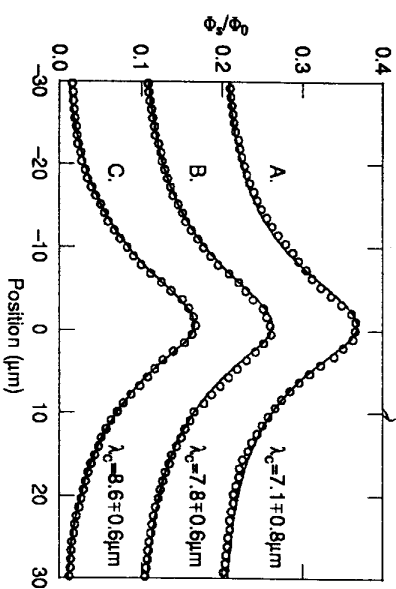


26

(Hg,Cu)Ba₂CuO_{4+δ}



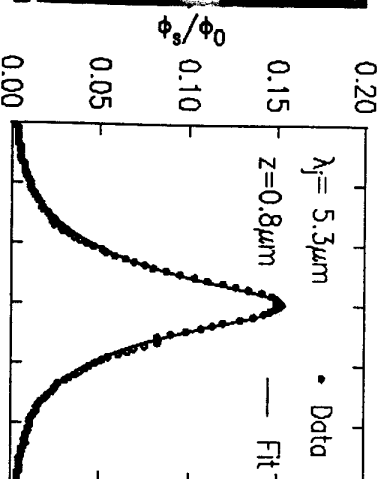
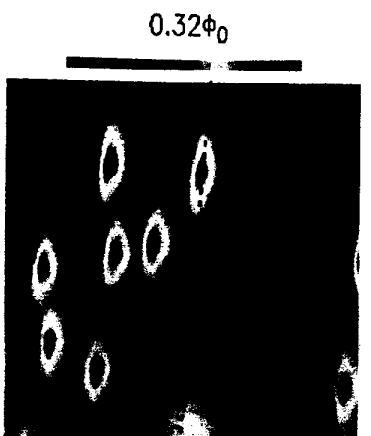
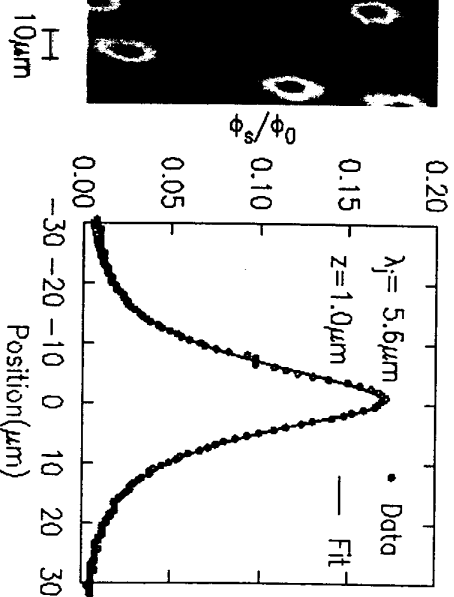
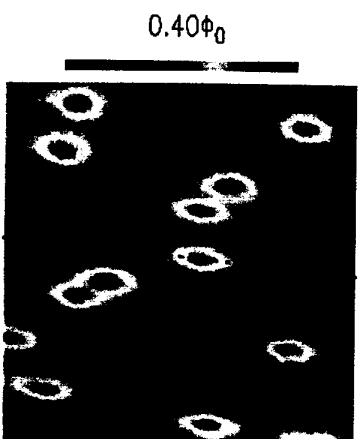
$\lambda_c = 8 \pm 1 \mu\text{m}$



KAM APS 1999

25

La_{2-x}Sr_xCuO₄



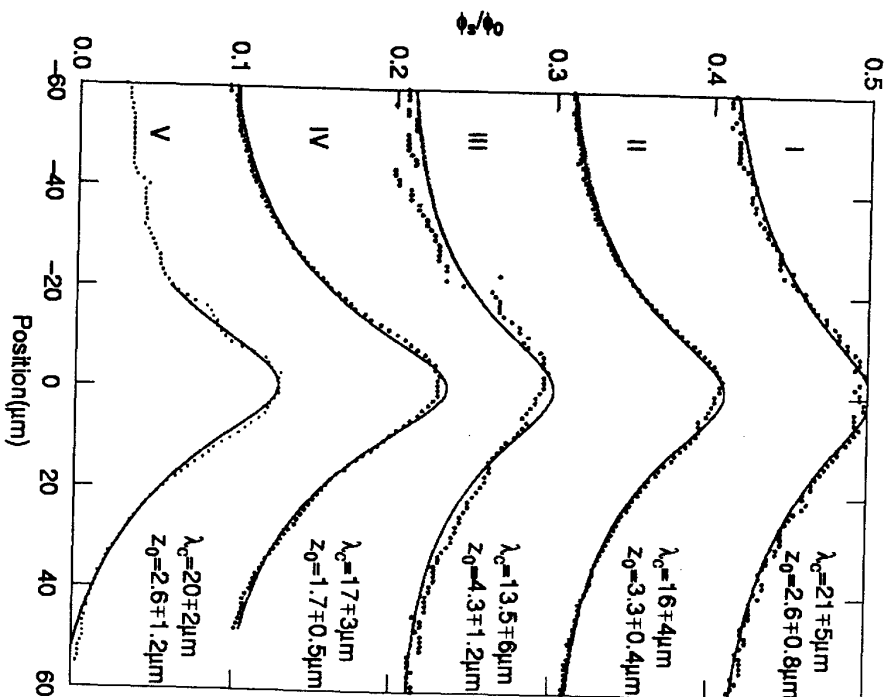
28

TI-2201 cross-section fits

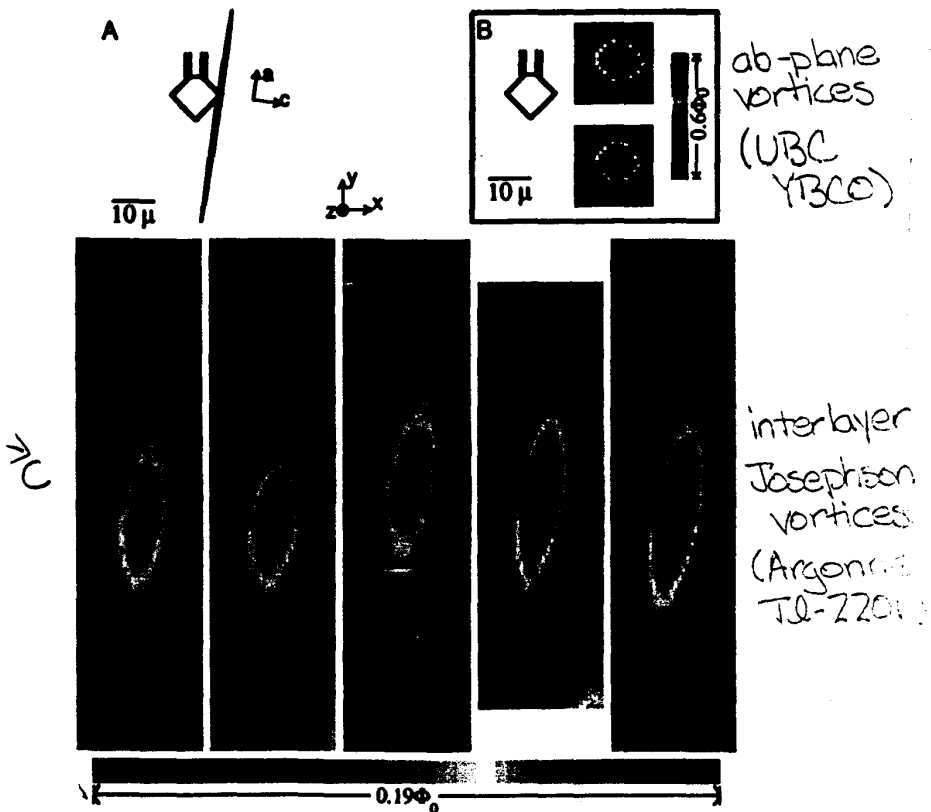
FWHM $\approx 36 \mu\text{m}$
 $\lambda_c \approx 20 \mu\text{m}$

Spreading Neglected
 $\lambda_c \approx 19 \pm 2 \mu\text{m}$

Anisotropic London
 model with interface
 $\lambda_c \approx 18 \pm 3 \mu\text{m}$



27

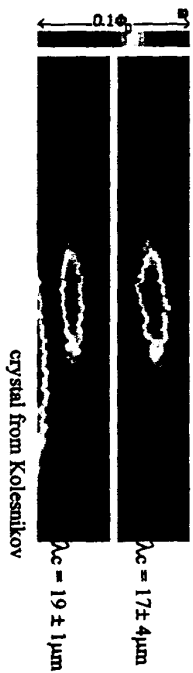


TL-2201
 Argonne
 onset T_c 90K
 midpoint T_c 77-79K
 width (10%-90%) 7-10K

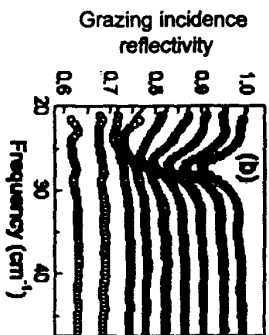
29

Are we measuring the intrinsic penetration depth in Tl-2201?

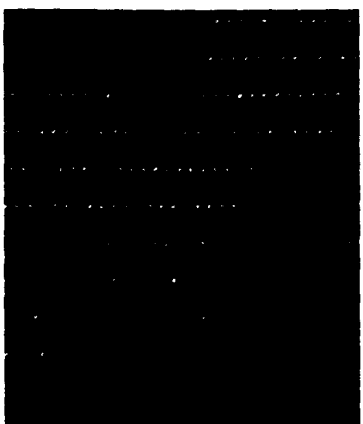
Vortices in 3 crystals from 2 groups gives consistent results with scanning SQUID microscopy.



Optical techniques give consistent results.



$\lambda_c = 17 \mu\text{m}$ Tsvetkov et al 1998 (thin films from Ren's group)
 $\lambda_c = 12 \mu\text{m}$ Basov et al 1999 (crystals from Hinks)

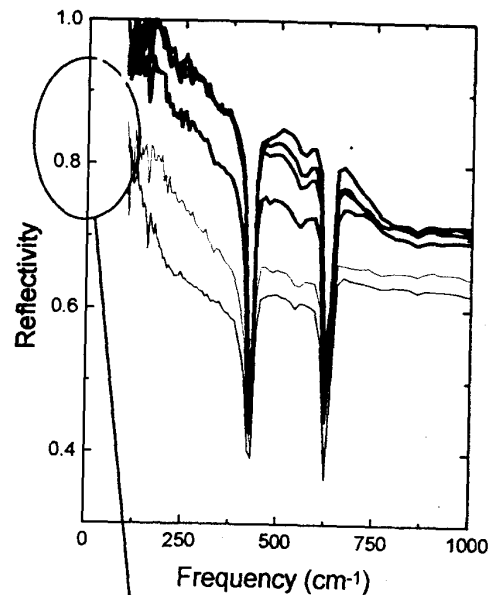


No evidence for stacking faults or superlattice structure in TEM or x-ray.

30

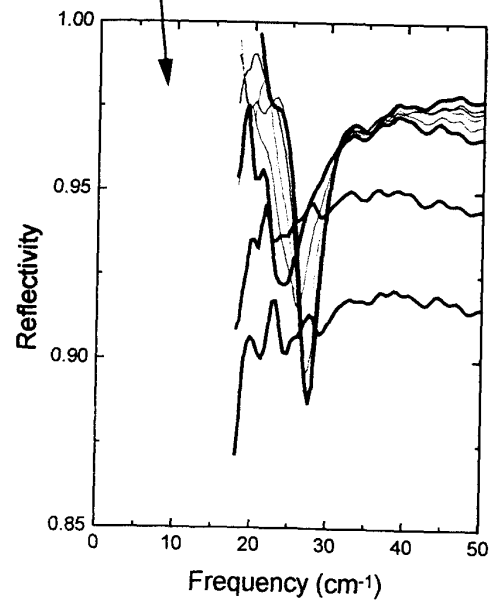
Single Crystal of $\text{Tl}_2\text{B}_2\text{aCuO}_6$

300 K
 200 K
 100 K
 70 K
 50 K
 4 K



Epitaxial Film of $\text{Tl}_2\text{B}_2\text{aCuO}_6$

90 K
 75 K
 50 K
 40 K
 30 K
 20 K
 10 K
 4 K



A. Tsvetkov et al, Groningen

Summary:

- Lawrence-Deniach provides a good phenomenological model to describe the magnetic properties of the cuprates (but leaves quantitative microscopic questions wide open)

The Inter-layer Tunneling (ILT) model proposed by P.W. Anderson and coworkers as a mechanism for superconductivity cannot supply all of the condensation energy (but this model or conceptually similar models may still play some role).

talk to Michael Tinkler at this conference...

λ_c in nominally optimally doped single-layer cuprates

	LSCO	Hg-1201	Tl-2201
λ_{ILT}	$\sim 3\mu m$ [Anderson]*	$\sim 1\mu m$ [Anderson] [†]	$\sim 1\mu m$ [Anderson]*
vortex imaging	$\sim 5\mu m$	$8 \pm 1\mu m$	$18 \pm 3\mu m$
optical ($1/\omega$)	$4\frac{1}{2}\mu m$ [Uehida]	$6\mu m$ [Basov]	$12\mu m$ [Basov]
optical (sum rule)			
optical (wp)			$17\mu m$ [van der Marel]
microwave	$4\mu m$ [Shibauchi]		
oriented powder susceptibility		$1.36 \pm 0.16\mu m$ [Panagopoulos]	
$\eta \equiv \left(\frac{\lambda_{ILT}}{\lambda_c}\right)^2$	$\eta \lesssim 1$	$\eta \sim 10^{-2}$	$\eta \sim 10^{-3}$

*Cp by Lorenn
†Cp by Charalambous