

Frustrated Magnets (III) [Balents]

• Frustrated Magnets Hunter's Guide:

(1) Is it an insulator? (from transport, ARPES)

(2) Is it a magnet? Curie Law (from χ)

(3) Sign of frustration?

$|\Theta_{CW}|$ (from χ) vs. T_N (from transition of χ , Cr, etc.)

low-T entropy (Cr) and density of states (from NMR)

(4) Identify state & compare with theory

• AB_2X_4 spinels

▲ Common valence: A^{2+} , B^{3+} , X^{2-}

▲ $X = O, S, Se$

▲ A sites form diamond lattice (which is bipartite...)

▲ B atoms form pyrochlore — decorate the plaquettes of the diamond lattice

▲ EXAMPLE: ACr_2O_4

▶ $S = 3/2$ isotropic moments

▶ dominant exchange: antiferro

▶ Zn $\begin{matrix} |\Theta_{CW}| \\ -390 \end{matrix}$ $\begin{matrix} T_N \\ 12 \end{matrix}$ $\begin{matrix} f \\ 33 \end{matrix}$

Cd $\begin{matrix} -70 \end{matrix}$ $\begin{matrix} 7.8 \end{matrix}$ $\begin{matrix} 9 \end{matrix}$

Hg $\begin{matrix} -32 \end{matrix}$ $\begin{matrix} 5.8 \end{matrix}$ $\begin{matrix} 6 \end{matrix}$

6 types :: lattice expanded

▶ Reduced f caused by increasing coupling to lattice distortions.

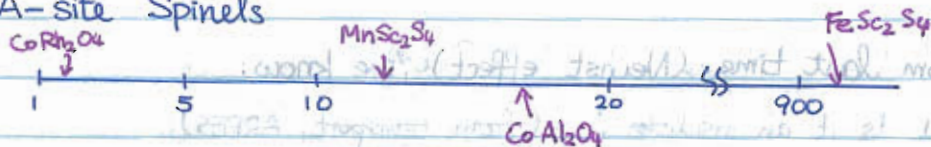
▶ Classical spin liquid — no long-ranged moment; dipolar correlation

▶ Plateaus in magnetization — 3:1 structure

▶ Plateaus caused by spin-lattice coupling, which favours colinearity.



• A-site Spinels



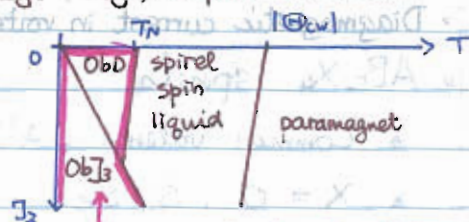
▲ In FeSc_2S_4 has $s=2$ but also has $s=2$ orbital degeneracy, which may act as $s=1/2$ pseudospin & increase quantum effects

▲ 2nd & 3rd neighbor exchange important.

► Minimal model: $J_1 - J_2$ exchange.

▲ $\frac{J_2}{J_1} = 1/8$ spiral (many degeneracy, in spiral wavevector....)

▲ Fix J_2/J_1 & introduce J_3



order by disorder. Entropy competition between patterns.

▲ Cs_2CuCl_4 — Cu^{2+} spin-1/2

$$\mathcal{H} = \frac{1}{2} \sum [J_{ij} \vec{S}_i \cdot \vec{S}_j - D_{ij} \cdot \vec{S}_i \times \vec{S}_j]$$

► quasi-D. In the 2D plane is spatially anisotropic triangular lattice

$$J > J' > D$$



► To fit neutron scattering data at 0 field to Heisenberg spin-wave theory, value of J, J' has to be adjusted by 40% in opposite direction (J, J' obtained from high-field measurement)

► Physical explanation — dimensional reduction



1st-order interchain energy correction vanishes.

Excitations include spin-1/2 spinons (~domain wall)

Spinons cannot hop between chain alone, but can

hop in pairs $\Rightarrow$ spinons tend to stay close to each other

• Quantum Spin Liquids

▲ Quantum fluctuation may prevent ordering at $T=0$.

▲ e.g. RVB states

▲ Quantum Spin Liquid

(1) $1/f = 0 \Rightarrow$ no ordering

(2) no spin freezing (hysteresis, NMR, μ SR)

(3) Structure of low-energy excitation ($\chi(T)$, $C_v(T)$, $1/T_1$, inelastic neutrons)

▲ Varieties of QSL:

(1) $U(1)$ states: (i) spinons unpaired

(ii) strong gauge fluctuations

(iii) gapless in $d=2$

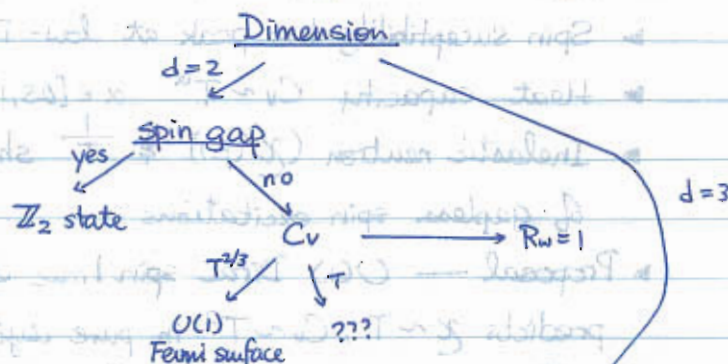
(iv) stable in $d=3$ at $T=0$ only.

(2) $\mathbb{Z}_2$ states: (i) spinons paired

(ii) weak gauge fluctuations

(iii) stable in $d=2$

(iv) Ising transitions in $d=3$.



QSL candidates

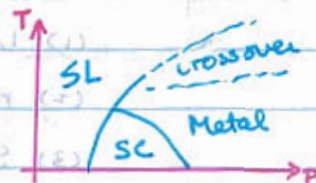


► Organic

► $S = 1/2$ triangular lattice, $t'/t \approx 1.06$
(nearly isotropic)

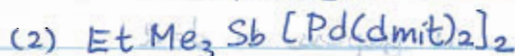


► suggestion: U(1) spin liquid with spinon Fermi surface



► $\left\{ \begin{array}{l} \text{susceptibility} \quad \checkmark \\ \text{heat capacity} \quad \times \text{ (too large)} \end{array} \right.$

► Spinon pairing?



► Less investigated than $\kappa - (\text{BEDT-TTF})_2 \text{Cu}_2 (\text{CN})_3$, but similar to it



► 2d spin- $1/2$ antiferromagnetic

► Problem — inversion between Zn & Cu (5-10%)

► Spin susceptibility has peak at low- $T \Rightarrow$ local disorder?

► Heat capacity $C_V \sim T^\alpha$ $\alpha \in [0.5, 1] \Rightarrow$ many low- T excitations

► Inelastic neutron ($\chi''(E)$) & $\frac{1}{T_1}$ show evidence of gapless spin excitations

► Proposal — U(1) Dirac algebraic spin liquid predicts $\chi \sim T$, $C_V \sim T^2$ in pure system



► Less disordered than $\text{ZnCu}_3 (\text{OH})_6 \text{Cl}_2$

► $\Theta_{CW} \approx -650 \text{K}$

► Specific heat — broad peak around 30K, power-law (exponent $1 < \alpha < 2$)

► Transport shows it a Mott insulator but close to Mott transition

Exotic Quantum Phases (III) [Continued]

► Strong spin-orbit coupling ($j=1/2$ instead of $s=1/2$)

⇒ $\chi(T)$ no longer tell low energy excitations

EXAMPLE: Bose-Hubbard
$$H = -t \sum_{\langle i,j \rangle} (b_i^\dagger b_j + b_j^\dagger b_i) + U \sum_i n_i(n_i - 1)/2$$

$t \gg U \Rightarrow$ superfluid $\quad U \gg t \Rightarrow$ Mott insulator

Approach from SF: $\Delta E \rightarrow 0$ as $U \rightarrow 0$

Approach from Mott: $\Delta E \rightarrow 0$ as $U \rightarrow 0$



Can approach by ϵ -expansion, $1/\epsilon$ expansion, Mott insulator



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EXAMPLE: rare-earth Hubbard on non-bipartite lattice

$$H = -t \sum_{\langle i,j \rangle} (c_i^\dagger c_j + c_j^\dagger c_i) + U \sum_i n_i(n_i - 1)/2$$

(no term surface) (no term surface) (no term surface) (no term surface)

