

1. (30 pts) The following three problems are not related.

(a) Find the derivative of  $y = \cos(x \sin x)$ . Leave your answer unsimplified.

(b) Find an equation for the line tangent to  $y = (x^2 + 1)(2x^3 + 3)$  at  $x = 1$ . Express your answer in point-slope form.

(c) Find  $dy/dx$  given

$$\frac{y}{y^3 + 5} = 2x^{3/2} - 3$$

by applying the quotient rule to the left side of the equation. Express your answer in terms of  $x$  and  $y$ .

2. (18 pts)

(a) State the limit definition of the derivative for a function  $f(x)$ .

(b) Let  $f(x) = 3x^2 + 7$ .

i. Use the limit definition to find  $f'(x)$ .

ii. For the given  $f(x)$ , find all values of  $c$  that satisfy the conclusion of the Mean Value Theorem on the interval  $[-1, 2]$ . You may assume that  $f(x)$  satisfies the hypotheses of the theorem.

3. (14 pts) Let  $g(x) = 2 + \sqrt[3]{x}$ .

(a) Find the linearization of  $g(x)$  at  $x = 1$ .

(b) Use the linearization to approximate the value of  $g(0.7)$ .

(c) Is the approximation an underestimate or overestimate? Be sure to justify your answer.

4. (12 pts) Timmy leaves home at 8 a.m. and walks west toward school at  $\frac{3}{2}$  m/sec. At the same time, his dog, Lassie, heads south to visit the dog park, trotting at 2 m/sec. After 8 seconds, how fast is the distance between them changing?

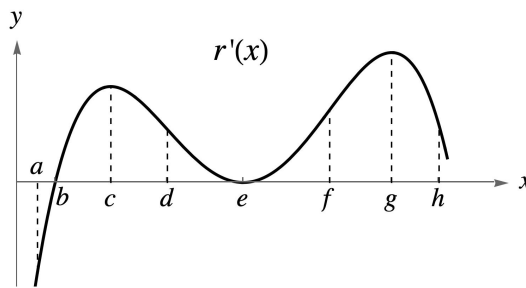
5. (26 pts) Problems 5a and 5b are not related.

(a) Let  $h(x) = (x^2 - 4)^3$ .

i. Find the critical numbers of  $h$ .

ii. Use the First Derivative Test to classify each critical number as a local minimum, local maximum, or neither.

(b) The graph of derivative  $r'(x)$  is shown below.



i. Among the  $x$ -coordinates  $a, b, c, d, e, f, g,$  and  $h,$  enter the coordinate(s) that correspond to each of the following quantities.

$\min r(x)$ at $x =$	$\min r'(x)$ at $x =$	$\min r''(x)$ at $x =$
$\max r(x)$ at $x =$	$\max r'(x)$ at $x =$	$\max r''(x)$ at $x =$

ii. At what value(s) of  $x$  does the function  $r(x)$  have horizontal tangents?

iii. On what interval(s) is the function  $r(x)$  concave up or down? Use the given coordinates as endpoints of the intervals.