APPM 1345		
Evom 2	Name	
	Instructor Richard McNamara	Section 150
Spring 2024		

This exam is worth 100 points and has 4 problems.

Make sure all of your work is written in the blank spaces provided. If your solutions do not fit, there is additional space at the end of the test. Be sure to **make a note** indicating the page number where the work is continued or it will **not** be graded.

Show all work and simplify your answers. Name any theorem that you use. Answers with no justification will receive no points unless the problem explicitly states otherwise.

Notes, papers, calculators, cell phones, and other electronic devices are not permitted.

End-of-Exam Checklist

1. If you finish the exam before 7:45 PM:

- Go to the designated area to scan and upload your exam to Gradescope.
- Verify that your exam has been correctly uploaded and all problems have been labeled.
- Leave the physical copy of the exam with your proctors.
- 2. If you finish the exam after 7:45 PM:
 - Please wait in your seat until 8:00 PM.
 - When instructed to do so, scan and upload your exam to Gradescope at your seat.
 - Verify that your exam has been correctly uploaded and all problems have been labeled.
 - Leave the physical copy of the exam with your proctors.



- 1. (25 pts) Parts (a) and (b) are unrelated.
 - (a) Find the average value f_{ave} of the function $f(x) = 9 x^2$ on the interval [0,3], and find all values of c on [0,3] for which $f(c) = f_{ave}$.

(b) Evaluate the following derivatives.

i.
$$\frac{d}{dx} \int_x^1 \sqrt{1+t^2} dt$$

ii.
$$\frac{d}{dx} \int_{\cos x}^{\sin x} \frac{1}{t+2} dt$$

2. (20 pts) The graph below represents a particle's velocity function v(t), and the corresponding position function for $0 \le t \le 6$ is

$$s(t) = \int_0^t v(u) \, du$$

The graph of v(t) consists of two quarter-circles and two line segments.



- (a) Determine the particle's position at time t = 0 and at time t = 3.
- (b) What is total distance traveled by the particle between t = 0 and t = 3?
- (c) When is the particle moving in the positive direction? Express your answer using interval notation.
- (d) When is the particle's acceleration positive? Express your answer using interval notation.

- 3. (27 pts) Parts (a) and (b) are unrelated.
 - (a) Evaluate the following integrals. Fully simplify your answers.

i.
$$\int \frac{x}{\sqrt{3x^2 + 1}} \, dx$$

ii.
$$\int \frac{\sin(3x^{1/3})}{x^{2/3}} dx$$

(b) Suppose g(x) is a continuous function such that $\int_{1}^{7} g(x) dx = 15$. Find the value of $\int_{0}^{2} g(3x+1) dx$. (*Hint:* Apply *u*-substitution.)

- 4. (28 pts) Parts (a) and (b) are unrelated.
 - (a) Consider the function $h(x) = \cos^2 x$ on the interval $I = [0, \pi/2]$.
 - i. Determine the numerical value of the Riemann sum L_2 for h(x) on I using left endpoints and 2 equallysized subintervals. Fully simplify your answer.
 - ii. Write an expression for the general Riemann sum L_n for h(x) on I using left endpoints and n equallysized subintervals. Express your answer using sigma notation.

(b) Suppose the following expression is a Riemann sum for a continuous function u(x) on the interval [-1, 2]:

$$R_n = \sum_{i=1}^n \left\lfloor \left(\frac{3i}{n}\right)^2 + 1 \right\rfloor \left(\frac{3}{n}\right)$$

Find the numerical value of $\int_{-1}^{2} u(x) dx$ by evaluating the appropriate limit of R_n . Do not use a Dominance of Powers argument when evaluating the limit. Fully simplify your answer.

END OF EXAM

Your Initials _____

ADDITIONAL BLANK SPACE If you write a solution here, please clearly indicate the problem number.

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