
INSTRUCTIONS: **Simplify** and **box** all your answers. Write neatly and **show all work**. A correct answer with incorrect or no supporting work may receive no credit. Books, notes, electronic devices (such as calculator or unauthorized electronic resources) are not permitted. **Give all answers in exact form.**

1. Write the word “agree” as your answer to question 1 to indicate that you will abide by the University honor code for this exam. An honor code violation on the final exam will result in an F in the course.

2. Simplify the following: (24 pts)

(a) $9y^2 - (2x^2 - 3y)^2$

(b) $\left(\frac{8x^4y^{-5}}{\sqrt[3]{xy^{-3}}}\right)^{-1}$

(c) $\frac{\sqrt{24a^6b^2}}{\sqrt{3a^2b^4}}$

(d) $-\ln(e^{3x}) + \log_4(8) + \log_4(2)$

(e) $\frac{\frac{1}{a} - 2a}{\frac{1}{a^2} + a}$

3. Solve the following equations for x : (20 pts)

(a) $-2 = x(x - 5)$

(b) $\frac{5}{6}x - \frac{1}{2} = -\frac{\sqrt{3}}{12}x + \frac{5}{6}$

(c) $27 = 3^{3x-2}$

(d) $\ln(x) = \ln(28) - \ln(x + 3)$

4. Consider the function $f(x) = \frac{x^3 - 2x^2 - 8x}{2x^2 - 8}$. Answer the following: (12 pts)

(a) Find x, y -coordinates of any hole(s). If there are none write NONE.

(b) Find all x and y -intercepts. If there are none write NONE.

(c) Find any horizontal/slant asymptotes. If there are none write NONE.

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5. Sketch the graph of the following functions. Label all intercepts and asymptotes as appropriate. (14 pts)

(a) $q(x) = \begin{cases} \sqrt[3]{x} & \text{if } x \leq 1 \\ 3x - 2 & \text{if } x > 1 \end{cases}$

(b) $h(x) = \sin x$ on the restricted domain $[0, 2\pi]$

(c) $k(x) = \csc x$ on the restricted domain $[0, 2\pi]$. Graph on the same axes as $h(x)$ and label any asymptotes.

6. A certain city has a constant elevation of 120 feet above sea level throughout the city. In the city, a building stands 225 ft away from you. You measure the angle from your feet to the top of the building to be 77.11° . How high is the top of the building above **sea level**? Leave your answer in exact form, do not attempt to approximate your answer. (6 pts)

7. Given $f(x) = e^x + e^{-x}$ and $g(x) = \ln(x - 2)$ answer the following. (14 pts)

(a) Find $g(3)$.

(b) Sketch a graph of $g(x)$. Label all intercepts and asymptote(s).

(c) Find $h(x) = (f \circ g)(x)$ and state the domain. Give the domain in interval notation.

8. Find the exact value: (18 pts)

(a) $\sin\left(\frac{3\pi}{4}\right)$

(d) $\cos\left(\arcsin\left(\frac{\sqrt{3}}{2}\right)\right)$

(b) $\cos\left(-\frac{7\pi}{6}\right)$

(e) $\sin^{-1}\left(\sin\left(\frac{3\pi}{2}\right)\right)$

(c) $\tan^{-1}\left(-\sqrt{3}\right)$

9. Verify the identity: $\sec \theta \csc \theta = \tan \theta + \cos \theta \csc \theta$ (6 pts)

10. Find all solutions to the following equations: (12 pts)

(a) $\cos \theta \tan \theta - 2 \tan \theta = 0$

(b) $\sin(3\theta) = \frac{1}{2}$

11. The following are unrelated (12 pts)

(a) Simplify as much as possible: $\frac{\cos(2\theta) - \cos^2 \theta}{\sin \theta}$

(b) Find the exact value: $\sin\left(-\frac{\pi}{12}\right)$

12. For $y = 2 \cos(3x)$ (12 pts)

(a) Identify the amplitude.

(b) Identify the period.

(c) Identify the phase shift.

(d) Sketch two cycles of the curve. Label x and y -values to receive full credit.

End of Exam

Formulas that may be useful:

$$1. a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$2. \text{ The quadratic formula: } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$3. \text{ Arc length: } s = r\theta$$

$$4. \sin^2 \theta + \cos^2 \theta = 1$$

$$5. \tan^2 \theta + 1 = \sec^2 \theta$$

$$6. \sin(a - b) = \sin a \cos b - \sin b \cos a$$

$$7. \cos(a - b) = \cos a \cos b + \sin a \sin b$$

$$8. \cos(2\theta) = \cos^2 \theta - \sin^2 \theta$$

$$9. \cos(2\theta) = 2 \cos^2 \theta - 1$$

$$10. \sin\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 - \cos \theta}{2}}$$

$$11. \sin^2(\theta) = \frac{1 - \cos(2\theta)}{2}$$

$$12. a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$13. \text{ Circle: } (x - h)^2 + (y - k)^2 = r^2$$

$$14. \text{ Area of a sector: } A = \frac{1}{2}r^2\theta$$

$$15. 1 + \cot^2 \theta = \csc^2 \theta$$

$$16. \sin(a + b) = \sin a \cos b + \sin b \cos a$$

$$17. \cos(a + b) = \cos a \cos b - \sin a \sin b$$

$$18. \sin(2\theta) = 2 \sin \theta \cos \theta$$

$$19. \cos(2\theta) = 1 - 2 \sin^2 \theta$$

$$20. \cos\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 + \cos \theta}{2}}$$

$$21. \cos^2(\theta) = \frac{\cos(2\theta) + 1}{2}$$