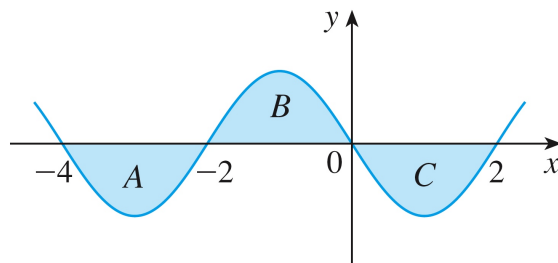


**INSTRUCTIONS:** Books, notes, and electronic devices are not permitted. Write (1) **your full name**, (2) **1350/Exam 3**, (3) **lecture number/instructor name** and (4) **SPRING 2018** on the front of your bluebook. Make a **grading table** for 4 problems and a total. Do all problems. **Start each problem on a new page.** **Box** your answers. A correct answer with incorrect or no supporting work may receive no credit, while an incorrect answer with relevant work may receive partial credit. **Justify your answers, show all work.**

1. The following problems are not related.

(a)(11pts) Suppose the acceleration of an object at any time  $t$  is given by  $a(t) = 3t^2 - 4t$  m/s<sup>2</sup>,  $t \geq 0$ . Find the velocity,  $v(t)$ , at any time  $t$  if  $v(1) = 1$  m/s. Show all work.

(b)(11pts) Each of the regions  $A$ ,  $B$  and  $C$  bounded by the graph of  $f(x)$  and the  $x$ -axis has an area of 5, see below. Find the value of  $\int_2^0 [\pi^2 f(x) - 4] dx$ .



Problem 1: Each of the regions  $A$ ,  $B$  and  $C$  pictured above has an area of 5.

(c)(4pts) Using right endpoints and subintervals of equal width, which of the limits below is equal to  $\int_{\pi}^{2\pi} \sin(x) dx$ ? (**No justification necessary** - Choose only one answer, copy down the entire answer.)

(A)  $\lim_{n \rightarrow \infty} \sum_{i=1}^n \sin\left(\frac{i\pi}{n}\right)$     (B)  $\lim_{n \rightarrow \infty} \sum_{i=1}^n \sin\left(\pi + \frac{i\pi}{n}\right)$     (C)  $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi \sin(i\pi/n)}{n}$     (D)  $\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi \sin(\pi + i\pi/n)}{n}$

2. The following problems are not related.

(a)(11pts) Suppose we want to approximate a solution to the equation  $3 \sin(x) = x$  using Newton's Method. What would the formula for  $x_{n+1}$  be? (To get full points for this question you must provide the explicit formula for  $x_{n+1}$  in terms of  $x_n$ , the generic formula for Newton's Method is not sufficient. You do **not** need to approximate the solution.)

(b)(11pts) Write the expression  $\int_2^5 f(x) dx + \int_{-2}^2 f(t) dt - \int_{-2}^{-1} f(x) dx$  as a single integral in the form  $\int_a^b f(x) dx$ .

(c)(4pts) Using differentiation, which one of the choices below can be verified to be equivalent to  $\int x \cos(x) dx$ ? (**No justification necessary** - Choose only one answer, copy down the entire answer.)

(A)  $\frac{x^2}{2} \sin(x) + C$     (B)  $\cos(x) + x \sin(x) + C$     (C)  $x \sin(x) + C$     (D)  $\frac{\cos^2(x)}{2} + C$     (E)  $\sin(x) + C$

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3. The following problems are not related. Show all work.

(a)(12pts) Use the Fundamental Theorem of Calculus to evaluate the definite integral  $\int_{-\pi}^{\pi} |3 \sin(x)| dx$ .

(b)(12pts) If  $f(x) = \int_4^{x^2} \frac{t-1}{t^2+1} dt$ , use the Fundamental Theorem of Calculus to find  $f'(2)$ . Simplify your answer.

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4. The following problems are not related. Show all work.

(a)(12pts) Use  $u$ -substitution to evaluate the definite integral  $\int_0^4 \frac{\sqrt[3]{1+\sqrt{x}}}{\sqrt{x}} dx$ . Show all work

(b)(12pts) Find the *average value* of  $f(x) = \frac{\sin(x)}{\sec(x)}$  on the interval  $[0, \pi/4]$ . Justify your answer.

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THE LIST OF APPM 1350 LECTURE NUMBERS/INSTRUCTOR NAMES FOR THE FRONT OF YOUR BLUE BOOK:

Lecture #	Instructor	Class Time	Lecture #
120	Susan HALLOWELL	MWF 9-9:50	120
130	Sujeet BHAT	MWF 10-10:50	130
150	Sujeet BHAT	MWF 12-12:50	150
170	Susan HALLOWELL	MWF 2-2:50	170
801	Sandra WILLIAMS	MWF 2-2:50	801

— END —