

1. The following are unrelated:

- (a) (8 pts) Suppose y is a function of x , find y' if $\sin(xy) = \frac{2}{3}$.
- (b) (8 pts) Suppose $f(x) = \sqrt[3]{-x + |x|}$. Find the derivative of $f(x)$ for all $x < 0$.
- (c) (8 pts) Find $\frac{d^2y}{dx^2}$ at $x = \frac{\pi}{4}$ if $\frac{dy}{dx} = x \sec^2(x) + \tan(x)$.
- (d) (8 pts) For a differentiable function $g(x)$, find $\frac{d}{dx} \left(\frac{g(x^2)}{x} \right)$.

2. (26 pts) Consider the function $y = x\sqrt{2+4x}$, with domain $\left[-\frac{1}{2}, \infty\right)$, to answer the following.

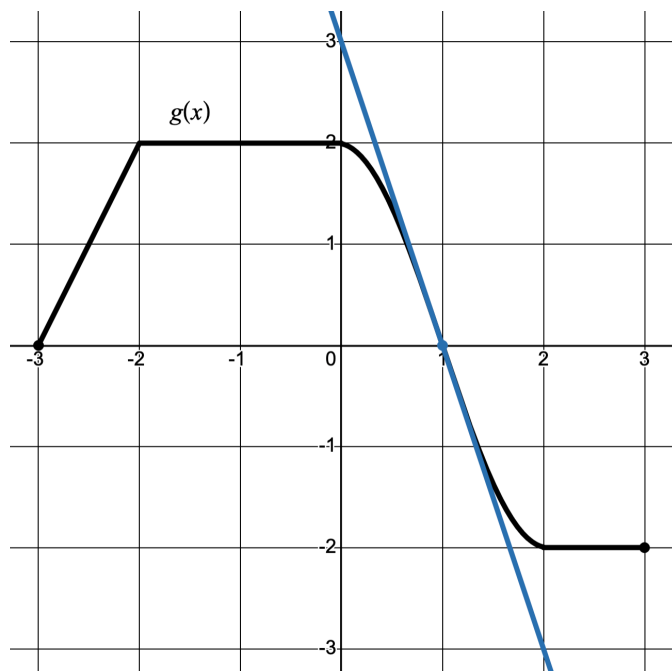
- (a) Find the x and y -intercepts of the function.
- (b) The first derivative is $y' = \frac{2+6x}{\sqrt{2+4x}}$. On what intervals is y increasing? Decreasing?
- (c) Find x and y coordinates of the local maximum and minimum extrema, if any.
- (d) Find the absolute maximum and absolute minimum values of y on the interval $\left[-\frac{1}{2}, 3\right]$.

3. (12 pts) For two resistors, R_1 and R_2 , connected in parallel, the combined electrical resistance, R , is given by $(R)^{-1} = (R_1)^{-1} + (R_2)^{-1}$ where R , R_1 , and R_2 are all functions of time and are measured in ohms. Suppose R_1 and R_2 are each increasing at a rate of $\frac{1}{2}$ ohms per second. At what rate is the combined resistance, R , changing when $R_1 = 2$ ohms and $R_2 = 4$ ohms?

4. (8 pts) A company, Better Boulder Dice (BBD), is going to produce new metallic dice in the shape of a cube. Suppose x represents the edge length of a metal cube.

- (a) The volume of a cube is $V(x) = x^3$. Find dV , the differential of V .
- (b) The edges of each cube are designed to have a length of 2 cm, but the machine creating the cube produces edge lengths of 2.01 cm. Use differentials to estimate ΔV , the difference between the designed volume and the machine-produced volume.

5. (22 points)



Shown above is the graph of $y = g(x)$ and the tangent line to g at $(1, 0)$. The function is differentiable on $(-3, -2) \cup (-2, 3)$.

- Sketch the graph of $y = g'(x)$. Clearly label the tick marks.
- Use the linearization of g at $a = 1$ to estimate the value of $g(1.3)$.
- The mean value theorem states that there exists a value of c in $(-2, 3)$ such that $g'(c)$ equals a certain value.
 - What is the value of $g'(c)$?
 - Suppose we wish to narrow down the possible values for c . In which of the following six intervals can c be found? Circle all possible answers. No explanation is necessary.

$(-3, -2)$

$(-2, -1)$

$(-1, 0)$

$(0, 1)$

$(1, 2)$

$(2, 3)$