

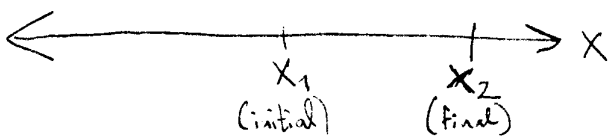
(Quickly review velocity, speed)

If speed & velocity can vary with time, we can define

instantaneous vs. average (mean) velocity.

$$\text{Average velocity} = \bar{v} = \frac{\text{change in position}}{\text{change in time}} = \frac{\Delta x}{\Delta t}$$

$$= \frac{x_{\text{final}} - x_{\text{initial}}}{t_{\text{final}} - t_{\text{initial}}}$$

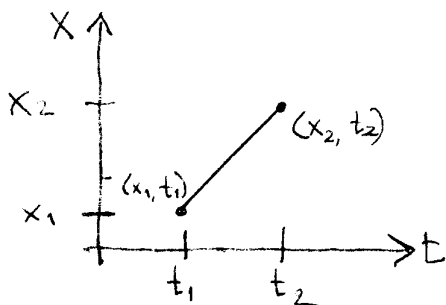


$$\bar{v} = \frac{x_2 - x_1}{t_2 - t_1}$$

so if x_1 had been final position and x_2 initial, \bar{v} would change signs.

$$\Delta x = x_{\text{final}} - x_{\text{initial}} = \text{"displacement"}$$

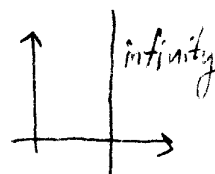
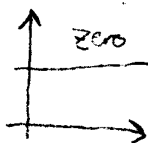
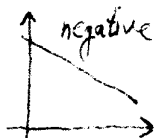
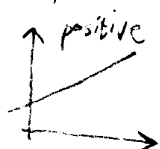
Now, think of plotting x vs. t : note x is the vertical axis here.



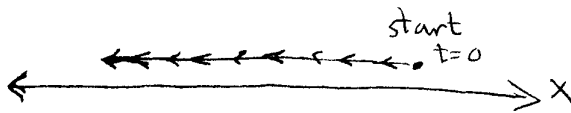
$$\text{Recall slope} = \frac{\text{rise}}{\text{run}} = \frac{x_2 - x_1}{t_2 - t_1}$$

So \bar{v} is the slope of the line connecting (x_1, t_1) with (x_2, t_2) .

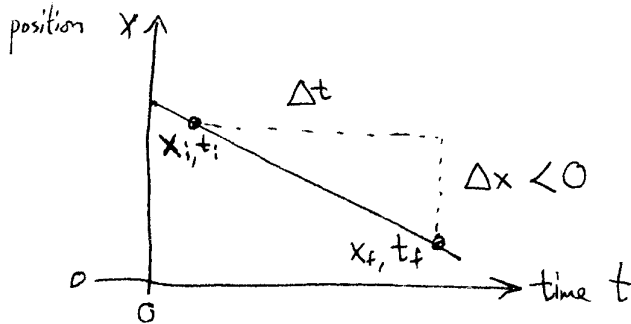
slopes:



Now, plot an object traveling at constant $v < 0$ (i.e. constant speed in the $-x$ direction):



The plot has negative slope:



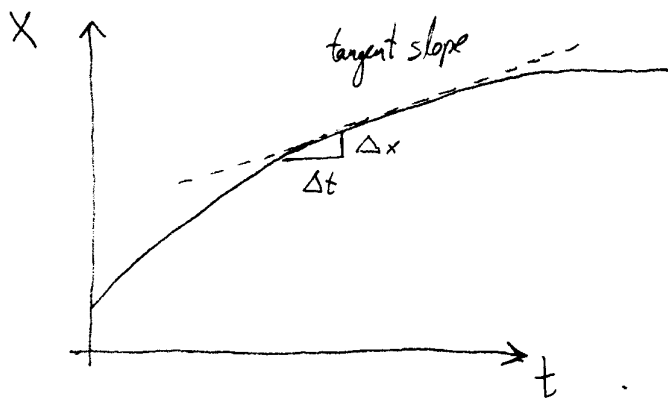
constant v :
straight line!

[Concept test 2-2:]

Now, velocity can change smoothly in time too.

[Concept test 2-3]

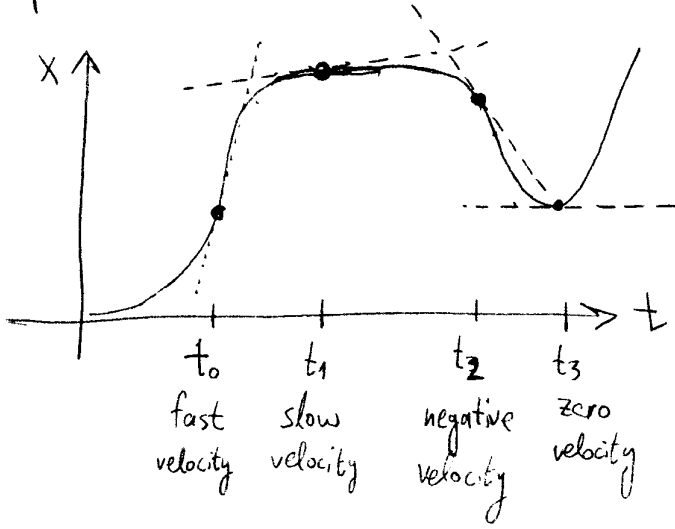
Look more closely at the plot in previous concept test:



The slope of the curve at a given t is the instantaneous velocity of the object at that time! (average v over a very short time)

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \text{slope of line tangent to the curve.}$$

Examples:



[concept test 2-5]

