

Intro to Mechanics
GEEN 1400-040
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Consider a bar clamped to the edge of a table, so the tip can move. The deformation can be described by

$$x = \frac{FL^3}{3EI}, \text{ thus } F = \frac{3EI}{L^3} x$$

where

x	Movement at tip; displacement
F	Applied force
L	Length of bar
E	Young's modulus, a material property that describes springiness
I	Rectangular moment of inertia; $I = \frac{bh^3}{12}$
b	Base; width of bar
h	Height; thickness of bar

Young's Modulus E: Approximate values, and density

Steel	30 x 10 ⁶ psi	7.86 g/cc
Aluminum	10 x 10 ⁶ psi	2.7 g/cc
Brass	15 x 10 ⁶ psi	8.5 g/cc
Copper	17 x 10 ⁶ psi	8.96 g/cc
Wood	1 x 10 ⁶ psi	0.6 g/cc
Glassy plastic	250 x 10 ³ psi	1.4 g/cc

For a bar with simple supports on the ends, and an applied force F in the center

$$x = \frac{Fl^3}{48EI}, \text{ where } x \text{ is the maximum displacement at the center.}$$

For a tube with inner and outer diameters d_i , and d_o , moment of inertia

$$I = \frac{\pi}{64} (d_o^4 - d_i^4)$$

For a box section, compute I for a solid box, then subtract I for the empty internal space.